THE CRAFT OF MUSICAL COMPOSITION

by

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BOOK I
(FOURTH EDITION)
Theoretical Part

English Translation by
ARTHUR MENDEL

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CHAPTER I

Introductory

"Perhaps some will wonder at my undertaking to write about music, when there are at hand the opinions of so many excellent men who have written learnedly and sufficiently about it, and particularly at my doing so at a time when Music has become an almost arbitrary matter, and composers will no longer be bound by laws and rules, but avoid the names of School and Law as they would Death itself . . ."

Thus wrote Johann Joseph Fux in the foreword to his Gradus ad Parnassum (1725),* the textbook of counterpoint according to whose basic principles the student to this day still learns his craft. Now for us the first decades of the 18th century represent the fullest flowering of the technique of composition. When Fux’s book was published, J. S. Bach was forty years old, and at the summit of his skill and creative power; and the minor masters who were to be found all over Europe exhibited even in works which were by no means heaven-storming a complete technical mastery. But Fux, the strict contrapuntist, whose field is vocal music, cannot reconcile himself to the shift of the center of the composer's work to the instrumental domain, with all that that shift implies for the style of writing. The step from the noble but narrowly limited art of writing for voices, in which instruments must always play a secondary rôle, toward freer and livelier tone-progressions

* "Mirroruntur fortassis nonnulli, cùm tot præstantissimorum virorum existent monumenta, qui de Musica perquæd doctè, & abscondentur scripserunt, cur ego ad hoc scribendi genus me contulerim, hoc maxime tempore, quo, Musicâ ferè arbitrariâ factâ, Compositores nullis præceptis, nullisque institutis obstringi volentes, Legum, ac Schola nonem ad mortis instar exhorrescunt; . . ."
such as naturally occur to the gifted instrumentalist, appears to him not as the beginning of a path into a new land, but as a descent which must be halted. How in both word and deed he opposed what he considered the barbarization of music may be seen both in his compositions and—with explicit reference to the master of the purest and most perfect style of writing, Palestrina—in the Gradus.

Perhaps the craft of composition would really have fallen into decline if a genius like Bach had not fought his way through to the highest and most complete mastery of his material, and if Fux’s Gradus had not put a brake upon caprice and exaggeration, and set up a standard of excellence in writing. For this was the first real textbook of composition in a time which had known on the one hand only the passing on from master to pupil of specific devices and tricks of the trade, or, on the other, deep-searching theoretical works that were of little help in learning the practical art of composition.

A musician who feels called upon in these times to contribute to the preservation and transmission of the craft of composition is, like Fux, on the defensive. He is, in fact, even more so than Fux, for in no other field of artistic activity has a period of over-development of materials and of their application been followed by such confusion as reigns in this one. We are constantly brought face to face with this confusion by a manner of writing which puts tones together according to no system except that dictated by pure whim, or that into which facile and misleading fingers draw the writer as they glide over the keys. Now something that cannot be understood by the analysis of a musician, making every conceivable allowance for individual characteristics, cannot possibly be more convincing to the naive listener. In Die Meistersinger one reads, it is true, that the composer must make his own rules and then follow them. But this privilege is granted only to a master—one, moreover, who knows, or at least feels, the bases of his work provided by Nature.

It is not surprising that things have developed as they have. The discovery, in the last century, of the extreme limits of power and subtlety in the effect of musical tone extended the boundaries of the tonal domain at the disposal of the composer into hitherto undreamed-of distances. New combinations of tones came to be recognized, and new ways of bending a melodic line were discovered. It seemed as if the sun had risen upon a new, glowing, iridescent land, into which our musician-discoverers rushed headlong. Blinded by the immense store of materials never used before, deafened by the fantastic novelty of sound, everyone seized without reflection at whatever he felt he could use. At this point instruction failed. Either it fell into the same frenzy as practice, and devoted itself to flimsy speculation. Instead of adapting its systems of teaching to the new material, or it lapsed into inactivity, and what had never been a very strong urge towards novelty turned into a barren clinging to the past. Confidence in inherited methods vanished; they seemed barely adequate now to guide the beginner’s first steps. Whoever wished to make any progress gave himself unreservedly to the New, neither helped nor hindered by theoretical instruction, which had simply become inadequate to the occasion.

A considerable portion of the responsibility for the failure of instruction belongs to the instructors themselves. Is it not strange that since Bach hardly any of the great composers have been outstanding teachers? One would expect every musician to have the desire to pass on to others what he had labored to acquire himself. Yet in the last century the teaching of composition was looked on as drudgery, as an obstacle in the way of creative activity. Only rarely did a composer integrate it as a component part of himself; the feeling of responsibility for future generations of musicians seemed to have become a thing of the past. Not until the last few decades do we again find composers who feel it their duty to educate pupils. These men act in the spirit of the old handicraftsmen, who aimed to hand on their skills intact. In times that boast of an enviable flowering of the craft of composition, great masters can afford to devote themselves exclusively to their own creations, paying no attention
to those who are to come after them. It is then the task of the teachers, who follow at a distance, to mint into current coin the wealth which the composers have mined. But today, when there is a general lack of skill in the technique of composition, no composer should withdraw from teaching.

There are two types of theorists: the teaching composer, and the avowed specialist in teaching musical theory. A gifted composer is not always a good teacher. But his instruction is bound to have a certain creative warmth, even when the composer is of modest gifts, because he is passing on directly what he himself has experienced. This is not true of the usual theory instruction, such as is given in most schools. The specialist who gives such instruction without himself being gifted for composition is in a difficult position. In the painful early stages of trying to bring dry series of figured basses and sets of rules to life, he cannot fall back upon his own creative activity. Thus he is likely to turn this most interesting of fields, which lies directly adjacent to that of free composition itself, into a morass of disappointment, instead of exploiting the many stimuli it offers for the better understanding of past and present styles of composition. Not every theory teacher can reach that high estate of knowledge and ability attained by the teachers (and textbook writers) of the last century, for they owed the richness of their harvest to the fact that composers had left the field of instruction to them. But he can at least prevent the theory lesson from becoming what students too often consider it: a boring, incomprehensible, and useless burden. And is it really any more than that when it consists in handing out “music” in the form of dead chord-progressions and monotonous, meaningless melodic lines?

The teacher must not base his instruction simply on the rules of textbooks. He must continually refresh and complete his knowledge from the practice of singing and playing. What he teaches must have been developed out of his own exercises in writing. For it is his task not only to teach the pupil a correct technique, but also to help him obtain a comprehensive musical education, seeing to it that his work in the practical fields is supplemented by an intelligent understanding of the theoretical side. It is up to him to pass

on the most personal and most painfully arrived at secrets of the great composers, so that he may call forth in the student at least a small reflection of their light. At the same time, he must exercise a guiding and calming influence on the young musician who is in the throes of experiment; he must steer him between the Scylla of blind worship of the past and the Charybdis of idolatry of the present. Anyone who follows this profession for the sole purpose of earning his living is just as unworthy of it as is the (fortunately not too common) composer who submits unwillingly to what he considers the slavery of teaching, and poisons the student with his inevitable musical bad temper.

One thing that makes instruction in this field more difficult is the unfortunate fact of its division into two separate parts. Of course the material must be presented to the student in easily graspable form; exercises for the development of melodic invention must alternate with those for the acquisition of a cogent harmonic style, just as the student of an instrumental technique employs both finger exercises and pieces for performance in learning to master his instrument. But complete separation of the harmonic material, followed after a whole year of work by melodic studies which are themselves insufficient, is as thoroughly wrong as would be a method of skating in which one had to practise exercises for working each leg separately before one learned to move on the ice.

In Fux's time, it was possible to get along with the material he worked out. But when the technique of composition developed further, particularly on the harmonic side, the teaching of harmonic phenomena and their treatment was set off in a separate field known as Harmony. This took place about the beginning of the 19th century (although it was based upon much research of earlier times). In this procedure, the new progress in composition seemed to have found the educational method appropriate to it. But that method soon turned out to be inadequate, and after barely a hundred years of an apparently brilliant existence, the fabric, which from the beginning has needed patch after patch, is now worn threadbare. On the other hand, the Fux system has lasted two hundred years, and is still passed on from teacher to student almost in its original form
—a grotesque state of affairs when one realizes that the practice of composition has long since forsaken the bases of this system. This fabric was never patched; it was made of more durable stuff. In fact, the stuff was so durable that it might well have been ripped out and worked over again. But no successors came to adapt its basic principles to new needs. Some were for greater strictness, and stripped Fux of an ornament here and there; others added new spangles to the old garment. But the truth is that no matter what is done to make it more presentable, it no longer fits our needs, and the want of something more suited to our own problems has long been felt.

If, then, every music student must go through these two courses of study, adapting himself painfully at first to the one, only to be torn away from it before he is really used to it and then have to begin all over again on the other, finally to realize that even when he has mastered the new discipline he has acquired no real mastery over his tonal materials—is it any wonder that the idea should arise that a composer should not let himself be disturbed by what he has learned in his theory lessons?

It is in the nature of such a teaching procedure that in the case of an unusually gifted student there comes a day when the teacher can no longer follow the activities of his pupil. He does not understand what the student is aiming at—although in technical matters there can be no secrets—and, as is touchingly described in many biographies, he lets him depart with his blessing, since there is nothing more he can teach him. Unfortunately for the teacher, in most cases the pupil comes to this conclusion on his own account, and does not wait to be dismissed.

Because of the situation described above, it is a particularly difficult task today to give a student instruction in composition. One teacher sticks close to what he has had handed down to him. For him what Riemann or Prout said is iron-bound law. His pupil learns the old styles of writing: he can modulate, write counterpoint almost in his sleep, from the first species to the florid fifth, and construct fugues to order, made according to the text-book rules, and containing anything but music. If the precocious student seeks to know more, mentioning that in the music he plays and hears there is more to be discovered, he is hushed up, or given excuses, false explanations, or denials; or the teacher becomes angry; or relations between pupil and teacher are broken off altogether. Or, on the other hand, the teacher may let the pupil flounder around in a field in which both are lost. But none of these ways brings the pupil any nearer to his goal.

Among the younger teachers—who have themselves experienced the impact of the new music on their own work, and now wish to spare the pupil the things that once caused them pain, anger, and disappointment, without arming them for later struggles—many allow the pupil considerable freedom from the start. But freedom is a bad thing at the beginning, since it does not provide the student with the necessary support. A conscientious teacher, who can hardly justify to himself the process of continuing to dispense outworn materials, is in a perpetual state of uncertainty, since no usable new method is at his disposal. How, in particular, shall he treat the more advanced student? He can settle technical problems with him only by relying on nothing more substantial than his taste, citing his own opinion and that of other honest seekers, and exploring the situation with the student. None of these solutions will do except the last, and this can be fruitful only if the teacher and pupil are sympathetically attuned, and both of exceptional gifts. But no general system of instruction can be based on such a happy combination of circumstances.

If confusion in the technique of composition is not to increase and spread, if the conflicting results of an outworn system of instruction are not to bring disaster in the wake of uncertainty, a new and firm foundation must be constructed.

I propose to attempt the construction of such a foundation. I am not animated by any desire to freeze into permanent shape what I
have been teaching for years, either to get it out of my system or to be rid of the burden of continually improvising new forms of the material which I have often handed out. Anyone who has for years taught students who wish to know why the masters are free to do what is denied to them, why one theme is good and another poor, why harmonic progressions may be satisfactory or irritating, why sense and order must prevail even in the wildest turmoil of sounds, and why such order cannot be arrived at with the traditional tools; anyone who has not sidestepped this unending struggle with the Why of things, and, at the risk of laying himself bare before his pupils, has taken each new question as a stimulus to deeper and more searching study—anyone who has faced these issues, I say, will understand why I feel called upon to devote to the writing of a theoretical work the time and trouble which I would rather spend in composing living music.

I have experienced the needs of the teacher as well as the strivings of the composer. I have lived through the transition from conservative training to a new freedom perhaps more intensely than anyone else. The new land had to be explored if it was to be conquered, and everyone who took part in this process knows that it was not without danger. The path to knowledge was neither straight nor smooth. Yet today I feel that the new domain lies clearly spread out before our eyes, that we have penetrated the secrets of its organization. This was not accomplished by the stubbornness of those who simply put up a pretense of strength by persisting in their accustomed disorder, or by those who were so self-righteous that they never experienced temptation. Anyone who is familiar with the development of music after the first World War will find step by step in these pages, which are intended to afford entrance to the newly won territory, traces of struggle with external circumstances as well as of that inner strife whose aim is the perfection of one's own work. But even a wider circle of readers will understand, at this first stopping-place on the road to complete clarification of both contemplation and action, that an attempt to explain the music of the present day had to be undertaken, if only to satisfy a personal need to pass on to new learners what had been acquired by learning, and to shorten for them the paths which until now have been inevitably roundabout.

I address myself above all to the teacher. True, I cannot (as is understandable in the case of a composer whose theorizing is only incidental and enforced) offer him a book of rules, polished down to the last detail, in which he can simply assign to his pupils three pages per lesson. Perfection cannot be attained at the outset of an innovation such as the present one, and the comprehensive working out of the material presented here will require the efforts and the experience of many musicians. The teacher will find in this book basic principles of composition, derived from the natural characteristics of tones, and consequently valid for all periods. To the harmony and counterpoint he has already learned—which have been purely studies in the history of style: the one based on the vocal style of the 16th and 17th centuries, the other on the instrumental style of the 18th—he must now add a new technique, which, proceeding from the firm foundation of the laws of nature, will enable him to make expeditions into domains of composition which have not hitherto been open to orderly penetration.

To the composer, as well as the teacher, the book offers new perspectives on his materials, and makes clear that for a well-intentioned but arbitrary arrangement of sounds he must substitute an order which only to the uninitiated will seem a restriction of the creative process. In reality, wisely and sensibly directed work will result in greater variety than a profusion of over-seasoned or over-sweet progressions, the formula for which is soon transparent and thus available even to those who have no inner musical vocation.

The reader who lightly turns these pages in the hope of a stimulating general discussion will not be well rewarded. He will find the subject matter remote and dry, the more so as he is used to meeting the materials of music in living and flowering form, rather than on the dissecting table. Moreover, he finds more pleasure in the actual sound of music than in reading about it, and thus he may well leave the present accumulation of descriptions of abstract tone-successions, practical rules, and musical examples to those who can feel
the pulse of music beneath the monotonous consideration of its materials.

Those industrious ones, too, who think that by memorizing and working hard at rules and precepts they will come by a recipe for producing convincing music had better give up the search. Finally, this book would represent a disappointment to the beginner who expected to find in it a reliable guide for self-instruction. It presupposes a considerable body of knowledge, and will therefore be valuable only to those who are already somewhat familiar with the technique of composition.

In the present Theoretical Part of this work, the underlying principles of the new theory are first established and then developed. I have limited myself to what is really new, and to that older material to which I give a new interpretation. Such elements of older theories as have remained intact throughout all periods and styles, because they are independent of period and style, I have left untouched, except where it has been more convenient to rename or reclassify them. Nothing is said here about those things which remain unchanged, or about the actual writing of music, with its rules for voice-leading, spacing, and so on. Book II, devoted to actual writing in two parts, contains all this material, both old and new, presented in pedagogic order.

In Fux's foreword, the following additional passage occurs:

"The practice of medicine is intended for the sick, not for the well—although my work does not aim, and I do not lay claim to the power, to control the current of a gushing stream that has overflowed its banks, or to reconvert composers from their heretical way of writing. For aught I care, everyone may follow his own fancy."*

But despite Fux's modest estimate of his powers, he actually did do away with heresy. His "gushing stream" seems to us, compared with the torrential flood of today, a mere overflowing mountain brook. Perhaps a single man's strength will not suffice today to dam the flood; perhaps what he attempts will not even be understood, much less valued. Yet the success of Fux's work shall be a good omen for mine.

The reader who thinks that the views here expressed amount to a deification of materials, an undue exaggeration of the importance of mere craft, should remember that there was once a time when he had to absorb the rules of harmony, which, despite the limitations of the chordal material dealt with, were numerous enough. There is no denying the fact that to learn a new system takes time and trouble. But if one gains both a wider outlook and a more complete mastery, it is worth it. Technical skill can never be great enough. No one is too able or too accomplished to learn more than he knows. Technique must be learned as a child learns to move his limbs: what was difficult at first must become easy; it must be at one's instantaneous disposal; it must function so perfectly that its action is no longer noticed; it must sink to the level of sub-conscious activity.

Although the creative process in its highest stages may always remain hidden from human comprehension, as may the mysterious source of artistic work in general, yet the dividing point between conscious and unconscious work can be raised to an extraordinary degree. If this were not true, everyone in whom this point lies at a very low level could assert that he is creating the greatest works of art. There would be no difference between Beethoven and any other composer, who had with difficulty achieved a mere quarter, say, of the height of artistic achievement that men may attain, and knew nothing of the other three quarters that still lay above him. Such a little man would not care to speak of technical matters, but would instead refer to his impulse, his feeling, his heart, which had prescribed the way for him. But must not this impulse be tiny and this feeling negligible if they can express themselves with so little knowledge? Is not an immense mastery of the medium needed to

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translate into tones what the heart dictates? Can the inner vision of the music that the composer has glimpsed make itself at all clear to another if the resistance of the tones and the refractoriness of tonal progressions is continually coming between the impulse and its expression in sound?

The road from the head to the hand is a long one while one is still conscious of it. The man who does not so control his hand as to maintain it in unbroken contact with his thought does not know what composition is. (Nor does he whose well-routined hand runs along without any impulse or feeling behind it.) The goal must always be such mastery that technique does not obtrude itself, and a free path is prepared for thought and feeling. The man to whom the tones are a necessary evil with which he must wrestle; or who sees in them a perfectly tractable medium in which he can express himself without any restraint; or who climbs up on them as on a ladder, or wallows in them as in a bog—such a man is simply adding to the infinity of pieces that are written every year without moving a human ear or spirit. The initiated know that most of the music that is produced every day represents everything except the composer: memory, cheap compilation, mental indolence, habit, imitation, and above all the obstinacy of the tones themselves. Our principal task is to overcome the latter. To do this we need precise knowledge of the tones and of the forces that reside in them, free from aesthetic dogma and stylistic exercises such as have characterized previous methods of instruction, but leading the composer rather according to natural laws and technical experience.

In this attitude toward the technical side of composition I am in agreement with views which were held long before the classic masters. We find such views in early antiquity, and far-sighted composers of the Middle Ages and of modern times hold firmly to them and pass them on. What did tonal materials mean to the ancients? Intervals spoke to them of the first days of the creation of the world: mysterious as Number, of the same stuff as the basic concepts of time and space, the very dimensions of the audible as of the visible world, building stones of the universe, which, in their minds, was constructed in the same proportions as the overtone series, so that measure, music, and the cosmos inseparably merged.

And the art of composition itself? To pious musicians it was a means of praising God, and of enabling the community of listeners to take part in that praise. That the work has been created to the glory of the Highest Being, of whose support it is thus assured, we can feel in the music of many composers—above all in that of Bach, whose "Jesu iuva" in his scores was for him no empty formula.

We cannot conjure up past times, although every man must come to some agreement with himself about the bases of his work. But that our consideration of tonal materials and its application by all who may concern themselves with it may catch a kindling spark from the spirit of the old masters is the hope from which this work springs.
CHAPTER II

The Medium

1

General Considerations

If we were to ask an intelligent musician, who knew his métier and who had a certain theoretical knowledge, what tones he would choose from among the audible range, what series he would consider the most natural, the simplest, and the most practical raw material for composition, he would undoubtedly reply after a moment's thought that we must mean a scale, for without a scale no ordered music would be conceivable. He would be thinking of the major and minor scales, which provide an inexhaustible supply of tones for all possible harmonic combinations, and according to which all melodies known to him can be classified. He would be forgetting, however, that our ancestors made use of other scales, and that even today peoples of other cultures use scales that often have little similarity to ours.

Even the simplest musical activity, uninfluenced by education or experience—the song of the savage, or the first attempts to draw tones out of a hollow bone or a reed pipe—must make use of some interval-progressions which are based fundamentally on a series of adjacent tones. The primitive musician, giving direct expression to his mood, will at first not be interested in the exact distance of one tone from another. Not until considerable experience has broadened his knowledge and raised the level of his desires will he feel the need of bringing order into the luxuriant tonal wilderness.

It will then develop that certain intervals make similar impressions upon all men. When even the man of the lowest level of civilization hears the interval of an octave, he will feel that the upper note is the higher image of the lower. Accordingly, in all known tonal systems, the basic scale-patterns, with few exceptions, fill in the space between two tones an octave apart.

After the octave, the next fixed point to be felt is the fifth. But the conception of this interval as something fixed and unchangeable is for the untrained ear a more difficult matter. The two tones do not merge completely into one sound, as do those of the octave. The upper tone is not felt, as is the upper tone of the octave, to be the mere higher duplication of the lower. Nevertheless, the interval of the pure fifth is so unambiguous and independent that it is to be found in almost every scale system. Other intervals (thirds, sixths, sevenths, and seconds) are less easily determined. The distance between the two tones of a major sixth, for example, can be diminished or augmented to a certain extent without destroying the impression of a major sixth. The slightest alteration in the size of an octave or a fifth, on the other hand, changes these intervals completely, so that the ear perceives them only as greatly expanded sevenths and fourths or greatly contracted ninths and sixths.

2

Overtones

We find the intervals embedded in the tonal raw material which Nature has made ready for musical use, consisting of an infinite number of tones, from the deepest barely perceptible drone to the whistle that lies at the other limit of audibility. Into this inchoate tonal mass we can introduce a certain order by the use of the immutable measures of the octave and the fifth. Nature, in fact, has herself introduced this order, and put at our disposal a whole series of other intervals as well.

The eye perceives in light which has been split up by a prism a natural series of vibration frequencies. The light of the sun always produces the same immutable series of colors, familiar to us in the rainbow. Now, just as light consists of graduated colors of the
spectrum, so a tone consists of many partial tones. The spectrum of the world of sound is the harmonic or overtone series. A tone produced by a voice or instrument carries with it a greater or lesser number of barely audible overtones. Their order is not arbitrary: it is determined by a strict law, and is as immutable as the color series of the rainbow. The series extends theoretically to infinite heights, but in practice a sounding tone is supported by only a limited number of overtones. It is well that this is so, for a tone accompanied by all the possible overtones, to the upper limit of audibility, would be obscured by their profusion, would lose its character, and would suffocate. Bells of poor quality, with their great number of prominent overtones, give us an idea of what such an overloaded tone would be like. For theirs is a chaos of tones, rather than a single tone, and as such it is of almost no use for musical purposes.

A tone completely devoid of overtones, on the other hand, is characterless. It has no profile; no expression. It cannot be produced on our musical instruments. A completely pure tone of this sort can be produced only electrically by means of an oscillator or similar apparatus. It is of virtually no musical value. Even tones which are relatively poor in overtones are not used in practical music, as the almost pure tones of tuning forks show. The soft, insipid tones of recorders of medium register, for example, or of the similar labial pipes of the organ, are of good effect only in combination with sharper tone-colors (i.e., those richer in overtones). Our musical instruments, of which the larynx is one, produce their tone by the joint action of vibrating solid bodies, which in turn cause the air to vibrate. All the vibrating parts of the instrument possess one or more tones proper to them, as we can observe by tapping the wood of the violin or the brass of the trumpet. Such tones are inseparably connected with the principal tone produced by the instrument. Even if the latter were free of overtones, the tones proper to the material of which the instrument is made would be heard along with it.

The overtones accordingly have an important relation to tone-color. The latter depends not only on the nature of the material and construction of the instrument producing it, but also on the manner in which its vibrations are excited: the articulation, the manner of drawing the bow, the touch, all have an important influence on the distribution of the overtones. Every tone-color corresponds to a certain grouping of the overtones. The ear hardly hears them separately; it only perceives the disappearance of some or the addition of others as changes in tone-color.

3

Nature of the Overtone Series

In order to study the nature and construction of the overtone series, we shall take the structure based on the fundamental tone C as the basis of our observations:

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<td>String-lengths (C = 1)</td>
<td>( \frac{1}{2} ) ( \frac{1}{3} ) ( \frac{1}{4} ) ( \frac{1}{5} ) ( \frac{1}{6} ) ( \frac{1}{7} ) ( \frac{1}{8} ) ( \frac{1}{9} ) ( \frac{1}{10} ) ( \frac{1}{11} ) ( \frac{1}{12} ) ( \frac{1}{13} ) ( \frac{1}{14} ) ( \frac{1}{15} ) ( \frac{1}{16} )</td>
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We know that this fundamental tone supports a series consisting of the octave, the fifth of the octave, a second octave, the major third of the latter, the octave of the earlier fifth, and so on, as illustrated by Fig. 1. The spaces between the individual overtones thus grow progressively smaller, in arithmetical series. If we assume a frequency of 64 vibrations per second for the fundamental tone C (a convenient and usual basis for reckoning, even though the C actually used in our music nowadays is somewhat higher—i.e., has a somewhat faster vibration rate)—then the second tone of the series will vibrate 128 times per second, the third 192, and similarly each tone will have 64 more vibrations per second than its predecessor in the series. The octave has twice as many vibrations as the fundamental, the twelfth three times as many, the double octave four times.
The air-vibrations upon whose duration the duration of a tone depends, whose wave-length determines its pitch, whose amplitude governs its intensity, and whose shape gives rise to its color, are in turn dependent for their dimensions upon the size and period of motion of the vibrating solid body which produces them. To find out about the form and tempo of the vibrations, we must examine the body which generates them. The most useful such body is the string. If we stretch a string over a sounding board, and provide it with a sliding bridge, we have the ideal instrument for measuring tone—the monochord, which has been used by musical theorists since antiquity.

To produce the octave of the tone proper to the whole length of the string—that is, to double its vibration rate—we must place the bridge exactly in the middle, so as to divide the string into two equal parts. Half of the string-length vibrates twice as fast as the whole; one third vibrates three times as fast, and so on:

On both sides of the bridge which has been placed in the middle of the string we hear the octave of the tone produced by the whole string. If we wish to compare the string-lengths and the pitch-relationships of the two tones of this octave interval, we may imagine two monochord strings of the same measurements, of which one vibrates as a whole and the other in two halves. The two tones an octave apart are then related as 1 (1 string-length) to 2 (2 equal divisions of the string-length), written 1:2. If the string be divided into thirds, each third produces the twelfth of the tone of the whole string. The interval of a fifth may thus be expressed 3:2. One string is divided into 3 equal parts (and accordingly produces in each of its parts the tone g, assuming the tone of the whole string to be C); the other is divided into two halves (each producing c); and the difference is the perfect fifth (c-g). Or, in terms of the overtone series: the interval of a fifth is produced by the second and third overtones.* (Accordingly, the fifth between the fundamental C and the G above it, since it lies an octave lower and would be produced by string-lengths twice as great, would have to be expressed $\frac{3}{2}:\frac{3}{1} = 1\frac{1}{2}:1$.) If we continue to subdivide the string, we arrive at the proportions 4:3 for the fourth, 5:4 for the major third, 6:5 for the minor third, 5:3 for the major sixth, 8:5 for the minor sixth, and so on for all the intervals which occur in the overtone series.

The strings of stringed instruments offer a true parallel to the monochord when they are used to produce harmonics:

* It is customary to call the fundamental number 1 of the overtone series; this makes the octave number 2, the twelfth number 3, and so on.
in which the part of the string which lies below the stopping finger is excluded from the production of tone—and the partial tones correspond exactly to those of the monochord, and consequently to the overtone series. The division into halves produces the octave, into thirds the twelfth, into fourths the double octave, etc.

The nature of the overtone series may also be easily observed in wind instruments. Those brass instruments which are so-called “natural” instruments (e.g., the bugle, post horn, hunting horn, Alp horn) sound the overtones of their fundamental, although only a small part of the series is used. The use of valves makes possible the addition of extra lengths to the tube, so that the ranges of the instruments are extended at the bottom.

Effect of the Valves of the B♭ Trumpet

Upon each of the tones thus added there rises the overtone series proper to it. The new overtones thus gained serve to fill in the gaps between the overtones produced by the original, unaltered tube, and thus make possible the playing of a scale. In trombones, the length of the tube is increased directly, by sliding part of it out, instead of by valves.

On our present-day brass instruments, players can reach about the 10th overtone, and on the lower instruments they can play some still higher in the series. Woodwind instruments, on the other hand, are confined to the first three or four overtones, produced, as on the brass instruments, by more intense blowing (“overblowing”, sometimes with the help of the so-called octave keys).

Overblowing on the (Boehm) Flute

Quarter-notes indicate the fundamental tones which, when overblown, produce the pitches indicated above them.

The scale is here arrived at not by lengthening but by shortening the tube. To fill in the gaps between the tones of the overtone series produced by the whole tube, holes are opened which prevent the air from penetrating to the further end of the tube. The air column is thus shortened, it vibrates correspondingly faster, and creates new and higher fundamental tones whose overtones are also produced by overblowing.
The Triad

Tones 1–6 of the overtone series (comprising the octave, fifth, fourth, and major and minor thirds)

with their higher octaves (the two-fold, four-fold, and eight-fold multiples of their order-numbers, frequencies, and proportions) outline the extended major triad, which is to the trained and the naive listener alike one of the most impressive phenomena of nature, simple and elemental as rain, snow, and wind. Music, as long as it exists, will always take its departure from the major triad and return to it. The musician cannot escape it any more than the painter his primary colors, or the architect his three dimensions. In composition, the triad or its direct extensions can never be avoided for more than a short time without completely confusing the listener. If the whim of an architect should produce a building in which all those parts which are normally vertical and horizontal (the floors, the walls, and the ceilings) were at an oblique angle, a visitor would not tarry long in this perhaps “interesting” but useless structure. It is the force of gravity, and no will of ours, that makes us adjust ourselves horizontally and vertically. In the world of tones, the triad corresponds to the force of gravity. It serves as our constant guiding point, our unit of measure, and our goal, even in those sections of compositions which avoid it.

Must not then a music which consists exclusively of triads provide the highest delight? Pieces of this description, such as those of early Italian choral music, do not, as a matter of fact, belong among the greatest revelations; their uninterrupted sweetness is apt to bore even the gentlest listener. Hence a master like Palestrina sees to it that in his works the slight tension that resides in continuous triad successions is increased many times by melodic means, by suspended and passing tones, and thus a real tonal ebb and flow is created even in the absence of passionate outbursts. Our aural nerves, as the result of the intensity of modern life and the surfeit of sounds, are very taut. Our ears take pleasure in music of a low degree of tension as a historical phenomenon, just as our eyes enjoy the quiet beauty of early painting. But of contemporary music they expect sterner emotions. They not only can stand passages without triads, they actually demand them. How great the span can be between triads is a question of the hearing habits of the listener and of the ingenuity of the composer. But from all the evidence it would appear that there is in the ear itself, apart from all questions of habit and ingenuity, a certain limit of irritability which it does not seem advisable to exceed by means of a music too far removed from nature—that is, from the triad. The awkwardness of a composer who cannot put together a convincing series of sounds, and the over-intelligence which, for fear of the commonplace, will not put a single triad on paper—both preclude any feeling of oneness with the work of art just as does the slanting floor of the “interesting” architect.

The feeling for the purity, the harmonic completeness, and the satisfying effect of the triad, which is the same as the unerring judgement in the aural measuring of the octave and the fifth, is accordingly just as natural to us as the body’s sense of space. It is based on the nature of the ear itself. The senses of sight and feeling need to make use of memory and comparison in order to arrive at even approximate judgements of size and proportion, and our sense of the passage of time similarly does not permit us to make exact estimates. The ear, on the other hand, is the one sense organ that is unerring in its sense of measurement and proportion. The eye is like a mirror that reports faithfully and distinterestedly on what is before it. But the ear is like a fabulous sieve, that not only sorts what it receives into large and small, but measures it exactly. It hears simple ratios as beautiful and correct sounds, and it recognizes perfectly that the purity of the octave, the fifth, or the fourth is clouded when the proportions of length or vibration frequency are not in the ratios of 1:2, 2:3, or 3:4. In the Cortian organ it literally possesses a minute frequency meter, each tiniest part of which is
attuned to a certain vibration rate, and responds to a certain wave- length. When vibration combinations in the simple ratios of 1:2, 2:3, or 3:4 strike this organ, they excite particular parts of its harmoniously designed structure, which distills from the feeling of correctness the most intense pleasure. This basic fact of our hearing process reveals to us how closely related are number and beauty, mathematics and art.

The seventh overtone in the series based upon C (C '_b') does not make the triad into a dominant seventh chord such as we know in practice. It is flatter than the bb that we are used to hearing as the seventh of C. Why we do not use the natural ratio 1:7 (or rather, 4:7) will be explained later.

Like the seventh overtone, the higher prime-numbered members of the series and their multiples do not fit into our tonal system. They also are either too flat or too sharp (indicated in our illustrations by the signs - or +)—although we must remember that it is only for simplicity’s sake that we can let that statement stand. The natural tones of the overtone series cannot of course be “too sharp” or “too flat” in themselves. It is just that our tonal system, which strives to bring incomprehensible multiplicity within our grasp, cannot find any simple and clear place for them. In acoustical reckoning, so far as it serves as a basis for considerations of composition, one does not need these prime numbers, or the “pure” tones which lie above the 16th in the overtone series. No theory of music that is to be taken seriously has ever gone beyond the series 1-16, and we shall see in the course of our investigations that an even smaller portion of this series suffices to represent all the tonal relations used in music.

5
Paths to Scale-Formation

The overtone series in its raw state is not usable for musical purposes, on account of the constantly decreasing distance between its adjacent tones. For the melodic endeavor that has been known to man from time immemorial, in the simplest form of musical ac-

[ 25 ]
requirement that must be met by a system designed for polyphony: the possibility of having two lines proceed in parallel motion. Even the simplest music will not always, it is true, move in parallel motion; yet the possibility of occasional parallels must not be limited to a few parts of the scale: it must be present everywhere. (The organum of the Middle Ages is only a preliminary step towards true polyphony; in the strict form of the uninterrupted coupling of voices it was rather the object of investigation by theorists than a type of living music.)

The next most important interval after the octave, the fifth, opposes considerable resistance to continuous parallel motion. As we shall see later, the uninterrupted connection of perfect fifths destroys the purity of the octave. But we cannot give up so important an interval altogether, and therefore we adopt it as the central pillar of our scale. With it we adopt the fourth, which is of course only the octave transposition of a fifth below the original tone.

Every octave will be filled out in exactly the same way as every other, so all we need is the scale pattern for one octave. In the following pages, the octave C-c is chosen as the range of the scale. To fill in the spaces between the first tone and the fourth, and between the fifth tone and the octave, there are several possible procedures. One of them seems to be indicated by the overtone series itself, for between the 8th and 16th overtones there is a scale-like formation

\[\text{\textbf{Diagram of scale-like formation}}\]

which contains the octave and the fifth, but not the fourth. On a wind instrument that can produce this series of the overtones of its fundamental, the 11th overtone, which is too high for the pure fourth, can easily be lowered by altering the embouchure, and the other tones can be similarly altered to fit. This practice was actually current for a long period; the so-called "Klarinblasen" on the trumpet, which existed up to Bach's time, was nothing else. But the continual tempering of the tones results, especially in fast tempi, in a good deal of uncertainty, and it is effective only in this one octave, since the overtones in the octave below do not form a continuous scale, and since not more than the first two or three tones of the octave above are attainable by human lips and lungs. This series of tones has been of importance in musical practice, but not in musical theory.

Another method is more productive. It, too, goes back to earliest experience in instrument-playing, for it takes its departure from the fingerboard of stringed instruments. The inherent tonal sense will lead the primitive player almost always to tune two adjacent strings in fifths or fourths; only after considerable harmonic experience are other intervals used for tuning. Now when he wishes to climb up from one open string to another a fifth or a fourth above, filling in the intervening space by finger by finger—that is, stepwise—he will divide this space either according to the convenient placing of his fingers, or according to mathematical considerations. If he then transfers the divisions thus found to the next higher string (and to others still higher) he has achieved a usable scale. The Arabian tonal system, with its highly developed theory of music, rests on such calculations. Scales so arrived at are admirable material for monophonic music, purely melodic in conception, while for polyphonic music they are practical only to a limited extent, since for the sake of identical fingering on all strings—carrying with it the possibility of parallel motion throughout—purity is neglected. The intervals formed by the tones of the scale do not all have the same proportions as their prototypes in the overtone series. But in polyphonic music, the measuring ear continually seeks the pure intervals of the overtone series, and is dissatisfied not to find them. And to the extent that scales of this sort do contain pure intervals besides the fourths and fifths, their immovable rigidity prevents any free harmonic development. Polyphonic music demands that the tones may at any time be able to change their tonal significance, by relating themselves to changing roots (either of chords or of overtone series). A tone that has, for example, already served as a third must be able to become root, fifth, or seventh in succeeding chords. It is, however, impossible, as we shall see, for one tone to perform all these functions without change of pitch. Thus
either the purity of nature must be disregarded or the pitches must be movable, which would take away from this type of scale its most characteristic feature.

6

Tempered Tuning

There is no solution of the scale riddle that can reconcile these opposite necessities. Purity must be neglected or the possibility of unhindered polyphony sacrificed. It is thus astonishing that one of the most inspired inventions of the human spirit should have been arrived at by the space-dividing method just described: the chromatic scale in equal temperament, such as we know on our keyboard instruments. It, too, is necessarily a compromise, but the sort of compromise represented in commerce by the use of money in place of barter. The small change of music, the twelve-tone series of the equally tempered scale, has become the musician's universal medium of exchange. Except for the octave, not a single one of its intervals is exactly equal to a pure interval of the overtone series; even the fifth sacrifices something of its value. But the difference is just big enough for the ear to perceive it without being disturbed by it in polyphony.

At the same time, the ear is subject to a certain danger in being exposed only to music constructed of tempered intervals; it accustoms itself to their clouded qualities, and like a jaded palate loses its sense of natural relations. Fortunately, however, the instruments and voices which can produce pure intervals are in a majority over the keyboard instruments, and we need hardly assume that musical sensitivity will ever sink so low as to allow keyboard instruments undisputed mastery. Yet their advantages are invaluable. Apart from their special tonal effect, it is they that first made possible to us full and unimpeded mastery over the entire tonal domain. But the fact that practical music makes a distinction between keyboard and other instruments (although the distinction is not very sharp) testifies to our realization of the fundamental irreconcilability of the two. Compared with orchestra music, or chamber music for strings or winds or combinations of the two, the literature in which the piano or organ is combined on an equal footing with other types is not very large. More often the keyboard instrument is subordinated, as in the piano accompaniment to a song; or it is contrasted as a solo instrument with the body of the others, as in the concerto for piano or organ. A sensitive string player will always find greater pleasure in chamber music for strings alone than in music with piano, and the latter seems the less pleasant, the more stringed instruments are set against the piano. In piano quartets and quintets, the group of instruments capable of pure intonation holds the balance even against the tempered instrument. Adjustments of the movable tuning to the fixed, which can be made in smaller combinations, are hardly possible in such groups. That is why this field of music, which shows the discrepancy at its most striking, has been little cultivated, even to the present day. The pitches of a single instrument capable of pure intonation, on the other hand, are easily adapted to the piano (which "gives the pitch") although mostly without the player's being conscious of the fact. Thus works for such combinations are numerous: they offer the composer the advantage of covering a great deal of harmonic ground with only two players.

7

Earlier Attempts at Scale-Formation

In our discussion of "Klarinbläsen" (the use of the upper overtones of the trumpet) we saw that the direct taking over of the "scale" in the fourth octave of the overtone series does not lead to a satisfactory result. Even the use of tones from still higher portions of the series would not help, unless a selection were to be made from among the latter, and they were all to be transposed down five or six octaves to the same register. But such a selection, in the absence of any suggestion from the nature of the overtone series, could be only a matter of individual taste; and if one is to proceed arbitrarily one has no need of handling such refractory material as the upper reaches of the overtone series.
Attempts were accordingly made in early times to derive laws for scale-formation from the proportion of the simplest intervals, that is, from the lower portions of the overtone series. One well-thought-out system was devised in ancient Greece: the Pythagorean. It requires that a fifth (the ratio 2:3 of the overtone series) be established on either side of a given tone. This results in the above-mentioned establishment of the fifth and fourth as the backbone of the scale. The fifth below the given tone is transposed up an octave to give the fourth within the octave in which the scale is to be constructed. The ratio 1:2, which, being the first interval of the overtone series, has priority over all the others, does not produce any new tones in such calculations, but simply enables us to transpose already existing tones, and thus makes it possible for us to gather within the space of one octave tones which were originally far apart. Above the fifth C-G and below the fifth F₂-C let us now construct another pair of fifths; this procedure can be continued as far as one wishes. But it need not be continued very far. For any seven-tone section of such a series of fifths will yield, when its widespread tones are gathered close together by means of octave transposition, a seven-tone scale made up of whole-tone and half-tone steps which will answer many requirements.

We can arrive at approximately the same result if we apply the interval originally existing between the fourth and the fifth—the major second—above and below each of our original four tones: the given tone, fourth, fifth, and octave. Such a scale includes tones, however, that do not form intervals corresponding to those of the natural series. Thus in the seven-tone Pythagorean scale starting from C with 64 vibrations per second, the E is too high:

This is owing to the downward transposition of the fourth fifth above C, the e with 324 vibrations, which is four vibrations higher than the fifth overtone of C (e with 320 vibrations). This very striking discrepancy in so important an interval as the third (the "syntonic comma") makes the Pythagorean scale unusable for polyphonic music.

Now if one continues indefinitely adding fifths in an upward direction (setting up the circle of fifths), one is headed for infinity, for with the twelfth fifth a tone is reached which is also a comma higher than the octave of the original tone:

The next octave of the scale would have to be based on this tone (transposed down), which would be too high, and each succeeding octave would begin correspondingly too high. Thus the connection with the given tone would be lost. The ear is easily reconciled to impure fifths, if the discrepancy is very slight, as the equally tempered scale shows; but it would not accept impure octaves.
In order to avoid the disadvantages of this reckoning in pure fifths, the ratio 4:5 was introduced into the calculations: that is, the scale was no longer erected by superposing fifths only, but by the use of pure fifths in combination with major thirds. (We need not consider the ratio 3:4, of course, since the superposition of fourths would simply arrive by the opposite method at the same result as that of fifths.)

The scale thus arrived at offers the greatest number of intermediate tones of pure intonation; the third, particularly, now corresponds to the natural third. Although the remainder in the reckoning cannot be done away with, but must always obtrude itself in an impure interval, it is here at least not allowed to cloud the octave or any of the other most important intervals. Just as in one's home one places an unwanted object in some dark, out-of-the-way corner, so the comma is now placed in an interval that is not often used. Thus if C is the given tone, it will be least disturbing if the minor second or the augmented fourth is made the victim. The Db or the F~ is then so out of tune that it cannot be used in an important place. Before the introduction of equal temperament, which took place during Bach's lifetime, keyboard instruments were tuned according to this system. Many varieties of the system were suggested, differing fundamentally only in the placing of the bad tone.

Anyone with a good ear who knows nothing of these things will be very much surprised by his experiences in trying to tune a piano. He will tend to be guided by his ear, joining one pure fifth to another; and by the accumulation of pure intervals he will go so far astray that in the end he will have achieved by great pains a tuning at least as bad as that he originally set out to remedy.

New Proposal

I now suggest a new method* for erecting a scale, which will lead us to goals that could not be attained by the method above described. From what has been said, it is evident that I shall neither conjure away the comma nor suggest new structures of tempered series. I shall simply follow the suggestions which to the understanding ear lie hidden in the overtone series, and shall thus arrive at a simple and natural construction of the scale.

Construction by means of series of fifths and thirds does not represent a primeval method of erecting a scale. One is simply taking the scale already present in practical music and trying to explain the intervals of the series, which have already demonstrated their usefulness. What other reason would there be for the quite arbitrary ordering of the fifths and thirds? Or for the setting up of intervals like the Pythagorean third, which have so little correspondence with anything in nature? A more rational procedure gives up the attempt to measure every interval with the same unit.

Let us imagine ourselves back in the time of the creation of our tonal building materials. We know at this point only the single tone. We discover above it the overtone series, and feel our way gropingly up it, step by step. When we come to know the second tone of the series, we can learn something about it by comparing it with the original tone. When we come to the third, we have already had the experience of two, and with each succeeding overtone the possibilities of comparison increase.

We start again from the C that has 64 vibrations per second. From the second tone, the c with 128 vibrations, we cannot draw any important conclusions. If we give it the same rights that accrue to its progenitor, C, by virtue of the latter's place at the root of its overtone series, then c (128) becomes the fundamental of a new series, which reproduces the first series an octave higher, but without other change. We thus take it as the upper limit of our scale.

Let us now consider the third overtone, g, in the light of our knowledge of the two earlier tones. We could assign to it, too, the rôle of the first tone. It would then serve as the fundamental of a new overtone series, but as such, it would lie outside the octave C-c which we have set ourselves as the space within which we wish to erect our scale. But if we take this g as the second tone of an overtone series (that is, assign to it the rôle played by the c in the
first series), it becomes the octave of a fundamental, to which it is related as 2:1. To arrive at this new fundamental, we divide the frequency of the g (192) by 2:

\[
\text{The result is } G (96). \text{ We may thus adopt the following rule for our procedure:}
\]

\[
\text{To arrive at each new tone of the scale, divide the vibration-number of each overtone successively by the order-numbers of the preceding tones in the series.}
\]

This formula gives us the key to all the remaining calculations. Anyone who has followed the path which we have taken from C through g to G will have no difficulty in understanding the origin of our tonal planetary system.

Let us apply the measures already discovered to the next overtone of C, namely c' (256). If we take it as the upper tone of the relation 2:1, we obtain, by halving its vibration-number, a tone we already have, c (128). But if we take the c' as the third overtone of a series—if we assume that it bears a relation to a fundamental like that of the g to the C (3:1)—we shall divide the vibration-number of the c' (256) by 3, and obtain the tone F (85.33):

\[
\text{We treat the fifth overtone, e' (320), similarly. As the upper tone of the ratio 2:1 it belongs to the fundamental e, a tone which lies outside the octave we wish to fill in, and is accordingly of no use to us. But if we treat it as the third overtone, and divide its frequency by 3, we obtain A (106.66). And if we treat it as the fourth overtone, we obtain E (80):}
\]

The g' (sixth overtone, 384), if treated as the second overtone, yields a tone (g, 192) which lies outside our octave. As the third, it yields the c which we already have as the second overtone of C. As the fourth, it again yields only a tone which we already have—the G. But by dividing it by 5 we obtain an addition to our series—Eb (76.8).

The seventh overtone is a special case, as we shall see. It thus draws a boundary-line above the six tones already considered. Let us then, before proceeding to its consideration, subject the first six overtones to a still closer scrutiny. Up to this point, we have treated each one as if it stood one or more places lower in the overtone series than it actually does. Now let us adopt the opposite path. This is a procedure of the second order. It is not based upon the experience which we gather step by step in going from one tone to the next, and which accordingly permits us to use at each new level only the relations which lie below it. Rather, it uses the sum of the experiences gathered in attaining the levels reached thus far (up to and including the sixth overtone), in that it considers the relations into which each successive tone of the original series could enter if it were considered to lie higher in a series (but not higher than the sixth overtone). This is no arbitrary procedure. Having set the upper limit of our calculations at the sixth overtone (because of the special nature of the seventh), and having treated each overtone with the measures of those preceding it in the series, there is no other way to arrive at new scale-tones except to apply to each of these overtones all the other proportions.

The third overtone, g, may thus be taken as the fourth, fifth, and sixth overtones of new series:
The fundamental tones of these series add nothing to what we already have. The $G_1$ (48) which results from dividing 192 by 4 is already represented by its octave, $G$ (96); likewise the $\text{Eb}_2$ (38.4), produced by the division by 5. Finally, division by 6 produces only $C_1$ (32), of which the octave is the $C$ (64) with which we started. We cannot, of course, change the scale-tones which we have achieved through our calculations (and which, be it noted, are now to be considered fundamentals, not overtones). But upward transposition by an octave constitutes an exception to that statement, since it produces nothing new except the second overtone, which is already present, in sound as well as in theory, and which can therefore belong to our scale just as much as its fundamental.

The frequency 256, belonging to the fourth overtone, $c^1$, is now to be divided by 5 and by 6:

\[
\frac{256}{5} = 51.2, \quad \frac{256}{6} = 42.66
\]

We thus arrive at $A_b$ (51.2) whose octave (102.4) will fit into our scale, and $F_2$ (42.66), which is already represented by its octave (85.33).

The fifth overtone, $e^1$ (320), treated as the sixth, and its frequency accordingly divided by 6, produces the lower octave of the $A$ which we already have:

\[
\frac{320}{6} = 53.33
\]

The seventh overtone

The seventh overtone of $C$, $\text{eb}^1$ (448), cannot be used. If we attempted to apply the same procedures to it as to its predecessors, we should arrive at terrifying results. According to these procedures, we should have to consider it in succession a second, third, fourth, fifth, and sixth overtone. This would produce:

\[
\frac{448}{2} = 224, \quad \frac{448}{3} = 149.33
\]

$\text{eb}$ (112) which lies above the limits of our octave; $\text{eb}$ which is unusable for the same reason; $\text{Bb}$ (113.78) which we may say in advance that it suits our purposes less well than the $\text{Bb}$ (113.78) which we shall arrive at by other means. (The superiority of the latter will appear from the consideration of the distances between the tones, which we shall soon undertake.) We should also achieve a $\text{Gb}$ (89.6) that suffers from the same disadvantage as the $\text{Bb}$, and finally an $\text{Eb}$ (74.66) which would cloud the $\text{Eb}$ (76.8) already present in our scale.

In the distances between the tones, there must be some clear order. The smallest interval thus far is the minor second between $E$ and $F$, and it should not be hard to establish this as the smallest interval in our scale. But the new smallest interval $-\text{Eb}$ (74.66) to $\text{Eb}$ (76.8) would assert its claims. And since it would not do to provide only one or two tones of the scale with auxiliary tones which were simply slight flattenings of the original tones, every tone of the scale would have to be provided with a similar auxiliary.
And these auxiliaries would have to have other tones at a similar distance below them, and so on, until we should have a hundred or more separate tones to the octave. Such a structure would be impractical, and instrumental technique could not cope with it. To realize to the fullest extent how meaningless it must remain for practical music, one need only imagine a singer hopelessly struggling with such small intervals.

In the play of harmonic intervals—that is, in chord-progressions—every tone of the scale must be capable of being used not only as a root but also as any other factor of a chord. To this rule the tones derived from the seventh overtone could be no exception. And every one of them would support an overtone series of which the seventh overtone must be treated like the seventh of the original series. The result would be chaos.

Is it not remarkable that musical mankind, after thousands of years of musical practice, should not have arrived at mastery of the characteristics of the seventh overtone? Attempts to include it in our tonal system have not been lacking. And, like other "impure" tones, it can of course be introduced melodically, if it performs a clearly subordinate function in filling out the main spaces. But its introduction into harmonic practice would have the results described. The attempt to expand our system in this direction is just as futile as it would be to try to make fractions instead of whole numbers the basis of our reckoning. Numbers and number-relations meant more to antiquity than they do to us, for we have lost the sense of the mystery of number through our familiarity with price-lists, statistics, and balance sheets. The secret of the number 7 was well known; to conquer it was to become the master or the destroyer of the world. It is understandable that such a mystic and unfathomable number should have been looked upon as holy. And in the world of tone, too, we must acknowledge the holy circle to be inaccessible.

Derivation of the Remaining Tones

The overtones lying above the seventh cannot be used for the derivation of further scale-tones, any more than the seventh one itself. In the course of such use, each one would have to serve once as seventh overtone, and thus the tonal tangle produced the first time would be made infinitely worse. But our scale is not yet complete, even though we have examined the realm of the six overtones from all sides.

The generative power of the parent tone, C, is exhausted. The tones c, G, F, A, E, Eb, and Ab surround it like a proud group of sons. They will begin to lead lives of their own only when they leave their father's house. This process in the family of tones is called modulation. But they can establish their own households while they are still under the protection of their father, and can present their progenitor with a throng of grandchildren. What this means is that we must treat those overtones of the tones G to Ab which lie within the compass of the first six overtones of C (C-G'), in the same way as we treated the original overtones. As the method is now familiar, only brief explanations will be needed.

The third overtone of G, d' (288) (3 x 96) gives us, when its frequency is divided by 4, D (72):

\[ \frac{288}{4} = 72 \]

With this we may compare the D that is produced by dividing the ninth overtone of C, d', by 8:

\[ \frac{288}{8} = 36 \]

We may further, by dividing this same d' by 5, derive Bb, (57.6):

\[ \frac{288}{5} = 57.6 \]

[38]
The upper octave of this tone (the tone itself lies below the octave of our scale) is B♭ (115.2), which is not suited to our scale, for the distance between it and the adjacent A (106.66) would be disproportionately large. What was said above about Eb (74.66) thus applies to this B♭, in the opposite sense. The next overtone of the G produces only tones which we already have, for it is the same as the sixth overtone of C.

The third overtone of F corresponds to the fourth of C, and accordingly is of no further use to us. But the f¹ (341.33) on the other hand, the fourth overtone of F (4 x 85.33), gives us something we did not have before, B♭ (113.78), arrived at by dividing the f¹ (341.33) by 3:

\[ \frac{341.33}{3} = 113.78 \]

Dividing this same f¹ (341.33) by 5 we get D♭ (68.27):

\[ \frac{341.33}{5} = 68.27 \]

The overtones of A (a and e¹) do not produce anything new.

From the E, by dividing its third overtone b (240) by 2, we derive B (120):

\[ \frac{240}{2} = 120 \]

The late-born sons Eb and Ab provide us with the tones G♭ (92.16), c♭ (122.88) and F♭ (81.92). But we shall not accept these gifts. We shall find the G♭ elsewhere, in a better form, at the desired distance from its neighbors (that of the half-tone E-F);

\[ 40 \]

the c♭ (122.88) disturbs the earlier grandchild B (120), and the F♭ (81.92) does not agree with the E (80). In the course of chord-progressions, these tones may occur, either through modulation, in which the relation with the C series is suspended, or, while still related to the C, as mere neighbors of B♭ and Eb, or otherwise in a harmonically subordinate rôle, so that they have no independent existence.

And now the sons of C have done their duty, and still our scale is not complete. If we arrange the tones in upward succession from C to c, we encounter a gap between F and G. The distance between every other pair of adjacent tones is a half-tone. We can complete the family by including in it the great-grandchildren of C. The grandchild B♭ (113.78) produces a G♭ (91.02), through the division by 5 of its second overtone b♭ (227.56):

\[ \frac{227.56}{5} = 45.51 \]

We may obtain the same tone from the Db:

\[ \frac{341.33}{5} = 68.27 \]

The fourth overtone of this Db, d♭ (273.08), divided by 3, gives a G♭ (91.03), whose insignificant fraction, like that of the G♭ (91.02), we may disregard. But the two grandchildren D and B also have offspring. The fifth overtone of the D, which is the same as the third overtone of the B (namely f²), divided by 4, gives an F² (90), having one vibration less than its related G♭:

\[ 41 \]
We apparently have here, in the relation of \( F^\# \) to \( G_b \), what we sought to avoid in our consideration of the seventh overtone: an excessively small distance between two tones of the scale. But this is true only in this one instance, and the other tones of the scale are not affected. We can accommodate ourselves to this slight disturbing factor, whereas we should have had no defense against the \( Götterdämmerung \) of the tones which the fatal seventh overtone would have initiated. A comma of the size of one vibration per second is in this register (the great octave) not as disturbing as the difference between the natural and the Pythagorean thirds (80:81), but it is nevertheless large enough to be perceived by the ear. Yet it is the smallest possible difference, and it is in any case more acceptable than the one which would have arisen from the adoption of the \( G_b \) (92.16) derived from the \( E_b \).

The family has no further development. True, the \( D_b \) could still produce an \( F_b \) or a \( B_b \), but we have better forms of these tones (E and A) already present; they would destroy the purity of our scale, and besides, we have already rejected \( F_b \) in the course of our calculations. All the other great-grandchildren are already represented in our scale, and we need expect no further enrichment from the offspring of the great-grandchildren. Since the grandchildren already suffer from the disability of the comma, their descendants would veer off still further in the direction of the impure, and lose their harmonic connection with the original tone.

Moreover, our scale is complete: we need no further tones. If we arrange in ascending order from C to c all the tones we have derived, we shall find that the distances between the adjacent tones are not exactly the same throughout. They are in the proportions that occur in the third and fourth octaves of the overtone series: that is, 15:16, 16:17, 17:18, and 18:19. (For practical purposes the fractional parts of the vibration numbers may be disregarded.) All these intervals are heard as half-steps. The ear is not in danger either of mistaking the largest of these intervals (15:16) for a whole-step or of finding the smallest (18:19) too striking a departure from the normal half-step, such as would have resulted from the use of the abovementioned \( -B_b \) (112), \( +B_b \) (115.2), \( -G_b \) (89.6), \( +G_b \) (92.16) or \( -E_b \) (74.66). It follows from the inequality of the half-tones that the whole-tones too are of different dimensions; but they stay approximately within the limits set by 8:9 and 9:10.

Does not this inequality of interval-dimensions conflict with the requirement mentioned earlier of simple and clear relations, and of the maintenance of the half-step interval first produced—that between E and F? No, for in the first place the discrepancy is never so large as to result in loss of the relation to the model half-tone, and in the second place it is just the inequality in the distances between the tones that permits us to feel clearly the relations of the scale-tones to their progenitor. Thus in the scale derived from C the tone-succession c-d\( _b \)-e\( _b \) would consist of an interval of 16:17 followed by an interval of 8:9; while in the scale derived from D\( _b \) the same succession would consist of 15:16 followed by 8:9, since in that scale the tones c-d\( _b \)-e\( _b \) would occupy the positions that are held in the C scale by the tones b-c-d.

Guided by their subconscious feeling for the intervals, singers and players of string and wind instruments differentiate quite sharply between large and small whole-steps and half-steps. So long as they stay within the scale derived from a single fundamental generating tone (remember that the inclusion of the "children" and "grandchildren" does not imply any modulation), they produce the half-step and whole-step intervals according to our model series. When the generating tone changes, the tiny differences in the intervals change with it.

In equal temperament, there is no such adaptation to the fundamental tone, and thus to sensitive ears music performed on keyboard instruments lacks the fine lustre of the light that falls at ever-changing angles as it is cast by different generators. It does not have any of that fine inner agitation that arises from slight variations of pitch. That is why keyboard music may often grow somewhat tiresome if the player does not know how to make up for this natural shortcoming through such subtleties of performance as registration, dynamics, and touch.
The Comma

The last-cited example (c-db-eb = b-e-d) shows what happens to the comma in melodic and harmonic progressions. Players of keyboard instruments do not have to worry about it; it is divided up and so distributed on their instruments that the octave is pure and no other interval bears the entire burden of the comma. All other musicians—singers, and players of wind and string instruments—use untempered tuning. Guided by the ear, they dispose of the comma by always seeking to produce harmonic intervals in their simplest form. This means that they make all fourths and fifths pure, while the thirds and sixths vary slightly according to the melodic and harmonic functions of their constituent tones, and the remaining intervals are determined to suit the requirements of the invariable ones. The comma is thus relegated to intervals in which the ear will tolerate a certain impurity. This is not always accomplished without difficulty. It is often not possible, at the required speed of harmonic change, to produce the chords in their purest forms. In such instances, the harmonic intervals at the more important points are made pure, and the others brought as close to pure intonation as possible. If the harmonic and melodic progressions are such that the ear has difficulty in relating the fundamental tones to the scale-tones derived from them, while the chord structure consists only of simple triad formations, then this more or less even spreading out of the comma may be replaced by a more disjunct treatment: every chord appears in pure form, and the comma occurs, either in whole or in part, between it and its surroundings.

Singers and players achieve the solution of the comma problem for the most part without realizing it. Even in harmonic progressions which because of their complexity or quick succession can be comprehended only slowly, their ear leads them to relegate the comma to the least conspicuous place. When, however, the harmonic relations become too opaque, or when the roots of combinations follow one another in an order which is not unambiguous, the ear becomes uncertain. The singer or the player does not then know where to make the adjustment, and he sings or plays out of tune. That is why passages based upon extreme chromaticism or enharmonic change are difficult—and for choral singers often impossible—to produce in pure intonation, even after all the experience that singers have had in the course of music history.

From this fact it is clear that musical practice, composition, and theory can never disregard the conditions laid down by the facts of the existence of pure intervals and the desire of the ear to perceive them wherever possible in tonal combinations. This does not mean that we must return to a more primitive level of harmonic and melodic practice. The harmonic and melodic material is, thanks to the constantly changing significance the composer can give it, infinitely variable. But all tonal phenomena are based upon inescapable facts, as they have been since men first began to make music, and will always be as long as they continue to do so. And these facts cannot be overlooked if order and purpose are to reign in music. Though the ear and the mind are capable of immense development in their ability to accept sounds of varying complexity, yet this ability depends on underlying natural phenomena, even though the latter usually lie hidden. Is it not superficial to try to attack phenomena so deeply rooted in the life of the soul as are the unconscious desire for the adjustment of the comma discrepancy, and the feeling for tonal relations in general, from so crassly physical a standpoint? We do not experience the relationships of tonal groups to the progenitor tones as a mathematical balance of vibration-numbers and ratios. It is not the derivation of scale-tones from the overtone series that causes our pleasure in listening to good music. What goes on in the realm of our emotions and sensations cannot be physically measured; indeed our procedure does not do justice even to the mere physical activity of hearing. Granted that, compared with the subtle spiritual stirrings which are the subject and object of our music-making, the observation of the overtone series with its quantitative relations is a rough and boorish procedure. Science knows much more refined methods of analyzing sound and hearing. But the crude facts of acoustics have one advantage: they are easy to observe and closely related to the instrumental handicraft that is in daily use by the musician. For him that which strikes the listener as an inner experience is first of all
a matter of tuning the vocal chords, of lip-pressure, or of finger-placement. The most moving beauties of Mozart are for him in the first place notes on a page; the intervals, no matter what their effects on the soul, are tangible, measurable units; chords are light or heavy; tones have mass and density, just as solid objects do. He must, it is true, know more than anyone else about the beauty of his music, and must not be stupidly ignorant of what wise reflection upon its nature can reveal. But what good is the greatest wisdom to him if he does not know how to tune the vocal chords, to apply his lips, or to place his fingers in such a way as to produce the tonal structure that will move the listener?

For the composer, and consequently for everyone who concerns himself with the technique of composition, the same is true as for the good performer: he must achieve the deepest impression by employing the best possible devices. He will come by them much better through our materialistic approach than through many a learned discussion of the bases of musical procedure. Acoustic phenomena as a mirror of the life of the spirit have always represented the best point of departure for studies in the technique of composition, and we may assume that in the near future no better approach will be found, in spite of all the fruits of modern research. Perhaps some day a highly gifted thinker, equally accomplished in the fields of scholarly research and of music, will evolve new principles upon which to base a system of expounding the craft of musical composition—a system far clearer and more comprehensive than we can imagine. Until then it seems to me the more important to limit ourselves to the crude, easily understood basic facts, since in all branches of musical activity, nowadays, attention to simplicity of means and directness of effect is urgently needed.

12

Perspective

We have now listened carefully to the pure sound of the overtone series, we have examined the nature and tendency of the overtones, and we have thus found the simplest and most logical method of arranging the constituent parts of the overtone series (a vertically constructed series of which the parts are arranged one above another in proportional relations, forming unambiguous and immutable intervals) in a different series: the twelve-tone chromatic scale. This series, by means of tones ascending stepwise, reaches from a fundamental tone to the octave of that tone. The distances between the adjacent tones are all equal, except for tiny differences which do not affect our impression of equal distance, but rather permit us to infer the functions of each tone in relation to the fundamental tone of the series. The method we have used for determining the pitch of the tones of our scale is not replaceable by any of the methods commonly used for that purpose. The logarithmic method, or that which employs “cents”, or any other division of the smallest pitch intervals, has no value for us, since none of these reveals anything about the most important aspect of our scale: the relation of the individual tones of the scale to their progenitor.

But I hear the reader who has attentively followed me thus far impatiently exclaim: “But what’s the good of all this? The chromatic scale is nothing new. It would have been simpler to take it for granted as something generally known, and to have spared us all this reckoning, which is no pleasure for a musician!” To this I must reply that although the chromatic scale is known, it is so only as an enrichment or a variation of the seven-tone major and minor scales. All earlier theories of composition start from the seven-tone scale as the basis of musical creation, and in this they express a view generally held. My experience has taught me that to put forward any other opinion is to encounter unyielding opposition from both musicians and laymen. The situation today is like that which obtained at the time of the transition from the church modes to the major and minor scales, in the Middle Ages. Practice has gone forward to a point to which theory has not yet followed it. All composers nowadays make use of the extended harmonic and melodic relations that result from the use of the material of the chromatic scale, but for lack of an adequate theoretical foundation they still try to cram every manifestation within the narrow confines of diatonic interpretation.
Anyone who has once realized how many complicated and unclear
explanations can be avoided by the assumption of the chromatic
scale as the basic scale of musical theory, will feel like the man
who has never deigned to pay any attention to the fire-escape outside
his window until one day a fire breaks out, the stairs are in flames,
and the scorned fire-escape becomes his only way out. From now
on he will appreciate it. In music we have had a fire, too, and we
are thankful not to have overlooked the escape provided by the
chromatic scale.

The adoption of the chromatic scale as the basis of music does
not mean that harmony and melody must consist of an uninter-
rupted series of whining half-tone slides, or that according to some
arbitrarily conceived plan the tones of this scale must be scattered
broadcast through our music, reappearing aimlessly in a thousand
different forms. Everything that can be expressed in the diatonic
system can be equally well expressed with this chromatic material,
since the diatonic scales are contained in the chromatic. The ad-
vantages of tonal connection and of chordal and melodic inter-
relation are as much ours as they ever were. But we have thrown
off chains that hampered our movement; we have discarded the
tinted lenses that transformed the many-colored world around us
into a dull and monotonous image.

In opposition to this view, the natural simplicity of the diatonic
scales may be adduced. But the calculations which we have made
demonstrate that the chromatic scale can be derived just as simply
from the overtone series; that, since it makes exhaustive use of the
clearest overtone relations, it has an even more natural basis; and
that it is thus the most natural of all scales, and the best adapted
to melodic as well as to harmonic use.

True, the pentatonic scale is a natural one. It is confined to the
natural intervals of the octave, the fifth, and the fourth, and does
not even make use of the major third to fill out its gaps. For us this
represents the absence of the most important element of harmonic
construction—the complete absence of the element of perspective.
Just as the pentatonic scale permits only a monotonous and in-
flexible harmony (which is not stylistically suited to it, by the
Derivation of 1
(Chroma scale)

The tones through which the scale-tones are derived are enclosed corresponding tones in equal temperament.

Tones from C

The series at the bottom gives the frequencies of the corresponding tones of the chromatic scale.
y), so the melodies that are based upon it are cool, undifferentiated, and remote. Thus even more for pentatonic than for other scales we need to have a knowledge of the people who created it and their environment. Pentatonic scales still play an important rôle in music, but in European music they have been little used, because of the small number of tones they offer within the octave. Only slight traces of Irish and Scotch folk-music, with isolated fragments from later sections, testify to their former existence in Europe.

The old Greek scales, which in slightly changed form represented modal material of mediaeval composition, certainly form noble bases for melodic construction. But they sprang so entirely from a lydian way of feeling, and were evolved so exclusively for melodic poses, that they are like tracks that guide musical thinking into infinite linear directions, although even the most strongly melodic forms of expression always make use of certain harmonic elements. Church modes really began to die from the moment that the monic sense first sought expression in the earliest polyphony. Every simultaneous combination of tones really contradicts the use of these scales, and can be explained in them only by patchwork additions to the modal system. The beginning of polyphony marks the beginning of the mastery of the diatonic major and minor scales. Yet for centuries men tried to explain the developing art of polyphonic writing in terms of scales not made for that purpose. But surely major and minor scales form a rich body of material? was it they that first made the great development of our music sible, especially on the harmonic side. True; but did they not favor the development of formulae and stereotyped turns of phrase which threatened to smother music? There have always been rebels against the tyranny of the major and minor—a few lians at the end of the Renaissance (such as Gesualdo, Prince of Venosa) and above all Mozart, who in a number of his works shook foundations of the major-minor régime.

The actual dethronement took place in the last century. In Wagner's Tristan the rule of major and minor was overthrown. Unquestionably, the diatonic scale was here replaced by the chromatic as basis for all lines and harmonic combinations. But the revolu-
tion came too soon. The decision and the consistency of this bold step were unique, and at first no one followed the new trail. For decades Tristan remained the only work based on chromaticism, and even its creator never again made so mighty a forward step into the new domain. Not until the turn of the century did the outlines of the new world discovered in Tristan begin to take shape. Music reacted to it as a human body to an injected serum, which it at first strives to exclude as a poison, and only afterwards learns to accept as necessary and even wholesome. What we have experienced, instead of a true understanding of the chromatic world of music, has been first the penetration of an ever minuter chromaticism into the linear and harmonic aspects of our music, then the disintegration of every element, a lapse into complete absence of plan and rule, and finally pure anarchy.

If today, from our point of vantage over the whole field, we definitely adopt the chromatic scale as the basic material for composition, we are only continuing what was begun eighty years ago.

13

A Forward Glance

Will the musician forever be satisfied with this tonal material? Will there not be within some reasonable time a further enlargement of it? To many, the introduction of the quarter-tone system is the answer to this question.

Scales may arise, as we have seen, in either of two ways: through the filling out of the octave with intervals measured by the proportions of the overtone series, and through the arithmetical division of the octave. This book recommends the first of these, and the only way in which this system of scale-construction could be expanded would be by the use of the seventh overtone, for there is no compelling reason why we should choose arbitrarily among the proportions offered us by the overtone series, or skip over one of the overtones and choose the next one as a basis for further reckoning. But I have shown that to reckon with overtones above the sixth leads to chaos. The system cannot be enlarged in this direction.

The twelve-tone chromatic scale is, as far as we can humanly tell, the most complete solution of the problem—at least for harmonic purposes.

The quarter-tone system proceeds from the second method of scale-construction. It takes the equally tempered twelve-tone system as its point of departure. That is a mistake. We have seen that equal temperament does not offer a single scale-interval in pure form. But what can be borne in a twelve-tone system becomes intolerable in a system in which there are twice as many tones that contradict nature. Anyone who has heard quarter-tone music frequently, especially on keyboard instruments, knows that this is true, if his sense of hearing is healthy, and he has not allowed it to be clouded by preconceived opinions. Stringed instruments can make this music barely tolerable, since even when working with these intervals they can so place the comma that the ear hears pure intervals instead of an uninterrupted series of mistuned ones. But this must contradict the intention of the quarter-tone composer, for the correction of one of his intervals by the size of a comma is, proportionately, a considerable "clouding" of the interval. The assertion often made in support of the quarter-tone system—that quarter-tones exist in the folk-music of many peoples—is not true. All singers with a natural feeling for music employ not only the octave but also the pure fifth and pure fourth (which do not exist in the quarter-tone system). These intervals are then divided up into smaller ones, according to taste and tradition. The results include third-tones, fifth-tones, sixth-tones and of course also quarter-tones. But nothing indicates that any one of these small divisions is particularly favored. And how would it be possible to ascertain whether it were or not, since the untrained folk-singer will hardly reproduce with accuracy the same minute divisions each time he sings his song? To establish anything of this sort, it would be necessary to compare very exact measurements based on numerous phonographic recordings of the same singer singing the same song repeatedly.

For that matter, our own melody employs and always has employed intervals even smaller than the quarter-tone. A semitone
for example, may, like any interval except the octave, fifth, and fourth, have infinitely varying dimensions, from the hardly perceptible departure from an original tone to the very close approximation of a whole-tone, depending on its melodic function. And of this great variety, based as it is on the highest sensitivity, the quarter-tone system would rob us for the sake of a decomposed harmony which, no matter how long we try to accustom ourselves to it, would no more satisfy our ears and spirit than concentrated food pills instead of a diet of naturally grown foods would satisfy the palate and the stomach.

Other expansions of the scale derived from the equally tempered system are, for the same reasons, necessarily sterile, whether based upon sixth-tones, eighth-tones, or any other divisions. So-called "pure intonation" instruments, in which a compromise is sought between the two types of scale-construction, are bound to have so many keys that they will always be too unwieldy to be of any use in musical practice.

Finally let us mention an aberration that has haunted and still haunts many inquirers: the micro-octave. It has been asserted that within the interval of a tone or a semitone very detailed divisions could be made, which would exhibit relationships like those of the octave, the fifth, the fourth, and so on. It is true that the ear can perceive such tiny tonal divisions, as is shown by melodic performance, which makes use of such minute variations as a means of expression. But the theory does not hold. The simplest way to disprove it is simply to listen to such subdivisions. This is no longer impractical, for they can be produced electrically, and it will at once be apparent that there is no trace of any such structure as we know between a tone and its octave. Where, indeed, should such a structure come from? The structure of the true octave is derived from the overtone series, from which nothing more complete than the comprehensive building material furnished by the chromatic twelve-tone scale can be developed.

CHAPTER III

The Nature of the Building Stones

1

Series 1

A single tone conceived as the root of a scale; the chromatically arranged twelve-tone series born of the tensions set up by the juxtaposition of vibrating units in the proportions of the simple numbers from 1 to 6;—does not all this seem like a distant echo of the musica mundana of the ancients, of those harmonies of the spheres that reigned above both earthly types of music, musica humana and the music "quae in quibusdam constituta est instrumentis"? Those harmonies so perfect that the inadequate sense organs of men could not perceive them, needing no realization in sound, since the ratios of numbers that underlie all movement and all sound are more to the reflecting spirit than the external part of music—sound—through which it becomes profaned and is brought within the sphere of man's perceptions? For us there is no longer, thanks to our understanding of their common physical basis, a fundamental difference between musica humana and musica instrumentalis, and even as concerns musica humana and musica mundana we may concentrate our attention today rather on those aspects which they have in common than on those in which they differ. We shall not do as the ancients did, and carry over earthly relations to happenings far out in space. Rather, we shall observe in the tiniest building unit of music the play of the same forces that rule the movements of the most distant nebulae. This world harmony, which in its reality is infinitely more stimulating and for
the musician more significant than the sounding hemispheres of
the ancients, exists not only for the seeking and calculating knower
of the stars; for the naive believer, too, it is a fact as real as it is
inconceivable. But just as today an astronomer cannot understand
his reckonings in light-years, or the equalization of time and space,
without knowing the workings of the electrons within the cosmos of
the atom, so to the believing musician the sense of his musical
material, the earthly image of the harmonious music of the universe,
can never be clear unless he continually returns to the deepest
kernel of the single tone, and seeks to understand its electronic
flux—the overtones in their proportional relations.

The nature of the atomic structure of music in the individual
unrelated tone is already familiar to us, and we have followed the
birth of the elements—the tones in the chromatic scale—from the
electron-like relations of the overtones. And now we learn the sig-
nificance of the tones. The order in which the tones of the scale
were produced by the progenitor tone is of the greatest importance,
in the view which this book represents. It is not only an indication
that the tones have a family relationship, expressed in their con­
nections to the principal tone; it is also an index to the ranking of
these connections.

To a given tone, the tone an octave higher stands in so close a
relationship that one can hardly maintain a distinction between
the two. The tone which is only a fifth higher than the given tone
is the next most closely related, and there follow in order the fourth,
the major sixth, the major third, and so on. As the distance from the given tone increases in this series, the relationship
diminishes, until, in the tones that stand at the interval of the aug­
mented fourth or diminished fifth, it can hardly be felt at all. This
value-order of the relationships is valid under all circumstances. In
every combination of tones, some tones must seem subordinate to
others. The stronger ones may subject extended series of chords
to their domination, or their rule may not last longer than a pulse­
beat, but the accompanying tones will always be related to them
according to the order laid down in our series. How benumbed our
natural sensibilities must be nowadays, when systems of writing are
put forward which are based on a complete lack of relationship
among the tones. The carpenter would not think of disregarding
the natural properties of his wood and putting it together any old
way, without regard to its grain. The justification of such attempts
to “expand” the musical language will be sought in vain in the
tonal material itself. The only excuse for them must be the complaisant ear, which, despite the delicacy of its construction, is robust
even to accept sounds put together without the guidance of taste or instinct, instead of rejecting such sounds with the same
unerring discrimination with which the senses of sight and touch
would reject a chair thus miserably pieced together. In the domain
of tonal relations no expansion or innovation is possible, no ques-
tions of style are applicable, and there can be no progress, any more
than there can be in the multiplication table or the simplest laws
of mechanics.

No other system gives us complete proof of the natural basis of
tonal relations. All theorists are agreed, it is true, that there are
various degrees of relationship, and the order of descending degrees
of relationship is the same in all theories. This is remarkable, for
in every other respect there is anything but unanimity among
musical theorists. It seems as if a true feeling for the relationships
had existed even without the only complete explanation of them,
here given for the first time. To be sure, theorists have always
sought to find those properties of the tonal material which might provide
the logical basis for this feeling, and it cannot be denied that at
least for the earliest relationships explanations have been found
that are just as logical as ours. If, for example, one follows the
overtone series up from any given fundamental, the closest relation­
ships will be found between tones 1 and 2, 2 and 3, and 3 and 4,
in the familiar order. But if one follows this series further, one will
find a series of relationships wholly at odds with the experience of
musical practice: tones related to the fundamental tone as 4:5
(major third), 5:6 (minor third), 6:7 (under-size third), 7:8
(over-size whole-tone), and 8:9 (large whole-tone) would be the
next most closely related tones after the fourth. To explain the tone that is really the next most closely related, the major sixth, it would be necessary to interrupt the process of following the overtone series directly upwards (since the major sixth lies between tones 3 and 5); and for the derivation of the remaining tones from a single overtone series, in anything like the order that corresponds to practical musical experience, no rule can be found. This derivation can only be arrived at arbitrarily, and thus would not furnish any theoretical justification for the experience of practice. The establishment of the major sixth as the interval 3:5 tells us the size of this interval, but not the degree of relationship of a tone which is a sixth above a fundamental tone.

We shall henceforth call the significant order in which the twelve tones of the chromatic scale made their appearance, in diminishing degree of relationship to the given tone, Series 1. The values of the relationships established in that series will be the basis for our understanding of the connection of tones and chords, the ordering of harmonic progressions, and accordingly the tonal progress of compositions. Just as in architecture the big supporting and connecting members—piers, columns, girders, and arches—determine the form and size of a building, as well as its interior division into rooms, corridors, and floors, irrespective of the material of which they are built—so tonal relations introduce order into the tonal mass. Rhythm determines only its temporal succession. In our analogy, rhythm would determine the dimensions of the parts of the building and their distance from one another. Of course one cannot separate one function from the other. The supporting and connecting function of the columns cannot be separated from their place in space, and tonal relations must have definite rhythmic dimensions for their effect. But separate forces are nevertheless at work, as we see in places where one is much stronger than the other: where rhythm retreats far into the background in favor of a broad harmonic flow; or, on the other hand, where rhythm is the predominant element, and harmony and melody are hardly more than the coloring of the beats. How the tonal relations operate, we shall learn in Chapter IV.

Combination Tones

Up to now we have treated the tones only as members of a family, grouped about a progenitor tone. But a single tone is not music; unrelated and motionless, it cannot be called anything more than an "acoustic phenomenon". Even tonal relations, which form the basic principle for the organization of tonal combinations, are not in themselves music. The individual tone is not music until it is directly connected with other tones, and tonal relations are not operative until tones and tonal combinations are in motion. The primary building material of music must therefore include a third element, in addition to the tone and the principle of tone-relations. Music arises from the combined effect of at least two tones. The motion from one tone to another, the bridging of a gap in space, produces melodic tension, while the simultaneous juxtaposition of two tones produces harmony. Thus the Interval, formed by the connection of two tones, is the basic unit of musical construction. If we think of the series of tones grouped around the parent tone C (as in Series 1) as a planetary system, then C is the sun, surrounded by its descendant tones as the sun is surrounded by its planets. Series 1 shows us the distance of the planets from the central star. As the distance increases, the warmth, light, and power of the sun diminish, and the tones lose their closeness of relationship. The intervals correspond to the distances of the various planets from each other. In their melodic function, the two successive tones of an interval are like two planets at different points in their orbits, while the formation of a chord is like a geometric figure formed by connecting various planets at a given instant.

Just as the tone-relations are arranged in descending order of value, so the intervals have a natural order, which we shall call Series 2. Since we possess no material other than the twelve tones of the chromatic scale, they must also present the tonal material for Series 2. But here their significance is entirely different from what it was in Series 1, since we shall use Series 2 to evaluate the distances
between the various tones, and not the relationship of each tone to the progenitor. The basic difference between the two series will be clear to us if we again think of the architectural function of their components in musical construction. Series 1 provided us with the principal members of the structure; Series 2 will furnish the smaller materials: bricks and mortar, rafters, floor-boards, lath and plaster. The stone that can only be made into a wall with thousands of other stones; the shingle that needs hundreds of other shingles and cross-pieces before the roof is complete—these things are not governed by the same rules as piers and girders. Even if the larger members are made out of the smaller ones, the properties of each of the latter are of importance only until the next similar unit is reached; the characteristics of these small building materials have little effect on the larger lines of the design. But it is only the knowledge of the properties of the smaller units that enables the builder to make walls, floors, and roofs out of them. We derived Series 1 from the overtone series. For Series 2 we must proceed to the examination of another natural phenomenon: combination tones.

When a stringed instrument plays a double stop, or two bassoons play together, or simultaneous groups of tones are produced in any other way, additional tones are involuntarily produced which bear the name of combination tones. They are usually so weak that the superficial ear does not perceive them, but this makes them all the more important for the subconscious ear. They are the third point of a triangle whose other two points are in the sounding interval, making possible for the ear a sort of trigonometry by which it is enabled to form a judgement of the purity of an interval. The musician who is not familiar with these phenomena had better impress clearly upon his mind the difference between overtones and combination tones. Overtones are produced in varying number by a single sounding tone: combination tones arise only when two or more tones sound simultaneously. How little the two phenomena have in common is shown by the simultaneous sounding of pure tones, having no overtones, previously mentioned as produced by special electrical means, or by tones poor in overtones, such as those produced by tuning forks. Such tones, poor or lacking in overtones, nevertheless produce combination tones; as a matter of fact, they produce them particularly easily.

Although the nature of combination tones has been known for a long time, they have never been applied in musical theory, in a degree appropriate to their significance, to the explanation of the properties of musical materials and the rules for musical writing. This is owing to the great pains formerly necessary to observe them and the meagre results obtained. Tuning forks and resonators, the classic tools for the investigation of combination tones, are inaccurate and clumsy weapons, to which they offer stubborn resistance. Today we have better tools, and while the appropriate experiments are not easily available to every musician, description of my own observations will enable him to follow my reasoning.

Many tone-colors are particularly favorable to the production of prominent combination tones. The latter can be clearly heard when two large tuning forks sound simultaneously, and the violinist hears them as soft bass tones when he plays double stops in pure intonation. Once the ear has become aware of them, it hears them easily, and in certain cases it hears the combination tones as strongly or even more strongly than the directly produced tones. This fact is of importance in instrument construction, as we see from a well known device among organ builders: in order to save the great expense and large amount of space required for the deepest labial pipes, builders of small organs who wish to provide for these very low tones take two smaller (higher) pipes which, when sounded together, will produce a combination tone of the desired pitch. From this fact we draw the important conclusion that an interval and its combination tone bear a certain immutable relation to each other, a conclusion confirmed by the following experiment.

Electric instruments for the production of tones permit us to let a given tone (say, c') sound uninterruptedly, with constant volume and timbre. In the following drawing, this sound is represented by the horizontal line starting at the point c'.
The equivalent in musical notation

We then take another tone and move it in a steady upward glide, starting at the unison, c', and rising to c" (the oblique line c'-c")

We can then hear, aided by sufficient amplification, a series of combination tones, also rising, which starts from zero (when the two tones are in unison), comes into being at a pitch so low as to be barely perceptible the moment we diverge ever so slightly from the unison, and forms, against the gradual ascent of the upper voice, a steeply rising curve. Towards the end of this curve the angle of the ascent decreases, and when the two main voices are at the interval of the octave the curve arrives at the pitch of the lower tone of that octave. The graphic representation of this procedure shows that beneath the played fifth we hear the octave below its lower tone, and beneath the fourth the double octave below its upper tone. That is, the simultaneous sounding of the tones c' (256 vibrations per second) and g' (384) produces the combination tone c (128), while the simultaneous sounding of c' (256) and f' (341.33) produces F (85.33). In other words, the fifth, corresponding to the overtones 4 and 6, carries with it a combination tone equal to overtone 2. Or, in ratios: the fifth 2:3 produces the combination tone 1; the fourth 3:4 (for the sake of comparison, we transpose the fourth c' to g-c', the fourth in our original overtone series) likewise tone 1. From these facts we may deduce the principle governing the relation of the combination tone to the directly produced interval:

The frequency of the combination tone is always equal to the difference between the frequencies of the directly produced tones of the interval.

This principle also takes care of the ratios.

Combination tones, being real sounds, obey the same laws as other tones. As component parts of sounding intervals, they produce further combination tones, which are, of course, less intense than the first ones. If a combination tone consists of the difference between the proportion numbers (or frequency numbers) of two tones, then by the same process we have already used we can
easily find the combination tones of the second order. Let us take for example the minor third e'-g' (320-384), which has the ratio 5:6. The first combination tone is the note 1, C, with 64 vibrations. This tone, in connection with one of the directly produced tones, results in a combination tone of the second order. The g' cannot be the tone that produces this second combination tone (in connection with the first), because it would produce nothing more than a change in intensity in the original interval: interval C-g' (1:6), combination tone e' (5). So it must be the interval C-e' (1:5) that produces the new combination tone—e' (4). If we find in this way the differences between the combination tones of the first order and the lower tones of the directly produced intervals, we shall arrive at the curve of combination tones of the second order.

This curve goes in the opposite direction to the first: it begins at the unison with the directly produced tone, and sinks slowly, arriving beneath the played interval e'-e' at g, beneath c'-f' at f. Beneath the played fifth it intersects the first curve, and then sinks more quickly to zero, whence its opposite arose.

The series of combination tones of the second order combines with the intervals already present, consisting both of directly produced and of combination tones, to create new orders of combination tones. Theoretically, the system may be extended to infinity.
But we remember that the overtone series, too, is theoretically infinite. In practice it is hardly possible to produce audible combination tones of orders higher than the sixth. For the ear's sense of intervals the later orders of combination tones are without significance, since they are hardly perceptible even to the fine discriminations of the inner ear (of which we are not conscious), and since furthermore so long as the directly produced intervals are kept close to the simpler ratios of the overtone series, nothing is produced but octave doublings of earlier orders of combination tones. For the purposes of our discussion we shall therefore content ourselves with considering the combination tones of the first and second orders.

3

Inversions

We cannot hear combination tones produced by either the unison or the octave. For the unison, the first order of combination tones is at the zero point, and the second order coincides with the unison of the directly produced tones. For the octave, the second order is at the zero point, and the first coincides with the lower of the original tones. Combination tones represent a clouding or a burdening of the interval. The octave and the unison, as the most perfect intervals, are not subject to any such impurity; the fifth has only one combination tone, since those of the first and second order coincide; all other intervals carry a double burden of varying weight. The clouding of the intervals is not so strong that any effort need be made to suppress the combination tones. Yet of course they must not be so strong as to overshadow the directly produced interval. Provided they remain below the level at which they would become actually disturbing, they give the interval its characteristic stamp. An interval without combination tones would be an abstract concept, as bodiless as the ratio with which we express it numerically. Now, for the musician who, despite the intangibility of his building materials, is a healthy realist in his craft, numbers and intervals are of value only as sounding entities. He will accept calculations employing proportions and curves only if they seem to offer practical advantages in the solution of musical problems. Thus the clouding of the intervals through the combination tones is not something that spoils his enjoyment of the abstract interval proportions; on the contrary, he uses it as a means of more precise perception of the intervals. The differences in the weight of the combination-tone burdens carried by the various intervals enables him to arrange the latter in order, so that starting with the octave, as the clearest, unclouded interval, and passing through the fifth (slightly clouded), each interval in succession carries a greater burden than its predecessors; that is to say, the purity and harmonic clarity of the intervals diminish step by step. In this series—Series 2—we are accordingly setting up a list of the individual building stones according to strength, hardness, and density.

The fifth bears, as we have seen, but a slight burden:

Its two combination tones coincide at a point which doubles one of its tones at the lower octave. The fourth, too, shows a doubling of one of its factors:

But since these combination tones do not coincide, but are an octave apart, the fourth seems somewhat more heavily laden than the fifth.

The major third and the minor sixth, too, show doublings of one of their constituent tones in their combination tones. In the major
third the lower tone is doubled: in the minor sixth, the upper. Both have a new tone, in addition, not contained in the interval directly produced. The minor third and the major sixth, on the other hand, carry two such new tones. Thus we see that the intervals seem to pair off according to the arrangement of their combination tones. The two members of each pair have the same combination tones. The only difference is that the second interval of each pair seems to reverse the relations of the combination tones (in this connection we disregard octave transpositions). If in the first interval the combination tone of the first order forms the fundamental of the whole tonal composite, then in the second interval of the same pair this tone takes the place which the second-order tone had in the first interval: in this second interval, the second-order tone becomes the bass. The major third \(c^\prime-e^\prime\) has combination tones in the positions C (first order) and \(g\) (second order); and the minor sixth \(e^\prime-c^\prime\) has \(c\) (second order) and \(g\) (first order), as may be easily seen by transposing upward the minor sixth \(c^\prime-ab^\prime\) in Fig. 37. The intervals thus pair off as follows: fifth and fourth, major third and minor sixth, minor third and major sixth, major second and minor seventh, minor second and major seventh.

Here we have a purely acoustical proof of the invertibility of intervals. That intervals are invertible, and that an interval adds up with its inversion to an octave, could hitherto be proved only from the ratios of the overtone series: the inversion of the major third 4:5 is the minor sixth 5:8 \((5:2 \times 4)\); the inversion of the minor third 5:6 is the major sixth 6:10 (or, in reduced terms, 3:5). Considering the above-mentioned dislike of most musicians for figures and other abstractions, proof offered by the combination tones ought to appeal to them more than that from the mere ratios, the more so as it provides us at the same time with another important item of knowledge: the two intervals that make up each pair are of unequal value. In order to understand that statement, let us keep two facts clearly in mind:

1. In groups of tones of different pitch sounding simultaneously, the deeper tones, with the slower vibration rates, have greater weight than the higher ones (a fact based on the weight of the vibrating material—the air masses).

2. Combination tones of the first order are significantly louder than those of the second order.

In the combination tones that arise from a major third, the lower, because of its low pitch, has the greater weight:

And it also (as a combination tone of the first order) surpasses its companion in intensity. The combination tones that belong to the inversion of the major third (minor sixth), on the other hand, present a less clear picture. Here too, of course, the lower tone (the doubling of the upper of the two directly produced tones) is the heavier; but it lacks the confirmation of this advantage which its prototype in the major third had. This tone is only the weaker combination tone of the second order, and is surpassed in intensity by the combination tone of the first order, which lies above it. It does not achieve the effect that is really due it, as the doubling of one of the original tones of the interval, because of the competition of its more intense but less significant companion (less significant in its relation to the tonal composite formed by the original interval and its combination tones). The aural impression created by the major third is thus distinctly clearer and more definite than that of the minor sixth. In the interval-pairs, both thirds and seconds show this more favorable disposition of their combination tones as compared with their inversions (sixths and sevenths). Between the fifth and the fourth the difference is not so marked, since the first-order combination tone lies below the second in both, whereas all other inversions exhibit the opposite disposition. But despite this favorable arrangement of the combination tones, the fourth is inferior to the fifth. The coincidence of the two combination tones
of the fifth gives it a purity which makes it superior to all other intervals except the octave.

4

Interval Roots

We have learned two lessons from our consideration of the combination tones—the proof of the invertibility of intervals, and the determination of the relative value of the intervals. A third awaits us.

If one of the tones of the directly produced interval is doubled, either in the unison or in a lower octave, by a combination tone, this accretion of strength gives it the upper hand over its partner. In intervals in which such doublings occur, the constituent tones are thus not of equal value. Rather, the tone strengthened by such doublings is to be regarded as the root of the interval, and the other as its subordinate companion. Numerous experiments have convinced me that the feeling that one tone of an interval has more importance than the other is just as innate as the ability to judge intervals exactly—everyone hears the lower tone of a fifth as the principal tone; the ear cannot be persuaded to attribute primary importance to the upper tone. Yet I have never found in any treatise the statement that intervals have roots—a curious circumstance, since this fact is of primary significance for the hearing and evaluation of harmonic intervals, and since its acoustical basis is so easily established:

The lower tone of the fifth is the root. The fact that both combination tones coincide at the lower octave of this tone makes it doubly strong; that is why the impression of the lower tone as root is so unmistakable, and the fifth is so very stable. In the fourth, the upper tone is doubled by the combination tones, and thus it is not the heavier lower tone that has the effect of a root. The interval is thus less steady than the fifth.

In the next pair of intervals, too, the root of the more stable major third is at the bottom, and of the minor sixth at the top.

The new tone introduced by the combination tones converts this interval into a triad, of which the root is doubled. The triad is not present in full strength, to be sure; yet it is so clearly represented that the rules of harmony permit the use of the “triad without its fifth”—a contradiction of the definition of a triad as consisting of three tones, while this interval contains only two. This pair of intervals offers a particularly clear example of the inferiority of the second interval, the minor sixth, in harmonic value. The major third contains in the pleasantest disposition the doubling of its lower tone by the first-order combination tone, while the new tone, which completes the triad, lying a fourth below the lower tone of the original interval, is appropriately weaker, being a combination tone of the second order. In the minor sixth, on the other hand, the root, which, because in the directly produced interval it is higher than its companion tone, is to that extent already weaker, is doubled only by a combination tone of the second order. The latter does, to be sure, lie in the bass, but because of its weaker intensity it is less prominent than the less important first-order tone which completes the triad. Obviously so ambiguous a tonal structure must produce a less satisfying effect than that of the major third.

The next pair of intervals consists of the minor third and its inversion, the major sixth.
Neither of the original tones is represented among the combination tones; instead, a new tone occurs, doubled in the octave, which again converts the interval into a major triad, but this time a major triad of which the root is not one of the original tones. That is, beneath the minor third lies the lower fifth of its upper tone, and beneath the major sixth the lower fifth of its corresponding lower tone. The minor third has the better disposition of the combination tones, since its first-order tone lies in the bass, whereas the lowest tone of the composite formed by the major sixth and its combination tones is the less intense combination tone of the second order. Since the new tone, not represented in the original interval, occurs in two different octaves among the combination tones, and since, lying below the original tones, it possesses greater weight than they, it fulfills all the requirements of a root. This confronts us with the somewhat surprising necessity of placing under every minor third and major sixth a tone which is not represented either in the directly produced interval or, of course, in its notation. Here theory comes into conflict with the practice of composition, which likes to deal with things that are clearly to be heard and seen, and would therefore like to take one of the two tones of the directly produced interval as its root. Practice could perfectly well yield to the theoretical requirement without the slightest hindrance, as long as the minor third and the major sixth appeared alone—that is, in two-part writing only. But as soon as these intervals appear in combination with others, which is by far the most usual practice in our music, the observance of this theoretical requirement would make our analysis far too difficult and too different from our habitual point of view, so that it seems more advantageous to treat both intervals according to the pattern which we have derived from their predecessors in the series. This would make the lower tone of the minor third, and the upper tone of the major sixth, the root.

Another consideration, besides ease in treatment and analogy with the root-determination of the other intervals, speaks for this procedure. This is the fact that whenever minor thirds and major sixths appear as parts of richer tonal combinations, they are almost always subordinate to stronger and more important intervals, so that it is unnecessary to set up a separate rule to cover the few instances in which these intervals are of governing importance, merely to satisfy theoretical requirements. We do not deny the existence of the real roots of these intervals, or their significance, nor does the system here set up as a natural and logical basis for musical composition suffer any lacuna on this account. We are simply making use of a convenient labor-saving device to render these intervals easier to handle. Whoever rejects this aid, even though such aids have always been adopted in practice, and prefers to make his study of musical writing more complicated in order to stick absolutely close to theory, may take the real root established by the combination tones as the root of every minor third and major sixth he uses.

Our decision makes it possible for us to use both intervals without hesitation. But if, although we need seek no farther, we insist on looking for an acoustical justification for the step we have taken, we may examine a little more closely the thirds that exist in the lower part of the overtone series. (The bias thus arrived at, however, will not change anything connected with the combination-tone structure of the minor third and the major sixth as explained above, and will not furnish a complete proof.) Within the first 11 overtones alone there are five different sizes of thirds:

the major 4:5, the minor 5:6, the under-sized 6:7, the over-sized 7:9, and the one which is between major and minor, 9:11. To these we may add the Pythagorean third, which we can easily calculate (see page 30), and which is between 4:5 and 7:9 in size. The ear
not only hears all these as thirds; it permits itself to be hoodwinked still further by this beautiful but characterless interval. If we play on the violin or other appropriate instrument a third that is as small as it can be without being a second, and if we then slide the upper tone up to the upper boundary of the third, just below the point where it would become a fourth, we cannot say just where the change from a minor third to a major third takes place.

In the middle space between the outside boundaries there is a field that can belong to either third, and is assigned by the ear to the major or the minor according to the harmonic or melodic context. With an interval that is so indefinite we can well afford to allow ourselves the liberty proposed.

Those intervals whose tones are separated by such great distances that they seem to be octave transpositions of fifths, fourths, etc., present much less happy dispositions of the combination tones than their prototypes, and accordingly justify the usual view, confirmed by a long history in musical practice, which assigns to them lower harmonic values, diminishing as the distance between their constituent tones increases. Even the octave, which stands above and beyond all calculation of interval values, loses so much of its value when it appears in the form 1:4 that, as its combination-tone structure shows, it is hardly equal to the fifth in clarity. In the form 1:8 the harmonic support of the interval by its combination tones is still less strong, and in the form 1:16 the composite becomes completely dissonant. Although all these forms are exceptional, adapted only to particularly characteristic and striking effects, and consequently seldom concern us as building material for the craft of composition based on a normal harmonic foundation, they are not useless. True, they seldom occur except as parts of chords containing one, two, or even more additional constituents, which take away the empty effect of the extended two-tone interval. But one might assume from the disposition of the combination tones of these intervals that when they did occur unmixed their effect would be much worse than it actually is. The fact that it is not is owing to the overtone series of the lower constituent tone of the interval, which is not disturbed by the comparatively strong combination tones that lie between the two tones of the interval, and which instead takes over their functions and fills in, sparsely but adequately, the large tonal expanse. When the tones of the interval are normally close together, the narrowness of the space and the force of the combination tones prevent any effect of the overtone series on the harmonic content of the interval.

The fifth in the position 1:3 still presents an excellent tonal picture; even 1:6 is good; not until 1:12 does it begin to lose value, although the freely unfolding overtone series of the lower tone of the fifth prevents it from becoming altogether worthless. The fourth is strikingly less fortunate—3:8 is still good, though a bit unstable; but 3:16 has no harmonic value (and who would think of introducing the fourth 3:16 into an otherwise smooth two-voiced texture?). That is owing not only to the combination tones, but also to the strong overtone series of the lower tone, in which the upper does not occur. The intervals after the fifth and the fourth lose their harmonic value in such octave transpositions even faster, and the inverted intervals (sixths) are, as one might expect, even worse off than the thirds.
The question then arises how these widely spread intervals are to be treated, for although in simple writing they never appear, and in the more complicated forms they occur only seldom, still we must know how to use them and what rank to ascribe to them. For this purpose one might determine separately the root of each of them, by experiment and by analogy, and then one would simply have to learn these roots by heart, in order to have them readily at hand when they were needed. But there is no point in going to all this trouble for a few exceptional cases. It is more practical here, too, to take a short cut, and to handle the spread intervals exactly like their close prototypes. This is quite sufficient for the practical purposes of composition.

5

The Minor Triad

In connection with the above description of the nature of the third we must mention a chord that has always given theorists endless trouble—the minor triad. To understand and explain the major triad is a task made easy for us by Nature, who places it in our hands as a handsome gift. But she gives us no hint about the minor triad. It does not occur in the overtone series, at least not in three successive tones. In the upper reaches of the series, minor triads can be constructed by skipping some tones (10:12:15); but this seems too far-fetched an explanation of a chord that appears almost as valuable as the easily explainable major triad.

We have seen that the value of a harmonic interval is determined by the grouping of its combination tones. The euphony of the major triad must accordingly be based not only on its favored position in the overtone series, but also on the disposition of its combination tones. In the major triad $c'-e'-g'$

the major third $c'-e'$ produces the combination tone $C$ (first order) and $g$ (second order); the minor third $e'-g'$ produces $C$ and $c'$; and the fifth $c'-g'$ only $c$. The directly produced triad is strengthened in the most complete way by the combination tones. How unfavorable, in comparison, is the picture presented by the minor triad. In the triad $c'-e^b'-g^b$

the minor third $c'-e^b'$ produces the combination tones $A_b$ and $a_b$; the major third $e^b'-g'$ produces $E_b$ and $b_b$; and the fifth $c'-g'$ produces $c$, as in the major triad. All that the combination tones tell us about the minor triad is that it is of less harmonic value than the major.

Almost all explanations of the minor triad have proceeded from the assumption that it is based on the converse of the natural principle of tonal construction. According to them the minor triad is a mirror image of the major. Within the boundaries of the fifth, the thirds are said to be so arranged that the order “major third, minor third” of the major triad is reversed in the minor. That is not hard to see, but it does not prove anything. In working with an element tied to the principle of gravity as closely as tone is, one cannot simply turn things upside down for the sake of a pretty idea. Every tonal composite is constructed from the bottom up; that is determined by the nature of the tonal world. Tones obey the laws exemplified in the overtone series just as the stones piled one upon another to make a building obey the laws of statics that apply in nature.

The cleverest of all the explanations based on the thirds contained within the fifth in the two triads is the one that says that the origin of the minor triad is in man’s desire to transfer to the world of tone the symmetry of his body. Since the major triad, on account of the inequality of its thirds, is an asymmetric structure, its opposite must be erected to restore the balance. This would be
convincing if other instances of such efforts to erect symmetrical counterparts were to be found in music. In the domain of visual forms, symmetry is one of the most important principles of design; tonal and temporal phenomena, on the other hand, seem to avoid it. Except in a few of the simplest basic rhythmic and formal elements (measure-rhythm and the simplest song-forms), it is hardly to be found in the field of aural forms. It is true that every more or less extended musical form consists of parts which offset each other to maintain the tonal balance of the whole. They are usually of unequal weight, since the juxtaposition of equal weights (a truly symmetrical arrangement) does not satisfy the listener. Hence the rule that when a section is repeated, or when a later section corresponds to an earlier one, changes of a formal nature—i.e., abbreviations or expansions—must be made. The extremely few examples of strictly symmetrical structure in musical works of recognized worth (except where other features eclipse the formal design) are the exceptions that prove the rule. Against the theory of symmetrical construction is also the fact that while it is true that we have a minor triad that is the opposite of the major, we do not have any opposite of the complete major tonality, which may be represented by its major triads on the fourth, fifth, and first degrees, in the shape of a really independent minor tonality. In harmonic progressions we make no distinction between the major and minor modes. Only the triad on the first degree tells us which mode is meant; all the other triads exist in both modes with major and minor thirds. A major dominant is the rule in minor, and the minor subdominant is fully at home in major, as are the Neapolitan and other alterations. Indeed, one form of the minor scale, the upward melodic, is the same as the major with the single exception of the minor third, and the fact that the other forms differ more importantly is due to a desire to reconcile the sixth degree with its close relative, the third: it is felt to be undesirable that an augmented fourth should exist between these two degrees. Thus there is no sign of symmetry between the major and minor modes.

A more daring explanation is the one that assumes a different effect of the overtones in the major and minor triads. The three overtones 4:5:6 that make up the major triad (c1-e1-g1 in the series based on C) have a common fundamental, of which the first tone of the triad forms the octave, while the second and third tones form the third and fifth.

The minor triad is said to exhibit the opposite relations. When it is in the corresponding close position, its three tones are said to have in the g1 a common overtone, which bears the relation of fifth, third, and octave, to the root, third, and fifth of the triad respectively. It is not clear why in one case a lower tone (fundamental or combination tone) and in the other a higher tone (overtone) should be added. The basic error of this explanation is, however, that it reckons with actual tonal relations which are no sooner cited in the case of one triad than they are disregarded in the case of the other. If the overtones of the minor triad are significant, then so are those of the major triad. But then we should have between the two g1, which occur as the overtones of the c1 and the g1, a g2, as the fifth overtone of the e1:

And here the whole house of cards collapses, for the minor triad should rank higher in the scheme of tonal values than the major, since its overtones are better arranged.

The most far-fetched and at the same time the most interesting explanation of the minor triad is the one based on the undertone series. The latter is the exact inversion of the overtone series:
It seems to me repugnant to good sense to assume a force capable of producing such an inversion. This force would do away with the gravitation that is expressed in the overtone series—and there is no evidence of the operation of such a force. In electro-acoustics there is a familiar phenomenon that it would be easy to mistake for an undertone series. Electric tone-producers can be made to sound, in connection with a given tone, combination tones having a wavelength twice, three times, four times and so on (and accordingly having a frequency one-half, one-third, one-fourth and so on) that of the given tone. This remarkable phenomenon, caused by the intersection points of the electric waves (and consequently of the air-vibrations), can never have for music the same significance as the overtone series. It occurs only under certain conditions, which were not possible before the days of electric tone-production, and which can never be produced by vibrating strings, pipes, or membranes. This “undertone series” has no influence on the color of the tone, and lacks the other natural advantages of the overtone series which arise without any artificial help and are available anywhere and anytime. Thus we have here no proof of any inversion of the overtone series occurring freely in nature. This phenomenon, which actually exists for the ear, does offer, like the purely theoretical undertone series, a tempting picture of the minor triad outlined by its first six tones. And yet even with special apparatus or with the help of the Dualistic theory we learn nothing about the minor triad except that it is the opposite of the major. For that we do not need the undertone series; the simple principle of interval inversion suffices.

What, then, is the minor triad, in reality? I hold, following a theory which again is not entirely new, that it is a clouding of the major triad. Since one cannot even say definitely where the minor third leaves off and the major third begins, I do not believe in any polarity of the two chords. They are the high and low, the strong and weak, the light and dark, the bright and dull forms of the same sound. It is true that the overtone series contains both forms of the third (4:5 and 5:6) in pure form, but that does not alter the fact that the boundary between them is vague. Pure thirds furnish us with pure forms of both major and minor triads. But the ear allows within the triads, too, a certain latitude to the thirds, so that on one and the same root a number of major triads and a number of minor triads can be erected, no two alike in the exact size of their thirds. Triads in which the third lies in the indeterminate middle ground can, like the third itself, be interpreted as major or minor, according to the context. But why the almost negligible distance between the major and minor thirds should have such extraordinary psychological significance remains a mystery.

It seems as if this middle ground between the thirds were a dead point in the scale, to which another similar but less significant dead point corresponds—the middle ground between the two species of sixths. Up to this point the harmonic force of the tonic has been working up from the bottom; here begins the dominance of the fourth and fifth, which extends from the boundary between the thirds to that between the sixths. Thus the minor triad would be associated with rest, and would derive from this fact its heavy, dull character. The major triad, of which the third lies in another field of force, would then receive from the active, life-giving sources other than the tonic its impulse, light, and energy.

Seconds and Sevenths; The Tritone

For the practical application of the next two pairs of intervals—major second and minor seventh, minor second and major seventh—it makes no difference which of the tones we take as the root. The combination tones do not point to definite conclusions. Seconds and sevenths are subject to greater variation than any other intervals; in both melody and harmony they occur in the greatest variety of sizes. A glance at our table of combination tones shows us that even
slight changes in the sizes of intervals have important consequences for the disposition of the combination tones.

If we transpose all the seconds that occur in the overtone series between tones 7 and 11 so that they have a common lower tone, then the undersized major second c'\textsuperscript{-}d\textsuperscript{1} (10:11)

has the combination tones A\textsubscript{b} and +b\textsubscript{b};

the major second (minor whole-tone) c\textsuperscript{-}d\textsuperscript{1} (9:10)

has the combination tones B\textsubscript{b} and b\textsubscript{b}

the major second (major whole-tone) c\textsuperscript{-}d\textsuperscript{1} (8:9)

has the combination tones C\textsubscript{1} and -b\textsubscript{b}

the oversized major second c\textsuperscript{1}\textsuperscript{-}d\textsuperscript{1} (7:8)

has the combination tones D\textsubscript{1} and a.

The situation is reversed, of course, for the minor seventh.

The minor second and major seventh exhibit still more complex dispositions of their combination tones. If we do not wish to make our work impossibly complicated, we must renounce hair-splitting distinctions between the various sizes of seconds and sevenths. We shall assume for each interval a normal size representing the average of the possibilities. The choice of a root is made more difficult by the wide choice of combination tones. It would be very tempting to take the lower tone of the second c'\textsuperscript{-}d\textsuperscript{1} as the root, because of the combination tone C\textsubscript{1} produced by the major whole-tone. Practical considerations, however, lead me to choose the upper tone as the root. Our familiarity with the dominant seventh chord leads us to hear the lower tone of the seventh belonging to this composite as the root, even when it appears alone:

At least this choice seems more natural than the opposite one. As the inversion always has the root in the opposite position, the upper tone becomes the root of the major second. We treat the pair consisting of the minor second and major seventh in exactly the same way: the root of the second is at the top, and of the seventh at the bottom. The objections of the doubter who made himself heard earlier, when we chose the roots of the minor third and major sixth, will no doubt be more vehement this time. In self-defense I can again cite the practice of composers. And to dissipate all doubts I suggest that the attempt be made once to find the true acoustic roots of all the seconds and sevenths one works with, among the many possibilities. Anyone who once carries out this very laborious procedure will soon find justification for avoiding undue complication of his work. For he would have to spend ten times as much time and trouble on determining the exact size of the intervals as on writing them.

To complete Series 2 we still need one interval: the tritone. This is the name given since time immemorial to the augmented fourth, reflecting its construction of three superposed whole-tones. The term does not really fit the enharmonically equivalent diminished fifth. But because of our constant use of chromatic and enharmonic formations, we differentiate between the two intervals nowadays only on paper, so that I do not hesitate to group both intervals under the name tritone. The tritone does not make a pair with any other interval. It stands at the end of the series of pairs, as the counterpart to the octave that stands at the beginning:

The octave is the proudest, the noblest of the intervals, and does not mingle with the others; the tritone is the most distant relative, the eccentric, barred from close association with the interval pairs like Loki among the gods of Valhalla—and similarly indispensable. The tritone has no root. It is accompanied by combination tones that stand in an unusual relation to it.
When its two tones are in their closest position (5:7), the combination tones form a fifth which combines with the tritone to make a seventh-chord, in which the lower tone of the tritone is the third, and its upper tone (although too low) the seventh. In the opposite, widest position (7:10) the combination tones form a fourth. The latter combines with the tritone to form a four-three chord, in which the lower tone of the tritone is the seventh, and the upper the third of the chord. All the tritone intervals that lie between these two extremes produce seventh chords which are between the two given above. Consequently, the tritone always has a dominant effect. It is characterized by a tendency towards a tonic, a tendency most naturally satisfied by a progression which takes the form of a "resolution" to the progenitor tone of its family (complemented by one or more tones which form with it either an interval or a chord). But already we see the dual nature of the tritone: if the preceding interval-successions have not made the relationship to a progenitor clear, one has the choice between two equally good resolutions. And in the resolution, the ear always hears one of the tones of the tritone as a leading tone to the root of the following tonic chord:

![Diagram of the tritone and its resolutions](image)

But since the ear cannot at once decide which of the tones of a tritone heard without clear family relations is the leading tone, it is always uncertain in its reaction to this interval. On the one hand the tonal uncertainty of the tritone, which makes it vaguer and more opalescent than any other interval, and on the other its strong urge for resolution, which at the moment of progression monopolizes the attention—this combination of indefiniteness and tension is what distinguishes the tritone, and makes it a foreign body and a ferment among the intervals.

Although this sanctimonious interval, at once obscure and insistent, permits us neither from its aural effect nor from its acoustic construction to declare one of its tones the root, we must at any rate, in order to handle it at all, be able to decide from case to case which of its tones is the more important. The sound of the interval itself artfully conceals from us any answer to this question, and we must draw our conclusions from its environment. From the tone, chord, or interval to which the tritone resolves we see to which family-progenitor it belongs. We shall consider that member of the tritone which proceeds by the smallest step to this progenitor (the root of the resolution interval) as the root representative.

![Diagram of the root representative](image)

We can easily understand how the tritone has in all periods of music history held its unique position among the intervals. Instrumental music has arrived at a modus vivendi with it, aided more or less by the mechanization of its method of determining the pitches of the tones. But to the singer, especially the choral singer, it is still loathsome. Musical theory has always been at odds with the "diabolus in musica", and has always treated it with a peculiar mixture of love and hatred. Theorists at first tried to get around it. The Greeks avoided it by the interpolation of a complementary tetrachord (synemmenon) among their four regular ones. In the church modes the device used was the substitution of B rotundum for B quadratum. The rules for organum and descant excluded the tritone, and its revenge was that this exclusion prevented them from prospering. Then a settlement was made: the treatises of mediaeval theorists are an endless chain of attempts to accommodate the "mi contra fa"; solmization is the attempt to take in the unwelcome guest with impunity. Finally, the tritone became the pet of harmony, through the outstanding importance given to all chord formations serving as dominants, through the harmony of Tristan and the chromaticism that followed in its wake, and even through such flimsily based devices as the whole-tone system that...
flourished about the turn of the last century. For us, who have now learned the position of the tritone within the family of intervals, and the grounds of its claim to that position, it has lost its terrors. Yet even for us it remains a civilized demon—"der Geist, der stets verneint": the spirit that ever denies.

7

Significance of the Intervals

The inclusion of the tritone completes Series 2. To refute once and for all the superficial observation that might be made—to the effect that Series 1 and Series 2 are so much alike, except for a slight difference as concerns the thirds and sixths, that the setting up of two series is superfluous—let us once more state briefly the difference between them.

Series 1 consists of tones, in relation to a progenitor tone from which they derive their tonal position. Series 2 consists of intervals, without relation to a progenitor tone. (Instead of taking c' as the point of departure for our interval series, we could perfectly well have taken a different tone as the basis of each interval, without disturbing the orderly procedure of our investigation in the slightest; whereas in the construction of Series 1 that would not have been possible.) In the following example:

\[ \text{\includegraphics[width=0.5\textwidth]{example}} \]

the effect of Series 1 is such that the g', as fifth of the c', assumes a preferred status. The a', as major sixth of c', is less closely related, and the e', as major third, even less closely. (As we shall see later, Series 1 will not be used for the analysis of such small tonal groups; it will be reserved for higher purposes, and is instanced here only for the sake of comparison.) Series 2, on the other hand, tells us that the skip of a fifth (g'–c') is stronger in harmonic effect than the skip of a fourth (e'–a'), which latter, however, is stronger than the third c'–e' or the second a'–g'.

The value-order laid down in Series 2 brings us close to the question of the consonance or dissonance of intervals. The interval-pairs do not indicate by a gap of any kind that there is any point at which the consonances stop and the dissonances begin. The two concepts have never been completely explained, and for a thousand years the definitions have varied. At first thirds were dissonant; later they became consonant. A distinction was made between perfect and imperfect consonances. The wide use of seventh-chords has made the major second and the minor seventh almost consonant to our ears. The situation of the fourth has never been thoroughly cleared up. Theorists, basing their reasoning on acoustical phenomena, have repeatedly come to conclusions wholly at variance with those of practical musicians.

Our investigation dissipates the fog that has hitherto prevailed. We know that no point can be determined at which "consonance" passes over into "dissonance". We can afford to let these terms stand for the extreme boundaries of the satisfying and unsatisfying effect of intervals and chords. The consonant intervals would then appear at the beginning of Series 2 and the dissonant at the end. But the rate at which the consonance of the intervals near the beginning decreases and the dissonance of those near the end increases cannot be determined exactly. Between the octave as the most perfect and the major seventh as the least perfect intervals, there is a series of interval-pairs which decrease in euphony in proportion as their distance from the octave and their proximity to the major seventh increases. The tritone belongs neither to the realm of euphony nor to that of cacophony; here again, as a unique interval, it remains outside our classification.

We have constructed Series 2 on the basis of the combination-tone curves, in the order of increasing complexity. The history of Western music has followed the same path through the centuries in its recognition of the values of the harmonic intervals. The ear at first recognized only single, monophonic lines, consisting of nothing but fundamental tones (tones numbered 1 in the overtone series). In the course of time, proceeding from interval to interval, it discovered the secret of composites consisting of two or more tones, the secret contained in the combination tones. Singing in
octaves occurred before the earliest beginnings of polyphony, as the natural consequence of the participation of voices of different registers. Successions of parallel fifths and fourths were the first polyphonic devices; and gradually the value of thirds and sixths became apparent. The tritone was—here, too—an exception: it appeared comparatively early, as a component of independent harmonic formations. This would seem curious if we did not know that uninterrupted successions of triads seemed to the musical ear, even in the earliest polyphony, a too unalloyed pleasure. Composers met the ear’s desire for a more intense sound by introducing the tritone in its mildest form: the first inversion of a diminished triad. The intervals between the pairs of tones contained in this chord are only, apart from the tritone, the minor third and the major sixth; the harsher seconds and sevenths are still lacking. They slipped into harmonic combinations late in the development, and then only by the side-entrance of melodic function (passing tones), until at the end of the seventeenth century the ear had learned to accept them, too, as independent intervals, usable for harmonic purposes. The tritone lies at the top of the inverted diminished triad; the important bass tone is free to move, unhampered by the tritone. Even today, minor seconds and major sevenths have not attained full equality with the other harmonic intervals; and a thousand years of familiarity will not achieve it for them.

For intervals are not like clay, which receives an impression and faithfully preserves it until the next one comes along and effaces it; they are elastic, rather, like steel, and although they vary in hardness, none of them is completely pliable. If we spoke earlier of breaking the will of the tones, this must have meant that we must see to it that the force that is latent in the intervals must be prevented from simply acting freely as it chooses—not that we could by main force stamp the raw material into any shape, without regard to its natural elasticity. Under wise treatment, the tonal material can be easily bent and welded. But if too great a strain is put upon it, or if it is not handled in accordance with the laws of its own nature, it will break like any other building material, and the music constructed from it will be useless.

Harmonic and Melodic Value of the Intervals

Every tonal movement arises from the combined working of harmonic and melodic forces—to ignore the rhythmical element for the moment. Harmony is the more robust of the two elements. It has its own tendencies and it is hard to force. There are many possible harmonic combinations, and the gradations between them are innumerable. The very quantity of the material commands the composer’s thorough consideration, and “inspiration” and “invention” can be effective only on the basis of adequate technical knowledge. The novice will hardly succeed in traversing the harmonic territory, which abounds in a wealth of the most manifold phenomena. Melody is less aloof. Many a dilettante, who has no conception of the craft of the composer, gives birth to pleasant melodic ideas. The melodic material is easier to conquer, being of limited extent, and light and airy as compared with the harmonic. But it is also more deceptive. In no field are taste, musical culture, and genuine inclination or the lack of it more important than in melody.

Harmony and melody are complementary elements. Neither is strong enough to stand alone; each needs the other for its full unfolding. Melody sets the sluggish harmonic masses in motion for no harmonic progression can be made except through melody—that is, by traversing the intervals. Harmony, on the other hand, connects and organizes the waves of melody.

Since intervals are the stuff of music, every interval must have harmonic and melodic characteristics. Series 2 shows the distribution of these characteristics clearly:

![Harmonic Force](image)

![Melodic Force](image)
Harmonic force is strongest in the intervals at the beginning of the series, and diminishes towards the end, while melodic force is distributed in just the opposite order. The strongest, most unambiguous interval, after the octave, which is unique, is the fifth, while the most beautiful is the major third, on account of the triad formed by it with its combination tones. From this point on, the harmonic effect decreases, until it nearly disappears in the minor second and major seventh. These two intervals are of almost exclusively melodic significance, since they form leading-tones. They can receive any considerable harmonic significance only through the simultaneous sounding of other intervals. The simplest melodic step of the minor second is followed, reading from right to left (after the minor seventh), by the strongest and most beautiful melodic interval, the major second. Just as the most beautiful harmonic interval was not at the very beginning of the series, so the chief melodic one does not lie at the very end.

Series 2, exposed to the free play of harmonic and melodic forces, now reveals clearly the weakness of those intervals which have the less favorable disposition of their combination tones, i.e., the inversions of the more favorably arranged ones: they offer less resistance. Harmonic force, which begins at the left, is almost helpless against the melodic strength of the seconds, whereas it is not without effect on the sevenths; on the other hand, melodic force, proceeding from the right, is helpless against the strong third, fifth, and octave. When these intervals occur melodically, that is, one tone after another, they organize even the most fluent line into harmonic groups. Their inversions yield more easily. Strong harmonic intervals exert a powerful attraction, while their inversions become more easily the object of attraction, and so are more likely to perform a melodic function. Thus the major seventh proceeds to the octave, the minor seventh to the sixth, the sixth to the fifth, and, at the left-hand side of the figure, the fourth yields to the attraction of the third. In the sixths, the two forces about balance. Harmonic force is not strong enough always to vanquish the tendency to melodic development—the step to the fifth—and on the other hand, sixths are not so strong melodically as to demand invariably melodic treatment.

An understanding of these things makes our admiration for mediaeval musical theory greater than ever, for, with all the limitations of its field, and all its clinging to a heritage at odds with musical practice, it always showed an astonishingly sure instinct in all matters pertaining to the intervals. It knew nothing of the power of attraction of the strong intervals, based on the combination tones, and yet it rejected the harmonic interval of the fourth; and it looked with disfavor on melodic leaps of a sixth, not to mention the use of the harmonic intervals of the second and seventh. We are less timid today. We have learned, particularly, to handle sixths either harmonically or melodically, according to the need of the moment, though even today we avoid the harmonic interval of the fourth in places where force and definiteness of expression are desired.

The tritone has no definite significance, either harmonic or melodic. In order to determine its position, we need a third tone. This third tone may sound simultaneously with the tritone,

\[ \text{in which case the tritone is harmonically determined. Or else the tritone may form a part of a group of three successive tones.} \]

When such groups are not mere broken chords (which would be of purely harmonic significance), and when no special means are employed to make the tritone the most important part of the group, it becomes melodically subordinate. One of its two tones becomes the neighboring tone of an interval that is harmonically unambiguous, which then purges the tritone of its indefiniteness.
The Conventional Theory of Harmony

There are four points in which the conventional theory of harmony appears too narrow a system for the determination and construction of chords:
1. The basic principle for the construction of chords is the superposition of thirds.
2. Chords are considered invertible.
3. By raising or lowering tones of the diatonic scales the chord-supply of a key may be enriched.
4. Chords are susceptible of various interpretations.

As to point 1:
Triads of all species arise from the superposition of thirds, and by the addition of further thirds seventh-chords and ninth-chords are produced. These groups of intervals may be changed, by the rearrangement of their layers, into chords of different degrees of tension. By this simple means, only a small selection from among the possible tonal combinations is made accessible—a selection which includes, to be sure, the best and most useful combinations. But music is caught in a net of which the warp and woof are scales with their inelastic tonal functions and chords with their inversions. Chords that cannot be traced back to a construction in thirds are unexplainable in conventional harmonic theory.

To explain the foregoing simple succession of three-tone chords, which is certainly not at all startling today, the academic theory of harmony has to employ the strangest devices. It may call them appoggiatura-chords or suspension-chords. But here it forgets that an essential part of the appoggiatura or suspension effect is resolution. As long as only the “dissonant” chord is present, and not its resolution, the conditions of an appoggiatura are not fulfilled, and the chords must be looked upon as independent entities. Or it makes the ridiculous assertion that the chords are incomplete, or that they are substitutes for other chords. But who is to decide in each case what parts of the chords are lacking, or for what other chords these are substituting?

As to point 2:
Simple three- and four-tone chords can be rearranged so that their inversions are recognizable as other forms of an original position. That is no longer easy even with ninth chords, and the conventional theory of harmony, in order not to have to burst the bonds of its own rules, chops off parts of these chords in order to fit them into its bed of Procrustes—the inversion system. But the majority of chords, especially those not built up exclusively in thirds, cannot be inverted:

The foregoing formations would lose their character and their sense if their members were rearranged. And we cannot even invert them according to the rules of harmony, since we do not know to what root-tone they are to be related.

As to point 3:
The tonal relations to a basic tone are not exhausted in the tones that belong to the scale of a key. In order to be able to include chords containing tones foreign to the scale of a key without abandoning that key, resort was had to the concept of alteration. Originally conceived to justify a few very common departures from the simplest tonality (such as the lowered sixth degree, and the Neapolitan sixth chord), this idea was expanded to shelter everything else that did not easily fit into the tonal structure, and the result was that such uncertainty and ambiguity were introduced into the system that the only rule that remained valid was: “Any chord can occur in any key.” That is the end of the diatonic system; we are now on chromatic ground. In the diatonic system, however, the newly added chords are looked on as subordinate harmonies, almost
as unwelcome intruders, whereas in the chromatic system they are considered from the first as independent members of the tonal system.

As to point 4:

If so definite a phenomenon as the dominant seventh chord (taken as a single example of the ambiguity which every chord possesses in harmonic theory) may be interpreted according to function and notation as being either in fundamental or in six-five or in four-three position,

the system is wrong. Of course it would be foolish to say that this chord has the same harmonic significance in all three forms, simply because it sounds the same. Similarly A takes on a different function in the domain of C than in that of F; and what we concede to the individual tone we cannot deny to the chord. Thus we see that in the first of the three resolutions the g' is related to the c'—is in fact its closest relative, as Series I shows us. In the second progression it is less closely related to the following root, of which it is the minor second. Naturally, this more distant relationship cannot produce so strong a harmonic step as occurred in the first instance. The third progression, in accordance with the relation of the roots of the two chords, which is what governs, is between the other two in strength: the g' (f#') is the major third of the following d#1 (c#'). From this example we see that the susceptibility of chords to various interpretations is not rooted in sound at all, but springs from the conflict between the acoustic phenomenon and its notation. On the keyboard there is no such ambiguity. Whether a triad is written dBb-Fb-Abb or Bx-Dx-Ax, it is always played on the keys c-e-g, and always sounds so. If we had a tempered notation, there would be only perfect, major, and minor intervals. Augmented and diminished and still more extreme categories would disappear, except in the case of the tritone, which would be the only interval to retain the ambiguity that is indicated by the terms diminished and augmented, and could never be expressed in terms of the normal measures of other intervals. If it is possible to regulate sound to the point where the fine interval-gradations disappear between the keys of a tempered keyboard instrument, it should be simpler still to introduce a solution along similar lines into so purely external a medium as notation. Whether this will ever come about, and to what extent it would be possible to reform notation so that it not only would have one symbol for each of the twelve tones, but also would include all the other improvements that are urgently required, we need not consider here. So long as we continue to use the double notation in sharps and flats, we must of course insist on the most logical and consistent notation of musical phenomena, just as in reproducing the spoken language in writing or in print we stick to the traditional spellings, and continue to use the spelling "sh", for example, while other systems of writing, such as the Cyrillic, or the phonetic, employ much simpler and clearer symbols.

Our somewhat complicated system of musical notation has the advantage of giving the singer or the player (especially of untempered instruments) in most cases a clear impression of the melodic or harmonic intentions of the composer. For analysis of the sound itself, on the other hand, it is not only worthless but actually a hindrance. For in such analysis our thesis must be that all intervals and chords are perceived, independently of their notation, as the ear first hears them, without reference to what has gone before or what comes after. The ear does not hesitate, in the course of this perception, between making all the necessary calculations of minute interval-differences, on the one hand, and, on the other, applying to each chord or interval the measurements derived from the simplest proportions of the overtone series. It always adopts the latter course, and hears every interval, even such as do not actually fit, as being of about the size of one of the intervals that we know from our two series. An interval whose tones stand only roughly in the proportions 5:6 is always heard by the ear as a minor third, whether it is written and intended by the composer as an augmented second, a minor third, or a doubly diminished fourth. Aural
analysis thus takes account of no diminished or augmented intervals except the tritone; it hears all other intervals as forms of the intervals derived from the first six tones of the overtone series.

Now this thesis will seem to many musicians an aberration based on crass materialism. But when they examine their objections closely, they will find that the only support for these objections is in notation—and notation, as we have said, is not to be touched. Apart from their love of correct notation, however, they are by no means so fastidious, for they mostly do not hesitate to use the piano in their teaching of harmony, and that instrument takes no heed of their desire for functional accuracy. They should find food for thought also in the fact that in listening to music on untempered instruments (choruses, string quartets, orchestras, etc.) they would always be faced with the question of which of the various interval-sizes to apply in each case, unless they knew the notation or their ears were kind enough to take care of the question independently. Even the hypersensitive ear goes through this same process of normalization in the perception of intervals, and it is well that this is so, for to an ear that analyzed every harmonic phenomenon with complete accuracy we should not be able to offer any usable tonal system. We should stand helpless before an incomprehensible world of tone. Thus we may recognize in our ability to accept complex intervals as versions of their nearest simple equivalents a friendly gift of nature that makes life bearable for the musical ear, as does for the spirit the ability to forget, and for the body the capacity for accustoming oneself to pain.

10

Chord Analysis

(See the table at the end of this book)

The requirements of a new system of chord analysis follow from our criticism of the conventional theory of harmony.

1. Construction in thirds must no longer be the basic rule for the erection of chords.

2. We must substitute a more all-embracing principle for that of the invertibility of chords.

3. We must abandon the thesis that chords are susceptible of a variety of interpretations.

Although all the chords that may be used in music must be covered by our new system in a clear and easily understandable order, it will not completely upset the theses of accepted harmonic theory. Despite the required basic changes, we shall make no such alterations within the relatively small domain covered by the chord analysis of the familiar theory of harmony that a stranger, wandering into our new structure, would be entirely lost. The ground-plan of the old building remains; it has simply been incorporated into a much larger one. The new structure must thus be regarded as a great and timely extension.

As to point 1:

We define a chord as a group of at least three different tones sounding simultaneously. Two tones do not form a chord, no matter how often they are doubled in any number of octaves; they form only an interval. The principle which is to replace that of the superposition of thirds as the basis for chord erection we derive from Series 2, and from the root effect connected with one tone of every interval. This principle will be clearest without a great deal of explanation and description if we approach it indirectly: We shall examine the nature of various kinds of chords, in order to deduce from them the means of synthesis.

At the beginning and end of Series 2, separated from the pairs of intervals, we have the octave and the tritone. The octave has no significance for chord analysis, since all it can do is to increase the weight of one tone of an interval, by doubling, without making any essential change in the content of the interval. The tritone, on the other hand, stamps chords so strongly with its own character that they acquire something of both its indefiniteness and its character of motion towards a goal. There thus arises an essential difference between chords containing a tritone and those without one; and our sense of the stability of chords and intervals thus divides the entire chordal material into two groups: Group A in-
cludes all chords that have no tritone; Group B includes all chords containing a tritone.

If we appraise the intervals of Series 2 according to the degrees of relationship of Series 1, the five pairs of intervals will divide into two classes: those consisting of the first-generation descendants of the progenitor tone (fifths, fourths, thirds, and sixthths) and those formed from the "grandchildren" (seconds and sevenths). This classification enables us to make a subdivision of the chords in Groups A and B. For if we construct chords using the intervals belonging to the first of these classifications only, it follows that such chords, owing to the simplicity and purity of their constituents, must form one division, the chords of which will be simpler and purer than those containing seconds or sevenths, which form the second division. About these we shall have more to say later.

Now as to the third factor that must be taken into consideration in our judgement of chords: the root, and its position in the chord. Chords consist of intervals, and since in each interval one of the tones is the root and dominates the other, the interval-roots try to bring other tones under their control, and to exert their dominance in the chord as well as in their own intervals. Every chord, then, with a few exceptions to be mentioned later, has a root. To find it, we must find the best interval of the chord, appraised according to the values of Series 2: the fifth is the best, the major seventh the weakest of harmonic intervals (except for the tritone). For our calculation, we must take into account every interval in the chord. A major triad thus consists of a fifth, a major third, and a minor third. Here we see the difference between our method and that of the conventional theory of harmony, which relates the chord factors to the bass tone, a process which makes inversions possible. But at the same time it reckons with the intervals of the uninverted, fundamental position of the chord, so that the root remains the same in all inversions, and the other tones of the original position also retain their original functions in the inverted position. This double reckoning is inaccurate; there can be but one basis of calculation if misunderstandings are to be avoided. We say, on the other hand: if there is a fifth in the chord, then the lower tone of the fifth is the root of the chord. Similarly, the lower tone of a third or a seventh (in the absence of any better interval) is the root of the chord. Conversely, if a fourth, or a sixth, or a second is the best interval of a chord, then its upper tone is the root of the chord. Doubled tones count only once; we use the lowest one for our reckoning. If the chord contains two or more equal intervals, and these are the best intervals, the root of the lower one is the root of the chord.

It makes no difference whether the tone that completes the best interval lies in the same octave or one or more octaves higher (in fifths, thirds, and sevenths) or, on the other hand, one or more octaves lower (in fourths, sixths, and seconds). In those occasional instances in which the compass of the whole chord is so great that the distance between the two tones of the root-determining interval permits the formation of "dissonant" combination tones such as were mentioned earlier, in the discussion of separate intervals (pp. 72-4), we have the choice either of making new rules or of simply treating the widely extended intervals like their closer prototypes.
Here, too, I hold it unnecessary to set up special rules to govern these few exceptions, instead of applying to the latter the rules that hold in the great majority of cases. We may therefore without hesitation treat extended intervals like those of Fig. 66 as fifths, fourths, etc., and accordingly assume the roots of these chords to be C, c, G, C, and B♭.

In such unusual chord arrangements as

it would usually be better to take melodic influences (such as will be discussed later) into account, rather than to rely exclusively upon harmonic analysis. These chords would then become subordinate to others more easily analyzed, so that either the roots which our rules would lead us to deduce (♭ and ♭, for the chords of Fig. 67) would be confirmed by their context, or else the more effective roots of the predominant chords would make the analysis of the formations here notated unnecessary.

As to point 2:

In the conventional theory of harmony, the inversion of a chord never has the same strong and definite effect as the chord had in its original position. For in the fundamental position the root and bass tone are the same; the root, already the strongest tone of the chord, is further strengthened by its position at the bottom of the chord. In inversions the two forces are separated; the root is now in an upper part of the chord, and opposing its strength to that of the bass. Strictly speaking, it is not the rearrangement of the tones of a chord that constitutes an inversion, but the transposition of its root into an upper part. Hitherto the fact that one chord (an inversion) had to be related to another chord, of different structure (the original position, in which the root and the bass tone were the same), has prevented a comprehensive use of the principle of root-transposition. By freeing this principle from its fetters, we gain not only a wider view over the domain of numerous chords not hitherto covered by harmonic theory, but also a new criterion for the appraisal of chords. All chords in which the bass tone and the root are not identical are subordinate to chords whose other characteristics (root and chord-group qualities) they share, but in which the root and bass tone do coincide. Here, too, we do not care whether the interval which determines the root lies in the closest position in the chord, or whether its tones are spread out over one or more octaves. There is, it is true, a difference in the sound and in the value of chords in which the root is emphasized by the close proximity of the tones of the intervals which determine it, as compared with those in which the root is weakened by being widely separated from its partner. But if we were to take account of these subtlest differences we should not be able to erect any practical system, since each tonal combination would have to have its own individual niche. The division here proposed may, however, despite the sacrifice of excessive subdivisions of sufficient accuracy, be accepted as a basis for the complete understanding of all chords, as will be seen when the picture is complete.

There is a kind of rearrangement of chord-tones which is not to be regarded as inversion, since it does not affect the root tone—which remains stationary—but simply transposes its complementary tone (perhaps with other chord tones) into a different octave. This is a change of what the accepted theory of harmony calls position ("close", "open", "mixed", "position of the octave", "fifth", "third", etc.). The ranking of the chords in the following example is the same whether they appear in form A or form B,
since it follows from what has been said that the increased distance between the root and its complement, despite the slight change in effect which results from it, does not affect the values we assign to the chords. This closing up or spreading out of the chord-tones is not possible in all combinations. Chords which, owing to their simple structure, possess only a mild tension are not greatly altered by such changes. But chords containing many tones lose their particular character when they undergo such changes of position. Exactly where the boundary lies between these two types of chords can be decided only in each individual instance.

As to point 3:

The division of chords into two main groups (A and B), the members of which are then further ranked according to their component intervals and the position of their roots, does away with all ambiguity. It does not, of course, abolish the harmonic uncertainty of the tritone. But anyone who considers this a failing should balance the uncertainty of a few chords against the inaccuracy of a system in which any chord may have a different meaning from that which the ear assigns to it.

As a matter of experience it is established that the tritone, when combined with other intervals to form a chord, subordinates itself to the best interval of Series 2. The intervals of the first two pairs (fifth and fourth, major third and minor sixth) do away with its uncertainty, but yield readily to its tendency towards a resolution. Thus it happens that in tritone chords containing these intervals the root is just as strong as it is in the chords of Group A, but stability is nevertheless lacking.

The intervals of the next pair (minor third and major sixth) have less strength to combat the uncertainty of the tritone and thus to make of it a clear harmonic combination:

Thus a chord which apart from the tritone possesses only a minor third or a major sixth remains as ambiguous as the tritone itself. Just as in the tritone itself, one of the tones of such a chord will be called the root representative. The contextual chord-succession determines which of the tones performs this function. There are only four such chords: the diminished triad with its two inversions and the diminished seventh chord.

Among the chords which have no tritone, also, there are two of which the interpretation depends on the context:

and which in consequence have no root, but only a root representative: the augmented triad and the chord composed of two superposed fourths.

Subdivision of the Chord-Groups

Within each of the two main Groups, A (without tritone) and B (with tritone), three subdivisions may be made, according to the principles already discussed. We shall label them with Roman numerals, so that Group A contains the sub-groups I, III, and V, while Group B contains II, IV, and VI.

Sub-group I of Group A contains chords having no seconds or sevenths, and in its first section (I,) only those in which the root and the bass tone coincide—in which, that is, the best interval is based on the bottom tone. There are but two chords that fulfill these
conditions: the major and minor triads. These noblest of all chords constitute a section in themselves. They alone are completely independent, capable of being used for conclusions, and of being connected with any other chords. The chords of the next section (I,) stand a little lower in the scale of values. These are the chords in which the root is not the lowest tone; the inversions of the major and minor triads. On account of the high position of the root, they are not independent enough to form satisfying conclusions; but otherwise they perform in somewhat weaker fashion the same functions as those of the preceding section. All the chords of these two sections are at most three-voiced; any additional tones can only be doublings of tones already present. These chords exhaust the possibilities of combining the intervals consisting of the tones most closely related to the progenitor tone (the "sons") in Series I.

The corresponding sub-group of Group B (II), contains the chords of three or more voices in which the tritone is subordinate to stronger intervals. The requirement that the chords must contain no seconds or sevenths cannot be maintained here, for the presence of the tritone always (except in the diminished triad and its inversions) involves seconds or sevenths. Yet in this sub-group we shall limit ourselves to major seconds and minor sevenths, as the less sharp representatives of their species. The mildest form of the intensification brought about by the presence of the tritone is the minor seventh, in a chord from which the major second, as the stronger and sharper of the two intervals, still remains excluded; the chord's stability is ensured by the coinciding of the bass tone with the root. In this section (IIa) we thus find only the two most important tritone chords: the complete dominant seventh, and the same chord without fifth. The chords in which the major second as well as the minor seventh may appear fall into three sections. The first (IIb,) includes those chords in which the root and the bass tone are the same: the strong dominant chords which are the next simplest after the dominant seventh, and which in their structure lean heavily upon the chords of their neighboring section (I,), the triads. The second section (IIb,2) contains the chords in which the root is not at the bottom: the inversions of simple dominant chords and similar structures. Common to all the chords of sub-group II thus far named is the fact that they contain only one tritone. The chords of the third section (Iib) are similar in every respect but this: they contain two or even three tritones. These chords are not included in the foregoing sections because their sound is so strongly colored by the tritones; yet they are not so intensified as to require assignment to sub-group IV.

Sub-group III of Group A contains chords of any number of tones which are extended by the addition of seconds or sevenths. These are a rough and unpolished race. The best of them are those with three or four tones, which either contain one of the chords of sub-group I, or at least in some of their tones approach this unattainable prototype very closely. And the chords that lack minor seconds and major sevenths (i.e., those limiting themselves to major seconds and minor sevenths) are of a higher class than the very sharp and grating ones which contain these intervals. None of the chords of sub-group III are independent; all of them depend very much on the course of melody; and they cannot be connected with all other chords. They include the secondary seventh-chords with their inversions. The first section again contains only those in which the root is in the bass; the second section contains those in which the root is in a higher part.

Sub-group IV contains a strange set of piquant, coarse, and highly colored chords. All the chords that serve the most intensified expression, that make a noise, that irritate, stir the emotions, excite strong aversion—all are at home here. The chords of this group can have any number of tritones, and the number of minor seconds and major sevenths is likewise unlimited. It would be unreasonable to expect chords of such strongly marked individuality to lend themselves without resistance to all chord-successions, as do triads and the simpler tritone chords. They are often very intractable, especially when they are used in progressions involving chords from various and rapidly changing sub-groups. The best of them are the easiest to handle—those that consist of only a few tones and that resemble chords of the simpler sub-groups.

Sub-groups V and VI are small. They contain the above men-
tioned uncertain chords—chords consisting of several superposed intervals of the same size. The first chord of sub-group V consists of two major thirds and an augmented fifth. The augmented fifth can be counted a minor sixth, in accordance with what we have already established, and thus the constituents of the chord belong to the same pair of intervals, and the root cannot be definitely determined. The chord built up in fourths, which belongs to group V, may occur in forms in which its root can be determined. It is uncertain only in its closest position (see the table), or when its highest tone is doubled above or its lowest below, or when the outer tones are spread an octave further apart and there is an octave doubling of the middle tone between them ($c^f d^f b^f$). Any other doublings produce a fifth as the best interval of the chord, which would place it in sub-group III. The same is true even when it consists of only three tones, expanded or contracted by the octave transposition of one of them. If we add further fourths above, we had better assume the presence of a root, for the choice of possible root representatives becomes too great. Accordingly we shall treat all chords consisting of three or more superposed fourths as having the root of their lowest fourth as the chord-root. Two superposed fifths do not belong to group V but to group III; likewise two superposed major or minor seconds. Chords consisting of two or more superposed minor thirds constitute group VI.

For handling the chords of Group B (those with tritone), it is not enough to know their roots. If we are to be able to make convincing chord-progressions, we must treat the tritone as their most important constituent. We find the root by the familiar method. But, in addition, one of the members of the tritone must serve as the guide-tone. To find the guide-tone, the following rules apply:

1. That tone belonging to one or more tritones in the chord which stands in the best relationship to the root (measured by the interval-values of Series 2) is to be considered the guide-tone:

![Diagram 1](image1)

In doubtful cases—as for example, when a choice must be made between two tones which lie above and below the root and are equally related to it—let that tone be taken as guide-tone which, itself a part of a tritone, leads best to the root of the next chord (if that chord has no tritone) or to the guide-tone of the next chord (if it contains a tritone).

2. When there is only one tritone in the chord, and the root forms a part of this tritone, the other tone forming the tritone is to be considered the guide-tone.

![Diagram 2](image2)

When isolated intervals appear between one chord and the next, they are to be regarded as belonging to that group to which their own nature would assign them. The fifth and the thirds belong to I, the fourth and the sixths to I, the seconds to III, the sevenths to III, the tritone to VI.

This system of appraising chords and intervals results in a classification of all chords. There is no combination of intervals which does not fit into some division of our system. Chords which a theorist would analyze only in his nightmares, and which any self-respecting counterpoint book would not tolerate, can now be easily explained.

The system is as comprehensive as it can be, in view of the possible variety of chords. Nevertheless, even by this system, there will always remain a certain number of exceptional chords which cannot be interpreted with complete satisfaction. These include those which consist of so many different tones that the individual units of which the structure is composed hardly count, as well as those which, although they contain only a few tones, are so spread out that their constituent tones can only with difficulty be perceived as constituting harmonic intervals. But it is a question whether a system of investigation which aims to make clear the harmonic side of tonal combinations should be applied to chords which, like the first-named, are effective chiefly through their intensity, their mass, or their energy, or, like the second group, result simply from the isolated effect of single tones or lines. An investi-
gation of these border-line cases will, however, produce an easy 
modus vivendi with such structures.

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The Value of Chords

The complete material of the conventional theory of harmony is 
contained in our sub-groups I, II, and VI, except for an isolated 
chord here and there belonging to groups III and IV. And, of course, 
all possible chords may occur under conventional harmonic theory, 
but it accepts them only as structures resulting from strong melodic 
tendencies, and it interprets all tones that complicate chords be­
yond the familiar limits of triads and seventh chords as passing 
tones, suspensions, appoggiature, etc. When one of the chords 
belonging to our groups III or IV shows an urge for independent 
existence, and cannot be explained as consisting of appoggiature 
or suspensions or passing tones, it is considered simply as non­
existent. There is no room in a well-ordered household for such 
rabble; they had better be chased from the door, before one is 
tempted to examine them more closely.

In another way, too, the familiar theory of harmony prevents 
chords from the free unfolding of their vital urge. For it proclaims 
as the highest harmonic law the relationship of tones and chords 
in a key. The diatonic scale with its limited possibilities deter­
mines the position and rank of the chords, which are the mere 
satelites of this power. The chord must blindly subordinate itself, 
and attention be paid to its individual character only as the key 
allows. This theory of harmony is like an employer who keeps a 
small number of gifted and versatile artisans at work. They are 
tied to him for better or for worse, and he has always kept them 
so dependent upon him that they are no longer capable of making 
their own decisions. Therefore he places a supervisor over them, 
who plans and thinks for them. The work of such men will never 
rise above a certain quality, since the directing personality is not 
onniscient and not equally well prepared at all times and for every 
contingency, since work which is not free cannot develop beyond a 
certain point, and finally since although the versatile and highly 
trained workmen are masters of many trades, the very quantity 
of their skills prevents them from the development of new and 
rationalized methods and the acquisition of specialized knowledge.

Our enterprise works along different lines. It has a far greater 
number of workmen at its disposal, and their work varies greatly 
in its value to the whole. From the special craftsman with the high­
est ability to the know-nothing, and from the most industrious 
worker to the drone, we can call upon people of all grades of ability.
We can therefore put at each place a workman whose abilities cor­
respond to the functions he must perform, and who will accordingly 
perform them faster, better, and more reliably than a man impeded 
by his very versatility. On the other hand, it is extravagant to 
waste the abilities of superior workmen at jobs which, though 
indispensable, can be performed by know-nothings and drones who 
could do nothing else. Our work thus becomes a competition among 
the strongest forces, which accomplishes more than the laborious 
execution of the arbitrary plan of any supervisor. But in order that 
our effort shall not flow off into all sorts of side-channels, there is 
a group of workmen of higher rank who take up the individual parts 
devised by specialists, put them in place, and assemble them accord­
ing to a plan worked out by a director of operations in adjustment 
to the needs of the market and the capacity of his plant. We have, 
accordingly, the most thoroughgoing specialization in the lowest 
levels of our production process, directed from above, firmly, but 
with an intensity that springs from a clear consciousness of purpose 
and the ability to fulfill it.

Let us translate this into musical terms. It means that the key 
and its body of chords is not the natural basis of tonal activity. 
What Nature provides is the intervals. The juxtaposition of in­
tervals, or of chords, which are the extensions of intervals, gives 
rise to the key. We are no longer the prisoners of the key. Rather, 
we now have a free hand to give the tonal relations whatever aspect 
we deem fitting. The different harmonic tensions which we need 
for this purpose are indicated by the ranking of the interval-values.
If the intervals are of different values, then the chords constructed
of them must differ correspondingly. A closer investigation of our chord table will confirm this statement.

From the considerations which impelled us in setting up our table it follows as a matter of course that the chords having no tritone (Group A) are of higher rank than those in which the tritone occurs (Group B). This general rule is however modified by the division of the chords into sub-groups with the result that sub-group II contains chords of higher value than those of sub-group III, even though the latter belong to the higher Group A, and similarly sub-group IV is higher than V. The tonal value of the sub-groups thus diminishes from I, containing the purest combinations, through the simple tritone chords of II, down to the uncertain chords of the lowest group, VI. Within the individual groups I-IV there are finer degrees of distinction, so that the higher numbered sub-sections come after the lower in the scale of values. Thus IIa is of higher rank than IIb, which in turn outranks IIb, and IIb; but we must not forget that IIb is higher than III. Thus in chord-successions a move from lower-numbered to higher-numbered chords is a step down; or, to put it in general terms, based on the visual appearance of our table: Every step downwards or to the right means a decrease in chordal value, and every step upwards or to the left an increase. (Chord-progressions toward a member of groups V or VI may represent an exception to this law; this possibility will be discussed later.) We have already stated that further distinctions are possible among the chords of one and the same group, but that the systematization of such differences would lead to an atomic view of our chordal material.

We may state the result of our investigations into the qualities of simultaneous tone-combinations as follows: In contrast to the conventional theory of harmony, in which all tones and tone-combinations are ranked according to their relation to an a priori tonal scheme, and thus have only relative values, our system attributes a fixed value to each. Between those of highest and those of lowest value we recognize a great number of gradations, each of which has a constant value. How tonal groupings result from the conjunction and contrast of these values is the subject of the next chapter.

CHAPTER IV
Harmony

Movement in Chord-Successions

We have seen that the individual tone is useful for musical purposes only as a result of the interval between it and another tone. Similarly, a chord, which is an aggregation of tones, has musical significance only when the appearance of another harmonic aggregation creates a space between them. The spanning of this gap—chord-connection—is the beginning of all harmonic reality. Thus in the realm of chords the procedure is the same, on a higher level, as that through which the simplest of all tonal building units acquired its significance: the creation of tension by the juxtaposition of two entities.

Three forces are at work in chord-connection: rhythmic, melodic, and harmonic. Each of them works in two directions. Rhythm determines the duration of the chords, and groups them by division into stressed and unstressed members of the structure. Melody in voice-leading regulates linear expansion, and in the two-voice framework sets the pitch limits. In the placing of the harmonic center of gravity and in the regulation of relationships we see harmonic energy at work.

We can leave the function of rhythm out of consideration here, but not because it is unimportant. Without rhythm—that is, without relationships in time—neither of the other forces could operate. It is rather the all-pervading force of the primeval element of rhythm that allows us to take it for granted, and to simplify our
work by ignoring it. Furthermore, all questions of rhythm, as well as of the formal characteristics of composition which spring from it, are still so largely unexplained that it seems impossible at the present time to include rhythm as an integral part of a system of teaching the craft of composition. In this work, which does not aim at the complete scientific explanation of the deepest impulses that underlie musical writing, but rather seeks to be of practical use, we shall limit ourselves to the examination of the other forces. Whereas rhythm can find expression without relation to the tones and chords—in fact, without relation to sound itself—these other elements, in order to make themselves felt, must behave according to the laws which we have come to know in Series 1 and Series 2. They thus form a coherent group, different from and counterbalancing the rhythmic element. We are limiting our field of investigation by excluding from it on the one hand the primary musical elements—pitch, intensity, and timbre—and rhythm, and on the other hand the forces of dynamics, phrasing, and agogics, which of course affect chord-connections but do not change them.

The special characteristics of melodic structures will be discussed in Chapter V. Still, we must treat the subject of voice-leading at this point in our discussion at least sufficiently to explain its workings in harmonic connections. In one type of musical writing, the form and content of the piece is determined by melodic force; this is contrapuntal writing. When, on the other hand, the chords and their connections are what give the piece its character, melody is of less significance.

Between the extreme of linear writing and a texture so thoroughly chordal in purpose there are innumerable species of the mutual interpenetration of melodic and harmonic forces. What determines our assigning of a composition to one or the other domain is not so much the external appearance as the basic attitude of the piece. In contrapuntal writing the composer takes the idea of movement as his point of departure, and the chords come about as the product of the play of line (although this product itself must have its own logic)—they form the adhesive which binds these lines together. In chordal writing, the composer sets out with the opposite idea: he breaks up the inert chord masses and breathes life into them by dividing their components among moving voices. The binding together of the flowing lines may be so firm, and the breaking up of the chord masses may set so much movement free, that a music in which the most alive linear movement is combined with the most logical harmonic progression can hardly be classed as primarily one thing or the other. In an idiom employing really independent voices, every tone of one chord moves to a tone of the next, while in a more compact idiom (such as in keyboard writing) no such melodic progression of the individual tones is sought, and it is rather chords that are juxtaposed, in whole or in part. Thus harmonic masses are set into flowing motion by melodic means of progression, on the one hand by the aggregation of individual movements of tones, and on the other by the shifting of entire chord-structures (see also Chapter III, Section 8).

In well balanced progressions involving really independent voices, all melodic steps are of great (though not of equally great) importance. It is not true, as many a theorizing aesthete would have us believe, that the voices are absolutely free to move as they choose, and that the chordal aspect may then be left to assume whatever shape it will. To leave the harmonic dimension, which alter rhythm and melody is the most important element of music, to chance—would this not be like planning only the horizontal parts of a building? Whether the architect is building a tower or a shed, he cannot escape vertical as well as horizontal elements. He can emphasize one element, and thus subordinate the other, but he cannot wholly exclude either one. In music, too, no matter how much attention is focused on the melodic lines, the harmonic aspect cannot be ignored. If it has no logical relation to the linear texture, and if it is not in itself logically developed, the music is unpalatable.

There is, of course, another linear style of writing from which, despite the convincing nature of the harmonic progression, we derive no satisfaction. Here independence has been pushed too far: every voice has such a strong and independent life of its own that the net result is a maze of activity that is difficult to understand;
rhythm and harmony can no longer impose unity on the various melodic personalities which insist on going their own way. Just as one cannot handle six different kinds of things at the same time, so one cannot follow a large number of independent voices; one's attention is torn hither and thither, and it takes account at each instant only of the most prominent point from among the tangled lines, subordinating the rest. Even two very independent and conflicting lines are hard to follow, unless they are bound together by a fairly simple harmonic foundation. When there are three voices, none of them is completely free in its spatial (melodic) aspect; therefore in skillful three-part writing one of the three voices is always subordinated to the other two. The significance of the voices, their prominence or lack of it, may change within time units less than one beat long. In contrapuntal writing for more than three voices, the relative prominence given to the voices needs even more care; here the sustaining of individual tones, the parallel coupling of voices, and the emphasis of the harmonic content bring about numerous gradations, of which the fugues of Bach furnish the most perfect examples.

Contrapuntal writing does not satisfy all demands. It is found lacking particularly by those players and hearers who seek in music more sweetness and gracefulness, as well as a greater display of force and a more immediate effect than the cool strength and logic of independent lines can produce. Writing which is primarily chordal and homophonic sacrifices the multiplicity of lines, and can accordingly allow to its small linear ingredient, which rests upon the chords as the wave does upon the waters, a freer and more sensuous development. What is important here is the exact fitting of the main harmonic components, and the strength of these easily carries the weight of the less important element; in fact, it carries much incidental and often even much superfluous material as well. The play of line may become so weakened that it can hardly be observed at all; music in which this happens runs the risk of utter futility, or of the same incomprehensibility that attends counterpoint pushed to dogmatic lengths. Incomprehensibility is the result also of too rapid changes of chord, of continual use of the sharpest combinations (those belonging to sub-groups III and IV), and of inaccurate or obscure harmonic progressions. The danger of becoming unintelligible is greater in contrapuntal writing; the chordal style is more liable to sink into shallow insignificance.

The Two-Voice Framework

In both the contrapuntal and the chordal idioms, harmonic development, which is tied to melodic movement, takes place within an external spatial frame—a skeleton which gives the chords the necessary contour. This framework is constructed by the bass voice and the most important of the upper voices. The bass line may be clearly melodic in character, as in contrapuntal writing, or it may hardly rise above connecting the main points of harmonic support, but it will always have, as the lowest voice and the foundation of the structure, decisive importance for the development of the harmony. The next most important line may in contrapuntal writing be entrusted to any one of the upper voices; or, since the voices perform functions of constantly varying importance, it may move about from voice to voice. In the chordal idiom, it will always be found in the “theme” or the “melody”, or whatever one wishes to call the linear formation that floats above the chords. Usually this is the highest stratum in the tonal composite; less often it is embedded in the middle of the chords. If the melodic aspect is so obscured by the rhythm or the harmony that one can hardly speak of any thematic coherence, then the upper voice that results from the chord-successions takes its place. If the bass voice holds an organ point, then the next higher moving voice constitutes the lower half of the framework, although one must be sure that the organ point really leaves the harmony free to develop, and does not have a disturbing significance of its own. For when the organ point becomes a constituent of the harmony (even though only in passing), it loses its organ-point function and is reckoned as part of the harmony. Similarly, when the upper voice holds a tone for some time, the next lower voice becomes the upper member of the framework.
If writing in several voices is to sound clear and intelligible, the contours of its two-voice framework must be cleanly designed and cogently organized. The bass voice must make with the most important of the upper voices, regardless of the difference in register between them, a good, intelligible piece of two-part writing, needing nothing further to complete it. The two voices must not interfere with each other, as they easily may if each is made to bear too much melodic weight; rather must they be contrasted and balanced one against the other, in their shape and in their time-values. This two-part framework is no mere scaffolding to assist the composer in his work; it is a living member of the body of the musical work. Thus it must not be limited to the form of a meaningless two-part counterpoint exercise, note against note. Yet it must also not assume such importance as to reduce the other elements of the piece to insignificance, for despite its importance it is only one part of the tonal structure.

The intervals formed by the two voices must be carefully planned. Thirds and sixths are pleasant intervals, but to construct a two-part texture mainly of them would be to bore the listener with continual sweetness. Seconds and sevenths add strength and tension to two-part writing; yet their continuous use would dull the ear and make it insensible to the subtler charms of the more satisfactory intervals. Thus a combination of euphony and sharpness of sound must be found, appropriate to the nature and purpose of the composition. Tensions and relaxations must alternate. But there is no place here in the Theoretical Part of this work for specific rules governing two-part writing; such rules will be found in the later volumes.

The progression of the two-voice framework is wholly independent of the other tones of the chords. To be sure, these other tones belong to the whole tonal picture just as much as the outlines themselves, but they have no more influence on the latter than the form of the spleen or the liver has on the external appearance of a man. Already in examining the nature of the individual chord we saw that the tones that filled it up, and their close or extended position, did not have the same significance as the position of the chord in space determined by the position of its root. In chord-progressions, then, since they are composed of individual chords, these filling-in tones are also of secondary importance. The path of a chord in space is affected only very little by the inner tones; its shape is determined rather by melodic progression, principally in the form of the two-voice framework. It is in the harmonic relations of the chords, and especially in the shifting of the center of harmonic gravity, that the inner voices play their full rôle.

In the polyphony of all ages and styles this two-voice framework will be found, tracing the spatial boundaries of the harmony. As the contour of the chords it acts as a constant reminder not to allow spots of harmonic color to become so gorgeous as to obscure the drawing itself; it is at the same time, however, like a rudimentary organ that remains in the human body as a heritage from some evolutionary ancestor, an honorable legacy from the dawn of polyphony, a relic of which we can no more free ourselves than we can of such atavistic parts of the body.

### Harmonic Fluctuation

A solid object—a brick, for example—can be pushed or pulled in such a way that its under side remains in uninterrupted contact with the surface on which it rests. But it can also be turned over on its side, or even moved violently enough to turn on one of its corners. In this case we have added to change of position a turning of the object on its own axis, resulting from a shift in its center of gravity. The brick then touches the ground with first one surface and then another. The first of these types of movement corresponds to the harmonic progression in which the relations of all the roots to their respective chords is governed by the same principle—as when none but chords belonging to a single sub-group (I, or I I I, etc.) are used. The second type corresponds to the shift of harmonic gravity; for this we shall henceforth use the term *harmonic fluctuation*.

If we look at the sub-groups of our chord-table—say, at group
I—, we shall see that the chords of the two sections I, and I₂ are differentiated by the position of their roots. The chords of I, are in what the conventional theory of harmony calls inversion: they have been turned side over side or end over end, so that they are lying on their sides or standing on their heads, while the chords of I₂ stand firmly on their feet. Now, we have already seen that there is a difference in value between the chords of these two sections: those of the first section are, because of their strong root-positions, higher in value than the less stable chords of the second. If in a chord-succession a chord of the first section is followed by one of the second, there results, as we have seen, a decrease in value. The step from a more valuable to a less valuable chord is in the harmonic sense, then, a descent, a fall, and conversely a step from a less valuable to a more valuable one is an ascent. But since in our chord-table the harmonic tension of chords increases from section to section and from sub-group to sub-group in the same proportion as the value decreases, the progression from a higher to a lower chord represents an increase in tension, and a step in the opposite direction a decrease. It is this up-and-down change of values and tensions which we shall term harmonic fluctuation. This fluctuation may be gradual or sudden according to the relative values of the chords which make up the progression. In progressions from I₁ to III₂, or from IIb₁ to IV₂, or the reverse, the ascent or descent may be regarded as sudden, because the value-differences are great; here the brick turns side over side or end over end and traverses a good deal of space. Progressions within one sub-group, on the other hand, as for example from I₁a to IIb₁, or from III₂ to III₁, may be considered gradual.

To create any harmonic fluctuation, chords of different value are always needed, be the difference ever so slight: as for example between two chords both belonging to section III₁, of which one resembles the chords of group I more closely than the other, and so stands slightly higher in the scale of values. Harmonic fluctuation is thus not to be confused with the scale of harmonic values which results from relationships within a key. Such relationships can give different significance to chords of the same structure and value: our brick is placed together with other identical bricks, and receives its particular significance from its relative position in the building. In the connection of chords of identical structure there is no harmonic fluctuation; there are only harmonic relations which vary and together with the rhythmic pulse regulate the tonal movement and build forms out of it. The foregoing may be made clearer through the following examples.* In the first example we see six harmonies all belonging to Group A:

The first and last of these harmonies, belonging to section I₁, are the best and most satisfying, while between them a harmonic development takes place which passes through two chords of I₂, one of III₂, and one of I₂ again. Thus there is an increase of tension from the first chord to the fourth, which is then resolved. The harmonic fluctuation is here not very sudden. The greatest gap is between I₁ and III₂, and this gap is smoothly bridged by the I₂ chords. There is a harmonic crescendo and diminuendo that is indissolubly connected with the nature of this progression; it cannot be altered by the performer. It is thus different from purely dynamic increases and decreases, the control of which always rests with the singer or player.

The fluctuation in the next example is less smooth:

* The drawings are intended to give an approximate picture of the changing tension in the musical examples. Beneath the chords of I₁, which are altogether lacking in tension, the upper and lower lines of the diagram come together, while the point of greatest tension corresponds to the widest separation of these lines.
Between the first chord and the second, the gradient, so to speak, is very steep. The highly tense chords of group III give the rest of this progression its character, while the fluctuation among them is not very wide, rising and falling between III and III.

Of all these chords, the fourth is the sharpest, its minor second (or ninth) e'-f exceeding in this respect the major seconds and minor sevenths of its neighbors. Between the next to the last chord and the last one there is again an important change of level, which gives the effect of a considerable relaxation of tension. The next two examples contain chords from Group B (with tritone), the first example restricting itself to the harmless ones of group II, while the second one employs the more biting combinations of group IV. The nature of the harmonic fluctuation will doubtless be clear to the reader with the help of the numbering and the diagrams.

For anyone with some knowledge of the devices of the technique of composition, consideration of harmonic fluctuation introduces no new difficulty, particularly since the conventional theory of harmony takes account of it, even though only to a slight degree: division of chords into those in root position and those in inversion is nothing else. Conventional harmonic theory does not provide, of course, any key to the construction of complicated designs of fluctuating tension; for this we must employ our detailed knowledge of chord-values. Whoever possesses such knowledge can create harmonic structures of the most daring thrust and tension without having to rely on the uncertain method of trying out each individual combination by ear—a process that soon becomes more a guessing game in pursuit of concealed possibilities than a form of creative work. We thus add to the time-honored practices of harmony—voice-leading, and the production of tonal relations—the observation of the rise and fall of harmonic tension as an exact and completely reliable procedure. Since this procedure adds to the accuracy of our planning and execution of harmonic structures, the composer may unhesitatingly accept the added work which this increased material brings with it. The secret of good arrangement of this rise and fall is completely open to him in our table of the chord-values.

The only rule we must observe which involves consideration of individual cases is to remember that the indeterminate chords of groups V and VI introduce an element of uncertainty into harmonic developments. When one is dealing with chords belonging to the other sub-groups, one stands on firm ground; but the introduction of the indeterminate chords is like a step into mud and quicksand. Usually a progression to such a chord represents a decrease in value and accordingly an increase in tension, as our chord-table shows. But sometimes the effect of the use of chords of groups V and VI is such that the whole progression takes on a wavering unsteadiness. The ear still perceives changes of value and tension, but it cannot determine the exact degrees of these changes. In such progressions, therefore, care must be exercised. A single step into uncertainty may be very pleasant, for variety’s sake, but a progression consisting exclusively of uncertain chords is always of poor effect. In such a progression we lose all sense of direction; we seem to be tossed aimlessly hither and yon on an endless series of waves until the ear becomes confused to the point of actual physical discomfort. As a counterpoise to the stable and tensionless chords of group I, a chord from group V or VI may be useful; it can almost always be successfully juxtaposed even against chords from group II. But in using it with chords from groups III and IV, care must be exercised. In the midst of such chords, a chord of group V or VI often puts us completely off the track; it seems to cause the whole chord-structure to collapse. Probably the vagueness which results from the complex, over-sharp profiles of the chords of groups III and IV is unsatisfactory when
associated with the opposite type of vagueness, which results from
the washed-out ambiguity of those of groups V and VI. Progress-
sions of this type must accordingly be handled with extreme care,
if they are not to be entirely inconsistent with the rest of the har-
monic development.

I can imagine that to a reader who is thoroughly entangled in
earlier ways of harmonic thinking the measurement of the harmonic
fluctuation will seem an unnecessary addition to the composer's
task. And not improbably even some readers who have accepted
all the innovations and extensions suggested so far will look on this
one as mere hair-splitting, instead of as a logical part of our system.
Perhaps both types of readers will be convinced of its necessity by
examining the following progression:

\[
\begin{array}{cccccc}
  & I & I & I & I & I \\
I & I & I & I & I & I \\
I & I & I & I & I & I \\
I & I & I & I & I & I \\
\end{array}
\]

The theory of harmony has no place for any of these chords ex-
cept the first and last. It admits only that the example is in a poor
sort of C major. But even our reckoning of the roots tells us nothing
more than that all the chords have the same root, c'. Since, how-
ever, they are, despite that fact, quite different from one another,
we must expand our analysis by the addition of another criterion.
The mere movement of the tones tells us only that against a con-
stant center, consisting of two voices sustaining their tones, two
lines are set in contrary motion (the upper one in parallel fourths),
reaching their widest compass in the fourth chord. In the two-voice
framework we see a unison expanding through a major third and a
minor sixth until it too reaches its widest span, a minor seventh, in
the fourth chord: and then, after the minor third, the indetermi-
nate tritone before the end introducing an element of uncertainty
into the progression. Only in the harmonic fluctuation have we an
explanation for the varying harmonic tension of different chords
upon the same root. We see there that after a sharp ascent from I,
to III₁, the third chord brings a further slight increase in tension,
which is somewhat relaxed in the fourth chord, containing no minor
second. The high point of harmonic tension is in the next to the
last chord. Thus the harmonic fluctuation has a quite different
development from that of the voice-leading or of the two-voice
framework. In this simple example we see the interlocking play of
the structural elements quite clearly. The more carefully these ele-
ments are balanced, the more convincing, the more interesting,
and the more attractive a harmonic progression will be. The pur-
pose of the progressions, the intensity with which they are to affect
the hearer, must always determine the coinciding or contrasting
designs of all the different elements.

In harmonic fluctuation we see how chords compare with one
another as tonal masses of particular forms and densities. We know
that the chords are placed in reciprocal relations by means of
voice-leading. We need no reminder that in these relations even
the most incidental tonal constituent cannot be left to chance. The
composer must find for every chord and every tone the treatment
that will best reconcile his artistic intention with the nature of his
material. For the quick appraisal of chord-progressions, without
which fluent work is inconceivable, a sort of abbreviated reckoning
is employed to indicate the value of a progression and to show its
direction (about which the harmonic fluctuation gives us no in-
formation). For this purpose, we make use of the roots of the chords,
and in our study of this subject we shall restrict ourselves to the
simplest relations: those between the roots of two adjacent chords.
These two roots, once they have been extracted from their chords,
we shall now consider apart from the tonal masses in which they
originated, simply as two tones of given pitches without chordal
relations. As such, they form an interval which has all the char-
acteristics we observed in Chapter III. Here, as in that chapter, a third is a strongly harmonic interval, while a second is essentially melodic; in short, we stand once again before the whole series of interval-values. This juxtaposition of roots derived from chords is a reliable means of judging the value of a chord-progression, equally useful for the analysis of progressions already in existence and for the construction of new ones.

Let us examine the chord-progressions within Group A, which because of their independence and complete certainty will furnish the clearest illustrations of what has been said. The simplest progressions are those involving only the chords of sub-group I. In the following example we see the roots of two adjacent chords first at the distance of a fifth, then of a fourth, and so on up to the major seventh (minor second).

A progression based on the interval of a fifth between its roots naturally has a surer foundation than one based on a minor sixth: this is the strongest of all chord-progressions. If we keep the values of the chords equal (as we have determined to do here, confining ourselves to the chords of group I), then the next best progression after that based on a fifth is that based on a fourth. Then follow in the familiar order progressions based on root-progressions of a third and a sixth, in which the softness of the root-progression is not only repeated but multiplied in the movement of the tonal masses of the chords. The melodic step of a second is similarly confirmed in the chord-progression based on it. The experience we have had with Series 2 teaches us that a chord-progression based on a root-progression of a tritone will be the least valuable of all.

The nature of root-calculation should already be clear from the few examples given. It serves the same purpose in the realm of tones, roughly speaking, as logarithms do in the realm of numbers: the reckoning is done with small exponents, which represent the quantities sought. The accumulation of melodic steps in the chord-progressions, the product of multiplied melodic tensions, can be reduced to the harmless addition and subtraction of single tones. But apart from the fact that our tonal materials are numerically limited, reckoning with roots has one disadvantage as compared with that with logarithms: chords, which are the sums of the tones of which they are composed, are not definite quantities, for over the same root a great variety of chord structures is possible. Here an investigation of the two-voice framework and the harmonic fluctuation will clear up all ambiguity.

The ever-obtrusive tritone is not satisfied with affecting the individual chord, or with its influence upon chord-roots: it also has a bearing upon the tonal sums that are juxtaposed in chord-progressions. Progressions like the following and similar ones always retain, despite the smoothest voice-leading, a certain unwieldiness, because the tritone is wedged in between them. That explains why the familiar progression of the tonic and dominant triads is satisfying when the dominant is a major triad, whereas when a minor triad on the dominant is connected with a major tonic the progression is less smooth on account of the tritone between the thirds of the two triads.
In the progressions from a minor tonic to a major dominant and from a minor tonic to a minor dominant (of course we are speaking only of progressions involving chords of group I), there is no tritone.

The strict antithesis of the unwieldy progressions obstructed by the tritone wedge is that in which all the tones move in minor seconds. This chromatic voice-leading produces the smoothest and most flowing progressions; it acts like a magic formula to make every imaginable chord-progression usable. The simultaneous movement of all voices over the same distance, though in different directions, brings the melodic step of the minor second so strongly to the foreground that the ear relegates the harmonic activity indicated by the root-progression to the background. This kind of universal joint cannot be used everywhere, on account of its soft and sliding effect, and it is particularly inappropriate in a style which in general makes very sparing use of chromaticism. Furthermore, its spell is weakened the moment the chromatic movement is not shared by all the voices. Yet even when only some of the voices move by half-tone steps, the chromatic influence is so strong that progressions which would otherwise be difficult to handle, on account of the position and context of the chords, may be made smooth by this means. This explains why in Figure 81 Examples b and d are smoother than the others: each contains two half-steps. In these progressions, the conspicuousness of the tritone is diminished by the chromatic voice-leading. Thus we experience once again in the realm of the simplest chord-relations what we observed in Figure 78, where the lack of root-progression was compensated for by the clearly defined harmonic fluctuation: the various forces at work in harmony may be so played off against one another that the sharpness of one element is made up for by the smoothness of another, and the weaknesses of one by the extra strength of another.

In the well-rounded progressions among chords of group I, lacking in tension as they are, such compensations for one force by another will take place only to a limited extent. But they become extremely significant when we introduce the sharper sounds of group III. The strong tendencies of the latter, arising from the fact of their containing numerous seconds or sevenths, require more careful treatment. Since it is not always appropriate to let these chords work themselves out in undiminished sharpness of sound, they can be adapted to their environment by means of smooth voice-leading, by gradualness of harmonic fluctuation, and by a smooth two-voice framework.

In reckoning roots, it makes no difference which octave they occur in. The differences in their position are of course of decisive importance to the harmonic fluctuation, but for the reckoning of roots a rough procedure suffices: we transpose all the roots, so far as possible, into the same octave, so that the intervals between them are always small.

With an understanding of root-calculation, harmonic fluctuation, and the two-voice framework, all chord-progressions using the materials of groups I and III can be easily handled. Formations which have always been very refractory, and the successful use of which has always been possible only by a constant process of trial and error, or by simple arbitrary decision, may now be handled with complete knowledge: they offer no more resistance to treatment than their more tractable comrades of group I.

A progression of which one member belongs to group I or III and the other to group V offers certain difficulties, because of the fact that the chord belonging to group V has no root. Since any one of its three tones may act as root representative, we may choose which one we wish to connect with the root of the other chord. In general, that one will be chosen which is the best connected to the roots of the chords preceding and following it. This procedure seems to smack of arbitrariness, but when we come to the analysis of more extended progressions we shall see that this is an illusion. The impression of arbitrary procedure will be heightened when we treat progressions involving two or more chords of group V. For in a progression of one of these chords to another, one has one's choice among six possible root representatives, and thus one can arrange
the root-progression as one pleases. But in a wider view the number of possibilities becomes much smaller, so that the one best suited to our scale of values and to the goal of the progressions is easily to be found. The advantage of these chords—their ambiguity—is fully preserved in this treatment, for they contain in their very texture an indefinite, opalescent quality; yet they can no longer escape being drawn into an orderly sequence. We shall handle them with care, and define them at least sufficiently to make them fit the mould which their context of definite chords leaves open to them.

5

Progressions Involving Tritone Chords

The addition of chords from Group B raises the number of possibilities of progression enormously. When the independent chords of Group A are connected with chords of Group B, the tritone, which seeks resolution, and which gives the chords of Group B their character, sets up fields of force to which the chords of Group A offer more or less resistance according to their individual natures. Whenever a tritone chord is followed by a chord of Group A, the tritone is thereby resolved, and the pure sounds of Group I, lending themselves willingly to this attraction, produce a feeling of complete relaxation after tension. Chords of Group III following a tritone chord also resolve the tritone, it is true, but because of their own considerable tension (though they are free of tritones) the resolution they offer is not complete. Similarly, the progression of a tritone chord to a chord of Group V may be only partially satisfactory, because where tension leaves, uncertainty enters. Progressions in the opposite direction—from a chord of Group A to a tritone chord—whip up the sound from rest to tension, and the more complicated the second chord, the greater the feeling of tension.

To gain a clear picture of the nature and value of all these progressions, let us compare the roots of the two chords in each case, as we have done in the progressions of Group A chords already discussed, and thus obtain a reduced and easily grasped image of the harmonic change. The resolution of the tritone, which we must also examine if we are to investigate the progression thoroughly, makes it necessary for us to add to our calculation. For this purpose we shall employ the guide-tone previously mentioned. In all progressions of a chord of Group B to a chord of Group A, the guide-tone of the B chord must move by a good interval to the root of the A chord if the resolution is to be satisfactory. The simplest resolutions occur when this takes place by the step of a second, or when the guide-tone remains stationary, being identical with the root of the A chord. In the second case, the difference in tension between the two chords can be but slight, since the holding over of an important factor cannot be more impressive than its motion by the step of a second. The reckoning of the guide-tone does not stamp any progressions as unusable, any more than did our other means of investigation based on the differing values of the intervals. Progressions of tritone chords in which the guide-tone proceeds by a good interval (the definitions of "good" and "bad" being derived from Series 2) to the root of the chord of resolution have, then, an advantage over those in which it proceeds by a less good interval. And this fact will enable the composer, in handling these often clumsy chords, to place exactly the right chord at the right place for his purposes.

The following examples show the application of the guide-tone principle:
Figure 83 shows progressions of chords of group II to chords of group I, the enharmonic identification of various guide-tones and roots in Examples d, f, and g, should, after what has been said, meet with objection only from those who are fanatics for correct writing. All these simple progressions may be produced without calculation of the guide-tone, simply with the help of the root-progressions. In the following examples (progressions of chords of group II to chords of group III) we could not make any accurate judgement of the value of the progressions without a conscious understanding of the treatment of the guide-tone.

In c and d of Figure 84, the roots progress by tritones. Now, when one tries these progressions out one will observe that c sounds quite satisfying, while d is less convincing. This is because the voice-leading in c is chromatic throughout, the resultant smoothness being emphasized by the holding through of the tone b, while the whole-tone step and the skip in d lay bare the tritone in the root-progression.

In Figure 85 tritone chords of group II are connected with the indeterminate chords of group V. The assumption of different root representatives makes possible in each case three different interpretations of the guide-tone progression.

More complicated progressions, in which the first chord is one of group IV, are shown in Figures 86–88 (IV–I in 86, IV–III in 87, IV–V in 88). The progressions using the indeterminate chords of group V permit, as always, a choice of root representatives. In 88a, the root-progression f–e avoids the tritone skip f–c, although the tritone is still present in the progression of the guide-tone (a–e). The root-progression f–g yields a good progression of the guide-tone, too, and is accordingly the best. It is almost impossible to judge the connection of the very sharp chords of group IV with those of group V—the augmented triad and the chord in fourths—without reference to any other chords preceding or following. The value of such progressions can be judged only from the wider harmonic context.

When several chords of Group B follow one another without interruption, the tritone remains unresolved. Instead of a resolution, each chord presents a new tritone, which keeps the harmony in approximately equal, though perhaps differently focused, tension. The succession of tension and relaxation which is indispensable to musical structure may be produced in such progressions by the harmonic fluctuation or by family relations among the chords. Not until the entrance of a chord of Group A is the tritone resolved as above described. Successions of chords within Group B are treated, so far as the roots are concerned, like the chord-progressions already discussed. The guide-tone of the tritone in the first chord moves to the guide-tone of the second. The interval traversed in this suc-
cession is again the measure of the value of the progression (in terms of the known interval-values), although only secondarily so, since in such progressions the root-succession is of primary importance.

Although the interval of the root-succession and the interval of the guide-tone succession should have values appropriate to the expressive value of the chord-progression itself, the two successions are dependent on each other only in relation to the two-voice harmonic interval based upon each separate root. The two lines of the root-progression and the guide-tone progression need not combine to make correct two-part writing. If each of the lines is logical in itself, and if at each point in their joint progression they form a clear and intelligible harmonic interval, it makes no difference whether they obey the rules of two-part writing or form the crudest infractions of those rules. Not until the resolution into a chord of Group A must the balance be restored by the progression of both root and guide-tone to the root of the chord of resolution.

The chords of group II and many of those of group IV have one particular characteristic. In a succession of two such tritone chords of which the roots in turn are separated by the distance of a tritone, there is a tritone also between the guide-tones of the two chords, and the tritone included in the first chord is also contained in the second:

This chain of tritones links these two chords so closely together that they seem almost like fractional parts of the same chord; they thus perform good service when a close but highly tensed progression is needed, but they are quite out of place when a strong root-progression is desired.

Progressions within groups II or IV, or those from II to IV are thus easy to appraise:

If the progression is from a chord of group II or group IV to one of group VI, the root of the first chord moves to the most convenient tone of the indeterminate VI chord, as it does in the progressions from chords of Group A to those of group VI, already discussed.

The guide-tone of the first chord, too, goes to any convenient tone of the indeterminate chord, whether it is the same one to which the root proceeds or not. Here, too, it is only in a progression of two chords torn from its context that the choice is completely free. If the chord of group VI is between two other chords, the latter do not leave many possibilities open—whether because the guide-tones of the preceding and following chords require a particular tone between them, or because the following chord is one of Group A, of which the root is a common goal for both the guide-tone and the root of the preceding chord, and must be reached in the smoothest possible way from the last definite guide-tone over the assumed guide-tone as a bridge. In progressions within group VI, the calculation of the root representatives suffices.
Family Relationship

The Construction of Tonal Spheres

One last force that operates in chord-progressions remains to be investigated: harmonic family-relationship. Here, too, we may make use of the abbreviated reckoning that served us so well in considering movement in chord-connection: we shall extract the roots of the chords, and work with them instead of with the complete chords.

When one hears the three tones c-e-g sung or played in succession, each tone being of equal duration, the ear perceives them as a broken c-major triad. It always takes c as the root and the other two tones as satellites of c. Even when the three tones appear in different order, c is always taken as the most important, and we know why this is true. According to the interval-values of Series 2, the fifth c-g outlined by the three tones is stronger than either of the thirds c-e or e-g, and since c is the root of the fifth it dominates the entire group and becomes the center of a tonal sphere consisting of these three tones: it is their tonic. If three successive root-tones form a broken chord of groups I or II, the root of this chord is the tonic of the succession:

![Diagram of tonic c]

To be sure, this relation can be so affected by rhythmic considerations that some tone other than the one determined purely by the interval-values may, by emphasis of metric position or duration, become the tonic. This is true even in melodic successions of individual tones which bear no chord-structures, and which because of their primarily linear significance offer a certain resistance to the influence of time-values. Of course, in so strongly chordal a succession as c-e-g, even the sharpest melodic emphasis, the greatest stress, and the longest duration of the e or the g will not deprive the c of its primary importance. But in melodic successions of less strongly harmonic design, such as c-f-e for example, duration and position in the measure are of decisive importance in determining the tonic: the stressed portion of the measure, the longest note, or the final note is needed to tell us which is the principal tone of the group. When chords are built on these tones as roots, the weight of the tonal masses makes the interval-relationships of the roots even less free; they are affected even more easily by stress and duration than in the case of successions of single tones, and their independence is accordingly still smaller. Another factor of importance in the determination of the tonic is the value of the various chords erected on the roots in question. A chord of group I will always try to act as a tonal center for chords of lower value, and thus may at times come into mild conflict with the harmonic values of the root-succession intervals. The skilful exploitation of all these forces produces even within the narrowest limits a richness of tonal possibilities.

A succession of roots forming a broken chord of groups III or IV is particularly susceptible to the influences of rhythm and of the harmonic fluctuation, since it does not have the stability of triad formations. If its tones are all of equal duration, and without special stress, the root of the best interval is again the tonic. The same is true of groupings which, because of their strongly melodic character, can hardly be perceived as forming chords. Root-successions which form a chord of groups V or VI are almost always so affected by rhythmic considerations and by the harmonic fluctuation that their uncertainty is dispelled.

Since according to our chord-table any group of tones may be considered as a chord, whereas in the succession of roots obviously not every possible chord of groups III or IV is taken by the ear as a broken chord, no precise line can be drawn between root-successions which count as chords and those which do not. In general, the feeling that successive roots form a broken chord does not
go far beyond the triad. Slight additions like neighboring tones and passing tones are counted as auxiliary to triad-formations, while the more complicated root-successions are split up into sections which, owing to the thirds and fifths they contain, show the triad-like formations which are lacking in the group taken as a whole.

A succession of chords of Group A must consist of at least three chords if it is to represent a tonal entity. A succession of only two roots does not clearly reveal any tonal coherence, for the interval formed by two adjacent roots has its own root, which to a superficial glance might seem to be the center of the group. But the mass of tones contained in the chords require a more definite determination; they are not satisfied with the confirmation of the central tone by only one other tone. That is why the juxtaposition of two other tones, supporting the central tone on both sides, is necessary to place that tone definitely.

A prominent position among the chords of a group is always held by their goal, the final chord (see the next section, p. 138, on the cadence). This chord, representing the end of a harmonic path, claims such a large share of the hearer's attention that it may always be regarded as one of the most important chords of the group, even when its structure and the position of its root in the tonal sphere are not of the highest value. If it belongs to the same group as the preceding chords, its position at the end of the group makes it play the leading rôle. If it belongs to a group of lower rank, and accordingly does not quite succeed in achieving that rôle, it nevertheless has such importance that a tonality otherwise stable enough may be undermined by it. As far as the root-successions are concerned, this means that the normal interval-values are modified somewhat in favor of the last tone of each such succession. Here again, inverted intervals, weaker than uninverted, offer less resistance.

![Tonal Center: d]

In root-successions like the foregoing, the preponderant significance of the final tone robs the earlier tones of so much value that in the first two examples of Figure 94 the f, which should really have the principal rôle, as root of a fourth, yields to the d. Similarly the a of the last two examples yields to the c: the root of the interval which is in itself higher in value (fourth, minor sixth) cannot hold its own against the power of the final tone.

The situation is different where chords of Group B are concerned. Several such chords are not needed to produce a feeling of tonality; a single one is enough. The tritone contained in them forces the ear to assume a chord of resolution. Although the ear does this willingly enough, it does not know in which direction to resolve the tritone. Thus the sounding of a single tritone chord is enough to create a feeling of tonality, but the tonal center is not defined. Only when the tritone is resolved can one know which chord-root is the tonal center:

![Tonal Center: c]

When a chord of Group B is followed by a chord of Group A, the root of the latter is the tonal center. It follows that in a series of successive tritone chords the tonality cannot be determined until the chord of resolution. When there is no chord of resolution the tonal center may be deduced from the roots just as it would be in a series of chords of Group A:

![Tonal Center: c]

The uninterrupted tritone tension dulls the hearer's senses to the point where they cease to notice it, and fail to feel the need of resolution, as long as resolution is completely avoided. In such a case the best interval between the roots of the chords serves to determine the tonal center, which is the root of this interval unless the final tone lays claim to that position.

If we are dealing exclusively with chords from group II, the tonal
center is not very stable, for the dominant effect of the tritone does not permit the tone which would result from our reckoning to be completely satisfying as the tonal center.

In such cases this tone too is of dominant effect, and thus we may say that in an unresolved series of chords of group II the tonal center is to be regarded as the dominant of a tonic lying below it. This implied tonic is a fifth below the dominant because the unresolved tritone of the final chord would resolve most naturally into an interval whose root would be a fifth below the root of the tritone chord.

Successions of chords belonging to group IV do not need this special consideration. If a series of them occurs without a chord of resolution, the assumption of a tonic lying below their roots is unnecessary. Chords of groups V and VI are treated, once their root has been determined, just like chords of Groups A or B with definite roots; in a long, uninterrupted succession of these chords (which in practice will hardly occur) the tonic could not be determined, and the tonal relationship of the succession would remain indefinite.
The type of tonal connection which has been described is so concentrated, owing both to its almost purely harmonic content and to its brevity, that it appears in actual music only under certain conditions. One usually feels that a design is well planned and well executed only when a brief and concentrated root-succession of this sort has rich melodic decoration, or when other harmonic ingredients space out and smooth over the abruptness of such unerring and unhindered movement straight to a goal. But there is one place where the strongest and most concentrated chord-successions of this kind perform an admirable service: in the cadence. Cadences are chord-progressions of which the effect is strongly final, and which in many styles are actual formulae of conclusion, composed, like all chord-successions, of rhythmic, melodic, and harmonic elements, but in which the tendency to bring a development to a provisional or complete ending is all-powerful. In them, the rhythm confines itself to a few clear and unmistakable time-divisions, the melodic steps proceed directly to their goals, the two-voice framework employs the simplest intervals, and the harmonic fluctuation exhibits the most unambiguous progression from less satisfactory to more satisfactory chords, from tension to relaxation. Their root-successions cannot produce anything different from what is contained in any other chord-progressions, but the predominatingly structural purpose of the cadence results in an intensification of the root-relations. Thus the increased value of the final chord of a succession, mentioned in the previous section, is even more important in the cadence than in other chord-successions, for every factor that contributes to the final effect of the cadence is grist to its mill. Even in root-successions which would ordinarily be indeterminate (such as a broken tritone) or in which more than one tonal center would have to be assumed (as in broken chords of groups V or VI), the final tone in the cadence is so strong that it becomes the tonal center. The extent to which every element in the cadence subordinates itself to the structural drive towards finality is shown by the fact that in the chords making up a cadence even the highest laws of clean writing are often disobeyed, and consecutive parallels, both open and covered, ugly melodic leaps, chromatic slides, and other devices which would ordinarily be used only with the greatest reserve and only for particular expressive effects, are employed without hesitation.

A cadence, like any other succession which is to determine a tonal center, requires three chords of Group A, or only two chords if the first is of Group B and the second of Group A. It is the participation of the individual forces, measured by methods now familiar, that determines the value of a cadence. Just as elsewhere, the root-succession presents a reduced picture of the harmonic progression. The strongest cadences are those in which the intervals of the root-succession are either exclusively fourths and fifths, or consist of a fourth or a fifth plus a step of a second:

The root-succession in which the tonal center is preceded by its fourth and its fifth forms the ideal cadence. What makes it ideal is not only the succession of closely related tones. For the chords built on the fourth and the fifth embody (at least when they are simple triads, the one on the fifth being major) a tritone divided between them, which is resolved in the final chord. To the strong relationship of the first and second roots to the third, which is strongly counterbalanced by their melodic relation to each other, there is added a sort of harmonic short-circuit between the first two chords in the shape of the oblique tritone between them, which contributes significantly to the tendency to a strong close.

This same tritone relation results from the cadential root-progres-
major second—fifth—tonic, and accordingly this progression is also very strong:

![](image1)

But it is not as strong as the first one, because it substitutes for the hard step of a second between the first two tones the more closely related skip of a fourth.

Cadential formations in which the final root is preceded by its fifth, but the fifth is preceded by some tone other than the fourth or the major second, vary in value according to the position of this new tone. We are here obviously in borderland territory, where the forces of Series 1 and Series 2 now conflict and now coincide. Take for example a chord-succession of which the roots are a-g-e:

In terms of Series 2 we have first a second and then a fifth; the fifth, being the better interval, determines the tonal center, which is c. According to the values of Series 2, the root-succession e-g-c would produce a better chord-progression, for the third e-g is higher in value than the second a-g. In isolated progressions of two chords, this is true, but in a cadence it is not just the relations between each two adjacent chords that count, for the ear relates them to the tonal center of the group, which is easily determined according to the interval-values of this same Series 2. Now, in the question of relations to a central tone it is Series 1 that governs, as has been suggested earlier. Although we shall comprehend the full importance of this principle only in the construction of extended chord-successions, yet the organizing power of Series 1 is clearly to be observed even in these cadential groups of only three chords. In the root-succession a-g-c, the a is closer to the tonal center c (as we know from Series 1) than the e in the succession e-g-c; accordingly, the cadential progression built on the root-succession a-g-c is the stronger. There follow in order the progressions built on e-g-c, eb-g-c, and ab-g-c. The progression d-g-c illustrates the coinciding of the pure interval-values and the relationship-values:

![](image2)

The d is not very closely related to the c and seems almost, by its melodic tendency, to act as a neighboring tone of c. At the same time, the high interval-value of the skip d-g gives the d so much force that it is hard to tell whether it is the interval-values of Series 2 or the relationships of Series 1 that are more active in this case. The root-successions bb-g-c, b-g-c, and db-g-c, show a strong melodic cast in the seconds bb-c, b-e, and db-c, interrupted by the strong fifth g-c; the harmonic power of cadences built upon these successions is accordingly much lower. In the root-succession f♯-g-c the tritone f♯-c does not fully count, since the f♯ is taken merely as the neighboring tone of the g.

If the tonal center of a cadential group of chords is reached by skip of a fourth downwards,

![](image3)

the value of the cadence is diminished, in accordance with both the interval-values of Series 2 and the relationships of Series 1. The great firmness of the cadences in which the final interval is a fifth is here changed into something smoother, but also something strange and inaccessible. And here, too, the quality of the cadence diminishes with the decreasing relation of the tone before the last interval to the tonal center.

A skip of a third between the tonal center and the root preceding it
makes the cadence soft and amiable; while a major second at the same place

\[ \text{\textbf{Figure 1}} \]

shows, in accordance with its melodic character, the familiar harmonic sharpness, which cannot be made up for, even by placing a better interval before it. The use of the minor second (upwards or downwards) just before the tonal center

\[ \text{\textbf{Figure 2}} \]

results, owing to its leading-tone tendency, in the mildest of all cadences. The tritone produces the poorest cadence, and can be used only with considerable help from other factors—rhythmic, melodic, and even dynamic and expressive.

The briefer cadences, consisting only of a chord of Group B followed by its resolution in a chord of Group A, may be appraised according to the same precepts. When there are only two roots, it is hard to recognize the fact that they represent not only an interval-value of Series 2 but also a relationship of Series 1; but in a larger harmonic context, without which a cadence-formation would have no purpose, these cadences take their place without hesitation.

8

Larger Harmonic Relations

Degree-Progression

Root-calculation permits us to form a judgement about the succession of two chords, and enables us to recognize without difficulty the tonal relations which underlie cadences. Roots are our guide, too, through larger harmonic sections, in which they are the supports of a wide tonal structure of which the thrusts and tensions act in accordance with the family-relationships of Series 1. This series of tonal values is here the undisputed master. The roots which support the burdens of larger harmonic groupings may be called degrees, and their succession in accordance with the demands of Series 1 the degree-progression.

According to a view widely held, larger harmonic developments are simply extended cadences. This is inaccurate insofar as it ignores the fact that, as we have seen, the structural tendency towards an ending in a cadence subordinates all other factors to it, while in other harmonic developments what is sought is the free unfolding of rhythm, melody, and harmony. But one thing such free developments do have in common with cadences: the roots of their chords must exhibit tonal coherence if the chord-successions which take place above them are to be understandable.

In a succession of only three roots, it was not difficult to determine the tonal center with the help of the interval-values. But when the degree-progression consists of more than three tones, the expanding force of the tonal relationships robs the interval-values of some of their significance. In such cases, the tone which attracts attention by recurring most often is usually to be taken as the tonal center; only in very short degree-progressions, in which no tone is repeated, do the interval-values still reign. But it is best to confirm the determination of the tonal center by subsequent repetition in any case; otherwise the ear may, in its quest for the tonal center, seize upon some tone other than that which is intended by the composer.

We can, however, spare the ear both the quest and the mistake. Besides the repetition of a root, it is the surrounding tones that determine the tonal center, according to their relationship to it. The closest relationships are its best supports. If the tonal center is to possess particular stability, one had better see to it that there is a nice balance of intervals in the degree-progression centering around it. If only the closest relatives are called upon, then it is best to use the fourth as a counterpoise to the fifth. For the further development of the degree-progression it is advantageous to use a balanced variety of tones of close and distant relationship, con-
taining among them as many good intervals—fifths and fourths—as possible. Samples of such arrangements, which may undergo the most varied changes, are contained in the following examples:

The degree-progression gives us a means of combating the effects of harmonic fluctuation in chord-successions. If the chords have very varied harmonic weight, being members of very unequal groups, the degree-progression may be very smooth, consisting largely of third-relationships and leading tones. If, on the other hand, the chords all belong to the same or closely related groups, and so vary little or not at all in tension, then the degree-progression must introduce variety, arranging contrasts between light and heavy, strong and weak, among the graded family-relationships of its tones.

The guide-tones of the tritone chords have no effect on the degree-progression. They are not continuously present, and disappear altogether when several chords of Group A follow one another; they appear only from time to time when occasional tritone chords are interpolated, and compose a continuous series only when a number of chords of Group B follow one another uninterruptedly.

The succession of guide-tones which results in this latter case is quite independent of the degree-progression of the roots, as we saw when we considered the connection of chords of Group B. But between the extreme points of such a succession (which are always at places where a chord of Group A causes the line of the roots to coincide with that of the guide-tones) the melodic development must be, like the degree-progression, logically developed and based on the relationship-values of Series 1. Unlike the degree-progression, however, the guide-tone line does not need to rest on a single tonal center, and in particular not upon that of the degree-progression.

An ill-designed degree-progression can prevent the free unfolding of the chords above it. Therefore in constructing the degree-progression anything that would obstruct the free unfolding of the harmony is to be avoided. Here, as everywhere in the realm of artistic work, no unerring rule and no prohibition valid without exceptions can be given for the construction of good designs. What is good in one place may be of lamentable effect in another. Nevertheless, for the degree-progression which is not too strongly influenced by the expressive requirements of the composition, or too clearly articulated into sections by cadence-formations, sequences, or other groupings, a few principles may be formulated. The observance of these principles, when the two-voice framework and the harmonic fluctuation are skilfully handled, will insure a smooth series of chord-progressions.

In a normal degree-progression the following factors are detrimental to the effect:

1. The absence over a long period of the strong-relationship intervals of the fourth and fifth:

This brings the danger that the less closely related intervals may subject themselves to the organizing force of Series 2 and thus determine a new tonal center, different from that of the degree-progression.

2. The melodic interval of the tritone. It can be used with good effect only where one of its tones becomes the upper or lower neighbor of a better interval, or when the expression of a composition calls for closely connected but not strong harmonic progressions.
If for one reason or another it is desired to maintain the effect of the tritone intact in the degree-progression, but without its being too prominent, the insertion of a rhythmically unimportant neighboring tone (of course bearing a chord upon it) to either the upper or the lower tone of the tritone will make the progression somewhat more flowing. The disturbing awkwardness that characterizes most progressions based on a tritone in the degree-progression can be overcome, as we have seen, by chromatic voice-leading in some or all of the parts.


Even the thirds of triads bind the chords built upon these roots very closely together. If the degree-progression traverses the tones of an augmented triad, the uncertainty of that chord is transferred to the progression. Degree-progressions in the shape of a tritone chord almost always produce, because of the strong power of association of the tritone, unsatisfactory chord-progressions. Broken-chord formations of whatever nature, even those consisting of as many as four different tones, must be handled with especial care if they are to produce a satisfactory effect.

4. Chromatic progressions—that is, several minor seconds in uninterrupted succession, or so little separated that the feeling of chromaticism persists:

5. Explicitly melodic treatment—that is, serious impairment of the clarity and intelligibility of the succession by the presence of subordinate tones: passing tones, anticipations, etc.;
that the tempo is not so slow as to give each of the intervals or chords its own harmonic value.

9

Modulation

We see in the tonal arrangement of the degree-progression how—despite the greatest strictness in the choice of material and in the construction of the harmony out of the interplay of elemental rhythmic, melodic, and harmonic forces—the boundaries of tonality have been extended. We have stepped from a small realm dominated by three triads and fenced in by modal scales to a broad land full of chords of all designs and governed by tonal relations. We must think back, disregarding historical considerations, to what was needed to accommodate a Db major triad in the key of C major, in order to realize what a narrow world we have left behind us: the minor triad had to be transformed in the imagination to a major one, and two tones had to be accommodated which did not occur in the triad proper to the key:

\[
\begin{align*}
\text{Db major triad} & \quad = \quad \text{major triad} \\
\end{align*}
\]

The form in which the chord really appeared flatly contradicted the analytical procedure that had to be applied to it. Is it not clearer and simpler to regard such a chord (the Neapolitan triad) as a chord of sub-group I with the relationship-value derived from its progenitor tone and measured according to Series 1? Let us remember, too, how arbitrarily all chords not built up in thirds had to be explained. Now we can determine their place in harmonic procedure just as easily and definitely as that of the triads. But although we can now embrace all conceivable chords within a tonality, and arrange them according to Series I, we must burst the bonds of a single tonality. Every tone seeks an importance greater than that which it has simply as a tone, or as a descendant of a progenitor tone, or as a part of a chord; it seeks to become the fundamental of an overtone series, the progenitor of a new Series I of its own, the tonal center of a degree-progression. When we yield to this tendency, when we allow one tone to usurp the place of another as tonal center of a degree-progression, we are modulating.

Modulation as an end in itself, isolated from the logical development of all the elements of musical writing, is an absurdity, no more possible than a chord-progression free of all but harmonic influences, or a melody in which melodic force alone operates. Yet in order to understand the nature of modulation we must separate it from its context and study it alone, just as we did with harmonic fluctuation, or the two-voice framework. Root-calculation, which has shortened our labors in other fields, does so here, too. We can determine the presence of modulation from the construction of the degree-progression alone; consideration of the progressions from root to root will show us the nature and the value of a modulation.

The prerequisite of a modulation is a firmly established tonal center as a point of departure. A tonality which is not definitely settled will not do, for it does not offer enough resistance to the subsequent tonal center, and accordingly becomes subservient to it. A tonal sphere is set up in the manner familiar to us, by the grouping of chord-tones around a tonal center. The new tonal sphere will be set up in the same way, through the grouping of roots around a new center. Since one tonality can include every kind of chord, it is not always easy to find the exact location of the boundary separating the two tonal domains. But we owe to the phenomenon of tonal relations the fact that we are able at all to feel our way among the degree-progression tones with their chords, belonging to the most varied tonal centers, and determine to which one each belongs. Within a single degree-progression, we always hear as the center of a tonal sphere that tone which occurs repeatedly within a limited space of time, or that one which outranks the others by virtue of its position at the end of a cadence, or finally that one which is supported by the presence of the tones most closely related to it (the fifth and the fourth). Yet the continual movement of a degree-progression in fifths and fourths does not necessarily produce a continual changing of tonality. Since the root-successions of a degree-progression are to be brought as close together as pos-
possible by means of octave transpositions, many of the tones to which the degree-progression moves by fifths can be brought into close proximity with the tonal center, where—as the third or the second of the latter, say—they are outshone by its fourths and fifths. It is true, as we have previously stated, that the clear significance of a degree-progression can be disturbed by an abundance of chords above it belonging to groups III and IV. The degree-progression and the fluctuation may actually conflict. In such cases the triads are what help us to an understanding of the harmonic development. Just as the ear in hearing intervals seeks for the natural ratios, and tries to hear the clouded intervals as pure ones, so among chords the triad is the ear’s natural unit of measure, which it tries to recognize wherever it can, and which it uses to help it in forming a judgement of other chords. In the ebb and flow of the most awkward chord-successions, triads will always stick out as points of rest, and will help, along with the tonal centers established by the degree-progression, to support the tonality—except where the composer wishes to leave the listener in doubt about the tonality for a brief period, and therefore uses a fair number of obscure chords.

The gradation of chord-weights enables us to set up chord-progressions in which two tonalities are at one point juxtaposed in the sharpest contrast and without connection. In the degree-progression this is not possible, because even those tones which have the most distant relationship to a tonal center are yet not completely unrelated to it. If these tones are skilfully worked into the degree-progression, the tonality will be supported by the tones standing in the best relationship to its tonal center, and we shall not need to assume constant changes of tonality in order to explain the presence of groupings only distantly related. Within the domain of new tonal centers the relationships to the old one are of course no longer valid, for the original Series 1 has been replaced by new ones, belonging to new tonal centers.

Between the parts of a degree-progression which are closely tied by skips of fourths and fifths to their respective centers, there are always passages that may belong to either sphere, passages where the tonalities overlap:

or there are transitional tonalities which link the others. In such cases, the ear has time to loosen its hold on the old tonal center, and to accustom itself to the new one before yielding completely to it. The clearer the way leading from one tonal center to the next, the more satisfactory the modulation. In such arrangements, the transitional sections of the degree-progression are so arranged that their function is obvious. They are subordinate and complementary to the tonal groupings which stand out as the bearers of tonality.

Often it is impossible to draw clear boundaries for either the principal or the subordinate tonal groupings; one listener hears the change as occurring at one place, another at another. But this is not a shortcoming; on the contrary, one of the greatest charms of modulation lies in the exploitation of this very uncertainty in the transitional passages.

The tonal centers of all the tonalities of a composition produce, when they are connected without the inclusion of any of the intervening tones, a second degree-progression, which should be constructed along the same lines as the first one, built of the roots of all the chords. Here we see the full unfolding of the organizing power of Series 1. The entire harmonic construction of a piece may be perceived in this way: against one tonal center chosen from among many roots others are juxtaposed which either support it or compete with it. Here, too, the tonal center that reappears most often, or that is particularly strongly supported by its fourth and its fifth, is the most important. As a tonal center of a higher order, it dominates a whole movement or a whole work. Exact statement of the principles of tonal organization is outside the bounds of theoretical discussion, and belongs rather to the teaching of composition itself. We shall therefore leave the subject after these few suggestions.
Does not the discussion of tonality contained in the preceding section contradict what was promised in the Introductory section of Chapter I? What good is a new theory of composition if it leads straight back to the old, "worn-out" concept of tonality? We have seen that tonal relations are founded in Nature, in the characteristics of sounding materials and of the ear, as well as in the pure relations of abstract numerical groups. We cannot escape the relationship of tones. Whenever two tones sound, either simultaneously or successively, they create a certain interval-value; whenever chords or intervals are connected, they enter into a more or less close relationship. And whenever the relationships of tones are played off one against another, tonal coherence appears. It is thus quite impossible to devise groups of tones without tonal coherence. Tonality is a natural force, like gravity. Indeed, when we consider that the root of a chord, because of its most favorable vibration-ratio to the other tones, and the lowest tone of a chord, because of the actually greater dimension and weight of its wave, have greater importance than the other tones, we recognize at once that it is gravitation itself that draws the tones towards their roots and towards the bass line, and that relates a multiplicity of chords to the strongest among them. If we omit from consideration the widely held notion that everything in which the ear and the understanding are not at once completely at home is atonal (a poor excuse for a lack of musical training and for following the path of least resistance), we may assert that there are but two kinds of music: good music, in which the tonal relations are handled intelligently and skillfully, and bad music, which disregards them and consequently mixes them in aimless fashion. There are many varieties between these two extremes, and of course it does not follow that all music in which the tonal relations are beautifully worked out is good music. But in all good music account is taken of them, and no music which disregards them can be satisfying, any more than could a building in which the most elementary laws of the vertical and horizontal disposition of masses were disregarded. For the creation of tonality it is all the same, being a matter of style and period, or of the manner in which a composer works, what kind of chord material is employed. A piece that consists primarily of very harsh and grating chords need not be atonal; and, on the other hand, limitation to the purest triads is no guarantee of clean tonal relationships. The only music which can really be called atonal, therefore, is the work of a composer who is motivated perhaps by a consciousness of the inadequacy of old styles to the musical needs of our day, perhaps by a search for an idiom that will express his own feelings, perhaps by sheer perversity, to invent tonal combinations which do not obey the laws of the medium and cannot be tested by the simplest means of reckoning. Such a man is not impelled by the instinct of the musician, who even in what seems his blindest groping never loses the true path entirely from view. But even among the music which can be completely analyzed there are two types which, although they cannot be called atonal, yet by the accumulation of harmonic means of expression place too great a burden on the listening ear for it to be able to follow them completely. One of these types, although it starts from diatonic premises, works with the material of the chromatic scale, and packs in so closely a multitude of dominant relations, alterations, and enharmonic changes, that the key is bursting with harmonic groups of short duration. The ear may succumb to an excess of harmonic procedures each reasonable in itself. The other type, by a continuous use of chords of groups III and IV, produces an opaque kind of harmony which in its avoidance of any chord resembling a triad seems to fly in the face of Nature. Neither of these types can be made reasonable by the logic of its degree-progression; both are too crowded with material to be enjoyed. The development of music has left far behind the style of accumulated dominant relationships within short spaces of time, in favor of more important things. This style was developed by the German post-Wagnerian school. About 1900 it dominated the entire technique of composition, and it was still throwing up sizable waves as recently as the second
The other style, which as a reaction to the outmoded diatonic style and the exaggerated technique of over-subtle harmonic relations and enharmonic changes, made great use of the sharpest chords, is still widely cultivated. We may assume that it will give way to a quieter and more enlightened style as soon as the quite praiseworthy joy of discovery on the part of composers and their preoccupation with technical speculation become less important, and the accumulated knowledge of the expanded tonal materials and their laws prepares the way for a fuller and higher craft of composition.

There are today a considerable number of composers who issue works that they call atonal. To what extent the atonality of these compositions rests upon the lack of a convincing degree-progression and to what extent it is a more or less developed tonality concealed by an uninterrupted succession of sharp sonorities, the reader himself can determine by extracting the degree-progressions of such pieces. Doubtless these composers see in their freedom from tonality a liberty that will lift their art to the infinity of time and space. Apart from the fact that I consider it impossible to abolish the inherent characteristics of the medium, I do not believe that liberty is achieved by substituting mere variety for the principle of natural order. Nowhere does Nature give us any indication that it would be desirable to play off a certain number of tones against one another in a given duration and pitch-range. Arbitrarily conceived rules of that sort can be devised in quantities, and if styles of composition were to be based upon them, I can conceive of far more comprehensive and more interesting ones. To limit oneself to home-made tonal systems of this sort seems to me a more doctrinaire proceeding than to follow the strictest diatonic rules of the most dried-up old academic. Is it not strange that the most fanatical lover of the piano will close his ears in horror at the falseness of the tempered chords of his instrument, once he has compared them a few times with those produced by a harmonium in pure intonation, to realize that with the blessing of equal temperament there entered into the world of music—lest the bliss of musical mortals be complete—a curse as well: the curse of too easy achievement of tone-connections. The tremendous growth of piano music in the last century is attributable to it, and in the "atonal" style I see its final fulfillment—the uncritical idolatry of tempered tuning.

The existence of this style seems to me only to lend final confirmation to the fact, everywhere to be observed, of the disappearance of understanding judgement and critical sense in the field of music. But already a decline is noticeable in the interest manifested in this music based on rules dictated by fashion and contrary to nature.

Anyone to whom a tone is more than a note on paper or a key pressed down, anyone who has ever experienced the intervals in singing, especially with others, as manifestations of bodily tension, of the conquest of space, and of the consumption of energy, anyone who has ever tasted the delights of pure intonation by the continual displacement of the comma in string-quartet playing, must come to the conclusion that there can be no such thing as atonal music, in which the existence of tone-relationships is denied. The decline in the value placed upon tonality is based on the system of equal temperament, a compromise which is presented to us by the keyboard as an aid in mastering the tonal world, and then pretends to be that world itself. One needs only to have seen how the most fanatical lover of the piano will close his ears in horror at the falseness of the tempered chords of his instrument, once he has compared them a few times with those produced by a harmonium in pure intonation, to realize that with the blessing of equal temperament there entered into the world of music—lest the bliss of musical mortals be complete—a curse as well: the curse of too easy achievement of tone-connections. The tremendous growth of piano music in the last century is attributable to it, and in the "atonal" style I see its final fulfillment—the uncritical idolatry of tempered tuning.

The concept of atonality arose at the end of the first World War. At that time there appeared, among much other propaganda material, a periodical which proposed to examine "atonal and antitonal" formations. The difference between the two forms of non-tonal music was never established, because no one could conceive of what was represented by "antitoneality". So atonality was left, but no one ever established exactly what that concept represented either. Today we know that there can be no such thing as atonality, unless we are to apply that term to harmonic disorder. The vagueness of the conception, arising from its negative origin—here even
less fruitful than in other fields of creation—, caused it to grow from a technical term into a popular catchword, used by some to praise to the skies any music they did not understand, and by others to condemn whatever they did not like, whether it consisted of strange harmonies, muted trumpets, *fortissimo* outbursts, or new experiments in structure.

There is another catchword that dates from the post-War period: polytonality. The game of letting two or more tonalities run along side by side and so achieving new harmonic effects is, to be sure, very entertaining for the composer, but the listener cannot follow the separate tonalities, for he relates every simultaneous combination of sounds to a root—and thus we see the futility of the game. Every simultaneous combination of sounds must have one root, and only one; one cannot conceive of additional roots somewhere above, belonging to other tonal spheres. Even the craziest harmonic combinations can result in only one degree-progression. The ear judges the total sound, and does not ask with what intentions it was produced. Skilful planning of the harmonic fluctuation will eliminate all accidental effects such as always come about when tonal successions belonging to different tonal domains are capriciously combined. But since organic work, growing out of natural roots, will always stand on a firmer basis than the arbitrary combination of different elements, polytonality is not a practical principle of composition.

**Practical Application**

A true musician believes only in what he hears. No matter how ingenious a theory is, it means nothing to him until the evidence is placed before him in actual sound. For the reader who has not held back from the assertions previously made in this book, I will now give a practical example of the procedure which results from the combination of all the technical devices described. It will be seen that a task may thus be accomplished which could not be accomplished with other means, unless long training in playing and hearing had made our tonal sense an infallible guide. But experience tells us that in most musicians the sense of the value of complicated chords is not nearly developed enough to provide a source of unerring judgements. Even if in the imaginative process, in the sheer formation of the conceptions of musical phenomena, it performs invaluable services, it is insufficient as soon as one tries to note down the imagined sounds. Just as in the literature that is written in letters, so in that written in notes everything must be clear and completely analyzable to the person who knows how to read it. The true work of art does not need to wrap any veil of mystery about its external features. Indeed the very hallmark of great art is that only above and beyond the complete clarity of its technical procedure do we feel the essential mystery of its creative power. We must therefore be able to illuminate the darkest corners of a composition, and explain its construction completely. There are doubters who will not approve of such a procedure, because they are entangled in older theories, and perhaps also are angry and somewhat sad about what they call the coarseness of feeling with which we strip bare matters which they would rather keep clothed in the semi-darkness of twilight. (In technical matters there can be no question of the temperature of our feelings: the true secrets begin, as we have said, on a much higher level.) But those of them who are not ill-willed in their disapproval must at least admit that new prospects are opened up for the technique of composition. Let anyone who, on the other hand, rejects our procedure out of mere antipathy try to arrive at more convincing conclusions by better means.

The conditions which I have set for myself in the treatment of the following example are far harder than one would ever find in actual music. I have purposely chosen so artificially complicated a case to show that even such problems can be solved. How much easier then must be the solution of the problems of free composition, which can never contain more than a small fraction of the difficulties of the following problem!
Suppose we were to find in a piece of music the foregoing series of chords. Let us grant that it sounds horrible—but can you honestly say that you have never encountered such combinations of tones? Suppose further that the composer of this series of chords admitted that what he had intended was to build a harmonic crescendo, in which the harmonic tension should increase sharply from the first chord to the fifth, followed by a diminuendo to the end. In accordance with our plan of leaving rhythm out of consideration, I have notated this example, too, in whole notes. This robs it, of course, of the slightest trace of attractiveness, and ruthlessly exposes the harmonic progressions in complete nudity. Let us now see whether the composer has succeeded in realizing what he intended.

The analysis of the five-voice example yields the following results:

1. **Linear construction.** Except for the next to the top voice, not one of the lines is built on sound principles of melodic construction. These principles are discussed in the next Chapter, and I shall therefore leave this aspect of the matter for now with the assertion that the lines are poor.

2. **Two-voice framework.** No plan is apparent. Up to the fourth chord there might seem to be one, but the weak fourth g-c3 in the fifth chord flatly contradicts the intention to make this the harmonic climax; here a strong interval (fifth or third) would be needed, rather than an inversion, which (as we know from the combination tones) is lacking in energy. Chord 6, containing a seventh, should have been followed by a chord of lower tension. Instead, chord 7 contains the tritone, and even it is not resolved: it is followed by a seventh, and only this last interval finds a satisfactory resolution in the final fifth ab-eb2.

3. **Harmonic fluctuation.** Obviously the composer had no conception of this. It follows an aimless, zigzag course which in no way results in the desired climax of harmonic tension in chord 5.

4. **Degree-progression.** The concentration of chords from the fourth to the eighth chord does not allow any harmonic life to unfold, while a further brake is provided by the repeated eb of the sixth and seventh chords.

5. **Guide-tones.** Their connection with the roots in the degree-progression is good, but they stand still in their tracks, and are accordingly, in this piece in which everything should contribute to the impression of movement, rather a hindrance than a connecting factor of repose.

6. **Tonality.** The tonal center in the degree-progression is undoubtedly G# (Ab), for that note occurs twice and is confirmed by the strong, repeated fifth. The leading tone, G, too, which occurs twice, strengthens the tonal center, and the third, B, also helps. In this connection the c# of the beginning and the A of the fourth chord are of subsidiary importance. The first four chords could also be related to A as a tonal center, supported by its third, c#, and by its leading tone, G#. In this case there would be a modulation from A to G#. The tonal sphere of G# overlaps that of A, since it begins as early as the third chord; from this point on, the sway of G# is undisputed.
All in all, we can say that the composer has not solved his problem well. Let us help him to a better solution.

1. *Two-voice framework.* As in the original version, let the upper voice move in a broken line while the lower moves down stepwise:

   ![Diagram](https://example.com/diagram1.png)

But now the intervals are well arranged: the harmonically strong fifth is followed by the weak major sixth, then the strong major third, then the strong tension of the major second, resolving to another major third. Now the intended climax of the piece has the necessary support. The framework has its climax in the third chord, of which the fifth is only a lower and therefore weaker repetition. If we succeed in placing the harmonic climax at the fifth chord, by means of heightened tension, then the two-voice framework and the harmonic fluctuation will be at odds—a desirable result, since the opposition of forces enhances the life of the tonal texture. The weakest place in the two-voice framework is in chord 6 (except for the major sixth in chord 2), from which the return is made through the sharp minor seventh $fsharp - e$ to the pure interval of the fifth.

2. *Harmonic fluctuation.* For the aimless arrangement of the fluctuation in the original version we shall substitute a planned distribution of the harmonic tensions. To accomplish this, several ways are open to us. If we wish to create the impression of a departure from rest and a return to rest, which would seem indicated by the design of the melody and the framework, we had better begin and end with chords of group $I_1$:

   ![Diagram](https://example.com/diagram2.png)

We can then place a chord of group $IV_2$ at the planned climax, and for the chords in between there will be several possibilities, of which those here proposed doubtless best serve the purpose. The reader is free to try other solutions. In filling up the chords we have a certain freedom in several places. We choose those solutions that make the best voice-leading for the inner voices. This produces the indicated form for our example.

3. *Degree-progression.* But we have produced a quite unusable degree-progression. The repeated $c$ at the beginning and the broken chord formed by the roots of the fifth to the ninth chords are responsible for the unsatisfactory effect of the whole. We shall therefore make the following improvements:
and try to preserve the chord-scheme that fits the planned fluctuation. But this is not possible throughout, for in the seventh chord the new tone of the degree-progression, d, makes a tritone with the upper voice, and thus will always produce a chord of Group B.

4. Guide-tones. The line of the guide-tones is poor since, with the exception of the first one (the f in the fourth chord), it contains nothing but the broken form of a chord of group Jlb. The improvement of this defect would bring about the collapse of the whole structure that has cost us so much pains already, so we shall postpone it until we have treated the problem from the tonal standpoint.

5. Tonality. The tonal spheres are not clearly worked out. The skip of a fourth between the second and third tones of the degree-progression permits us to group the first tones, as far as the B♭, around c as a center, the c♯ at the beginning being taken as the upper leading tone of the c, unless one is to take it, since it is the first tone, as an independent tonal center. But as such it would lack any support. From the fourth to the eighth tones the center is B♭, the A as leading tone and the d as third being its auxiliaries, while the e♭, the fourth, appears as the neighbor of the harmonically stronger third. The tonal center G♯, which although it stands at the end and is reinforced by its upper leading tone A is not completely definite, would be stronger if we provided it with another supporting tone. This we can do by substituting for the d of the seventh chord, which stands a tritone away from the G♯ anyway, another G♯:

This note is a very strong (almost too strong) support for the tonic, being separated from the final note only by the A, which has now become a weak returning tone, and being itself supported by the dominant d♯ (e♭). This restores to us the possibility of placing a chord of group III in the seventh place, as we had planned. But if we retain the IV chord in the sixth place, the progression of the guide-tones will be poor. We had better therefore use a III chord in this place, too; it will change the intensity of the harmonic fluctuation, to be sure, but not its direction. Indeed, we shall be realizing even better than before the composer’s intention to make the fifth chord the climax. The line of the guide-tones is now just as correct as the degree-progression.

6. Linear construction. The voices which are not parts of the two-voice framework now have better lines than in the original version of the example. Complete purity of all the elements cannot be attained under the extraordinarily severe conditions which we set ourselves; the slight linear shortcomings at the end of the second and third voices are therefore to be regarded as the least of the possible evils.

I know the outcry that will greet such an analysis in some quarters: “Why, this is pure constructivism! What is there left for invention?” But it has always been true in the craft of composition that something which others had mastered and with which one was not yet thoroughly familiar oneself was looked on as invention-killing constructivism. The only reason the rules of harmony and counterpoint are not considered constructivist schemes is because we are used to them. Between these simple technical disciplines and a more comprehensive sort of instruction, where does constructivism begin? For him who has never thought about the theory of composition it begins no doubt with the first chords that he plucks like forbidden fruit from the tree of his insufficient harmonic knowledge; he loves them especially as the children of his sin against the theory of harmony, and consequently does not wish to know them in all their most hidden characteristics. But for the strong musician, who is sure of his creative impulse and of his knowledge, there is no
such thing as constructivism. Every additional device that helps him master his material brings him a step nearer the inmost shrine of music itself.

12

Non-Chord Tones

According to the procedure we have followed up to this point, we must consider every appearance or disappearance of a tone amid chord-structures as creating a new chord. This view is valid so long as the tempo is so slow that the alteration of the sound seems important enough to cause a separate chord to be perceived. But there are many such tones which do not produce independent chords—chord splinters, or offshoots, they might be called. Such tones enrich chords without essentially changing them. Melody, as we have earlier determined, is what sets tonal masses into motion. But melodic force works not only by a general attack on the inert chord-masses. It also splits off separate tones from the chords, in such a way that the ear perceives the new sound in the first instant as something exceptional and different from the normal run of chords, and relates it to the harmonic progression only when the next chord enters. The rigid chordal structure thus has to give up portions of itself bit by bit to melody, the action of which in these skirmishes is comparable to that of an acid upon a metal. A tiny bit of a mighty force gnaws and bites at the material under attack, not strongly enough to destroy it, and yet affecting the surface enough, by etching scratches and grooves into it, to roughen its smooth finish.

These little bits of melody strewn in among the harmonic texture have long been known as “non-harmonic” or “unessential” tones. I prefer the term “non-chord” tones. The following varieties may be distinguished: returning (“changing”, “auxiliary”) tones, passing tones, suspensions, neighboring tones (“appoggiature”, “unprepared suspensions”), neighboring tones left by leap, neighboring tones approached by leap, anticipations, unaccented free tones, and accented free tones.

Returning tones. The returning tone occurs when one member of a chord moves from its place in the chord to another tone for a short time and then returns:

In most cases the new tone is a second above or below the chord-tone, but it may be further away. What is essential, however, is that the foreign tone should be less important rhythmically than the chord-tone—that is, that it should occur in a less stressed position. Usually it is at most equal to the preceding chord-tone in duration; a longer time-value would take away from its auxiliary character. Generally it is a tone really foreign to the chord—that is, the combination that occurs during the moment of its sounding belongs to a group of lower rank than the main chord. There are, however, returning tones that form a combination of higher harmonic value than the main chord, or that do not affect the value one way or the other. It is often doubtful whether such cases involve real returning tones or rather broken-chord formations.

Such returning tones usually occur in connection with chords of relatively low harmonic value, and they must be of short duration if the higher-value combination which they produce is not to usurp the principal place and so invert the intended effect. Returning tones may occur in more than one voice at a time:

and they may move in opposite directions:
There are also whole returning chords, in which the main chord is left for a new one, built on a different root, and then the main chord returns:

Here, too, it is often hard to decide whether the middle chord is only an auxiliary chord or whether there is a really significant change of chord and root. For the returning chord to appear unmistakably as such, it is even more important than for the returning tone that it should have the lesser rhythmic and harmonic value.

**Passing tone.** The passing-tone formation consists in a stepwise transition from one chord-tone to another:

It can consist of one tone or of several, and must, like the auxiliary tone, result in combinations of lower harmonic value than that of the main chord, and be of short duration and in unstressed position. Passing tones can also occur in more than one voice simultaneously, and in contrary motion:

But here there is the danger that the quantity and position of the passing tones will make them more important than the principal tones. Passing tones can also fill out the space between a chord-tone of one chord and a chord-tone of another:

In such cases the formation is not finished within the area of the first chord, since the chord when it moves to the next contains the foreign tone; but the passing-tone character is preserved because the goal of the passing tone follows immediately in a new chord-tone or in the neighbor of such a tone. Auxiliary tones and passing tones also occur in two-part writing:

**Suspension.** A suspension occurs when, in a succession of two intervals or chords, part of the first is held over into the second, where it creates a tension with the other chord-factors, and is accordingly resolved during the existence of the second interval or chord:

In two-part writing every interval can thus become a suspension which is subjected to the attraction of a harmonically stronger interval.

The most natural resolution of the tension generally occurs when the suspended tone moves downward by a major or a minor second. Upward resolution is good when it is by the step of a half-tone, because of the leading-tone effect, while upward resolution by step of a whole tone is less often successful.

The resolution of the suspension by the upward step of a major second is most useful when a leading-tone progression or several
simultaneous half-tone steps in other voices contribute to the smoothness of effect.

In three or more parts the tension created by the suspension is greater, because of the greater definiteness of the surroundings; the effect of the suspension is accordingly enhanced, and the resolution is even more satisfying. We have established the fact that the suspension always resolves to a better chord-factor. But in three or more parts this does not mean that the chord-progression always follows the pattern poor—good. The effect of the resolution of a suspension is always created, even in writing in more than two parts, by the relaxation of the tension of a single interval. Thus in the three-part examples of Figure 131, the suspension—resolution relation is not always accompanied by the change from a sharper to a milder chord. Instead, the five chord-progressions given contain the following interval-successions, each embodying the principle suspension—resolution: minor seventh—major sixth; major seventh—minor seventh; major seventh—major sixth; major seventh—minor seventh; augmented prime (minor second, minor ninth)—major seventh. It should be noted that the ear places the succession suspension—resolution where it perceives the sharpest interval; in the first example of Figure 131, therefore, it hears it in the succession minor seventh—major sixth, and not in that of fourth—major third. For the same reason, the last example is felt to consist of the succession minor second—major seventh, not major sixth—fifth. Since the rhythm is determined by the chords bearing the suspension, the resolution usually occurs in less stressed position than the suspension: the reverse is infrequent. Suspensions can occur simultaneously in all voices but one, in any desired number, and resolving in different directions, even successively. But the ear will always seize upon one of them as the principal one, and this, as has been stated, will be the one embodying the greatest tension.

If the second of the two chords is one of the simpler varieties (that is, does not belong to groups III or IV), the whole first chord can be suspended, with the exception of one supporting tone.

Suspensions are not always resolved by step:

Often the tension may be resolved by substituting for the tone which would have been attained by step another good chord-factor; but this procedure is recommended only in very simple chord-relations. Between the suspended tone and its resolution, any number of tones may be interpolated, if they are so placed, rhythmically and harmonically, that they do not impair the effect of the resolution:

Particular warning must be given against tones which fit the chord too well, since they result in a premature dissipation of the tension of the suspension.

A particular variety of the suspension is the six-four chord before the dominant in the familiar cadence.
There is no reason to attribute independent value to it here, since it is entirely dependent on the chord that follows. In reckoning the degree-progression, too, it must be looked upon as a suspension, and thus has no root of its own but shares the root of its successor. The six-four chord in this usage has been called a “pseudo-consonance” or a “perceptual dissonance”. In our system, however, chords cannot seem different from what they are, and contradictory interpretations of their degree of consonance cannot arise if their analytical assignment to the proper groups (I–VI) is rigorously carried through. When the six-four chord occurs otherwise than as the fore-runner of the dominant, it keeps its own root.

A notion with which conventional harmonic theory seeks to explain those things for which it has no other place is that of the “unresolved suspension”. Our system does away with this notion. The chord in which the alleged “unresolved suspension” occurs is an independent chord, belonging to one of the inferior chord-groups, and thus needs no resolution. The effect of tension and resolution created by the suspension may be found in any progression in which chords of inferior value are followed by those belonging to superior groups. Often only the rhythmic characteristics of a passage will indicate whether it contains a suspension or simply an undecorated chord-progression.

Unprepared suspension or neighboring tone. A tone occurring in a relatively strong rhythmic position, at the interval of a second above or below a chord-tone, and resolving to the latter while the rest of the chord remains,

may be considered a suspension without preparation or a passing tone which lacks the usual point of departure. It is particularly like a passing tone in effect when its step of a second is preceded by others, belonging either to chord-tones (of the preceding chord) or to passing tones:

Thus the very common scale-passages which are ordinarily viewed as series of accented and unaccented passing tones are really combinations of passing tones and neighboring tones, since our definition rejects the existence of accented passing tones. When the neighboring tone is relatively long, it has the character of a suspension rather than a passing tone:

This is true, too, when it is not weakened by being preceded by the step of a second, and is approached by leap instead:

Between it and the chord-tone that follows it, other tones may be interpolated, just as between the true suspension and its resolution, and what was said in the latter connection applies also here:

Neighboring tones, too, can occur in more than one voice at a time. Finally, a neighboring tone may be preceded by its own, subordinate neighboring tone.

Neighboring tone left by leap. On the final, rhythmically weak fraction of the time-value of a chord, one (rarely several simul-
aneously) of its tones may move up or down a second to a tone whose relation to the rest of the chord is less close than the original chord-tone:

![Diagram of a chord](image)

Immediately following it, the new chord begins. The voice that has moved to the neighbor of one of the chord-tones of the first chord must reach its tone in the second chord by leap; hence its name. If there is no leap, the tone is only a passing tone.

*Neighboring tone approached by leap.* This is a tone (not often more than one at a time) standing at the interval of a second from one of the tones of the second chord, but sounding during the time-value of the first chord, which is what differentiates it from the unprepared suspension.

![Diagram of a neighboring tone](image)

Rhythmically it must have slight value; otherwise it will acquire harmonic importance of its own. It must be approached by leap from the first chord. Like the neighboring tone left by leap, it must occur in a rhythmically weak position and be of short duration. Both of these types are inseparably connected with a leap; they differ in their relations to the chord-progression. The one is connected to the preceding chord, and the other to the following one. The characteristic leap follows the one and precedes the other.

*Anticipation.* This is the opposite of a suspension. One or more tones of the second chord of a progression are introduced too soon, so that they occur during the duration of the first chord:

![Diagram of an anticipation](image)

The anticipation is as weak as the suspension is strong. The suspension increases the tension of waiting for what is coming, demands a certain energy for its understanding, and then rewards the listener with the resolution. The anticipation is the premature satisfaction of the listener's curiosity, and it should consequently be handled, like a pleasant but very cloying flavor, with discretion. Since even one anticipation is apt to be very obtrusive, the simultaneous use of several anticipations is usually not advisable.

*Unaccented free tone.* A tone of slight rhythmic value, in unstressed position, which is not a part of either of the chords between which it occurs:

![Diagram of an unaccented free tone](image)

Its effect is similar to that of a neighboring tone approached by leap, but it is possessed of more tension, since it is not the neighbor of a chord-tone, but is approached and left by any interval not contained in the chords.

*Accented free tone.* This tone is in a rhythmically stressed position, and in this respect resembles the unprepared suspension.

![Diagram of an accented free tone](image)

But since, unlike that tone, it is not resolved by step of a second, but moves to a chord-tone by leap, it is sharper in effect, and does not create the effect of tension smoothly resolved.

There exists no convenient and space-saving set of symbols for the clear indication of the various kinds of non-chord tones in analysis. For this purpose we may use symbols consisting of letters to which slight additions are made to indicate their varying functions:

- W Changing tone (returning tone) \( \text{[Wechselton]} \)
- D Passing tone \( \text{[Durchgang]} \)
- V Suspension \( \text{[Vorhalt]} \)
- N Unprepared suspension (neighboring tone) \( \text{[Nebenton]} \)
- N' Neighboring tone left by leap
- N Neighboring tone approached by leap
- V Anticipation \( \text{[Vorausnahme]} \)
Our discussion of the non-chord tones is based on the assumption of normal metric rhythm, in which the "strong beats" are stressed. When the opposite is true, in syncopation, the relations of the non-chord tones are correspondingly inverted. An unresolved suspension will then, since it normally occurs on the "strong" part of the beat, occur on the "weak" (but now stressed) part, and the neighboring tones approached and left by leap will occur at the ends of "strong" beats.

Among the non-chord tones the most varied combinations can occur: suspensions may be combined with passing tones, neighboring tones with changing tones and free tones. Moreover there are borderline cases in which it is not possible to label the non-chord tones precisely. Indeed it is often difficult to decide whether to consider a given tone as part of a chord or as a non-chord tone. What has been said above in connection with the suspension applies to all the non-chord tones. If the chords involved belong to groups I or II, then the explanation is simple, for the combinations produced by the non-chord tones stand so far below the main chords in our scale of values that there can be no doubt of their subordinate importance. But chords of groups III and IV are often just such combinations as are produced by non-chord tones with those of groups I and II. Value-differences between these chords and the still more complicated combinations they make with non-chord tones are hard to establish. If then the rhythm adds to the confusion, in that the added tones are not short enough to be unmistakably subordinate, a definite line cannot be drawn.

CHAPTER V

Melody

I

Theory of Melody

It is an astounding fact that instruction in composition has never developed a theory of melody. Every student learns harmony, and from the traditional theoretical instruction one would think that the handling of tonal materials depended mainly on a knowledge of harmonic facts. But everyone knows that rhythm and melody form at least equally important parts of the musical structure, as well as that they are without doubt the more fundamental elements. The direct appeal to the senses made by a rhythmic succession and the curve of a melodic line are more easily remembered by the naive listener than the differences in tension between juxtaposed harmonies. The domain of harmony has been explored from end to end, while rhythm, as I have previously stated, has escaped all attempts to study it systematically. Melody, although no definite melodic theory has been developed, has not been entirely ignored in musical theory. The study of counterpoint begins with the building of the simplest melodies, and thus sets out from the first to complement the study of harmony. But unfortunately it does not follow up its first steps. Instead of a systematic investigation of melodic phenomena, instead of approaching musical writing from the standpoint of the movement of tones, it ends up in a more or less distinctive figuration of chord-successions constructed according to the rules of harmony. The results of this melodic research, which goes no further than its first steps, are embodied in the cantus firmi, of which the following is an example:

[ 174 ]
These brief melodic successions are still, owing to their firm structure and their cool impersonality, excellent types of primitive melodic formations (provided that they are well made and not just the mournful and characterless formulae of academic counterpoint), and they are useful even in music not of educational purpose as a basis for contrapuntal work, owing to these same characteristics. But what we mean in the usual sense by a melody is related to these primitive types about as one of the higher vertebrates is related to the star-fish. The melodies we know from the works of the masters are full of life, character, and independence.

It will not be maintained that free, living melody, one of the prime factors of music, is not important enough to be worthy studying as a separate subject. The moment a student is advanced enough to begin what is called “free composition”, melody, which has been neglected throughout his previous training, suddenly assumes its full importance. Now he is free to write melodies of the freest kind, and it is assumed that he is master of a craft of which he has been taught only the most elementary principles. Does the nature of melody somehow conflict with the strictness of theoretical instruction? Such instruction is only the road to a knowledge of the technique of composition. If it had grown so independent that it could consider free music, for which it is supposed to be a preparation, as a discipline which did not fit into its domain, then the time would have come to replace it with something better. Perhaps many people think that the forms of melody are too manifold and various to be summed up in rules. Yet they must have observed that the melodies of the masters are not built up without rhyme or reason. Anything made by man, no matter how many varieties it assumes, and how much of the superhuman it seems to contain, must reveal its secret to the close observer. Why should one not be able to analyze melody, when it is possible to reduce the incomparably more numerous and more ambiguous phenomena of harmony to a comparatively small body of rules?

There are grounds of another nature, I believe, which have kept theoretical instruction from including the systematic study of melody. Melody is the element in which the personal characteristics of the composer are most clearly and most obviously revealed. His creative fancy may hit upon the most individual harmonic progressions, the boldest rhythms, the most wonderful dynamic effects, the most brilliant instrumentation; but all that is relatively unimportant compared to his ability to invent convincing melodies. On this point the expert and the naive listener are agreed. Stylistic differences in melodic formation are often almost impossible to analyze. Several composers follow the same melodic line, and yet the version of each one is recognizable from the tiniest details. The material of harmony is enormously varied; it is not, however, critically sensitive. Melody, on the other hand, can be reduced to a few, meager, basic facts, upon which, to be sure, infinite variation is possible. Undoubtedly this possibility of variation is what made it seem hopeless to earlier theorists to set up a clear system of the laws governing tonal movement. There may also have been a certain hesitation about laying bare the most personal and secret characteristics of a composer. It was not hard to maintain this silence. For composers have seldom been good theorists, and when they have been, they have preferred to deal with the most elementary points, rather than with what really concerned them so closely, while other writers could hardly describe convincingly what they knew only from hearsay.

We shall not be undermining the nature of melody, of which the finest details will always elude analysis, if we seek to know the basic principles of linear movement. And in so doing we shall be contributing to the end of the arbitrary lawlessness which reigns in this department of composition, as well as to the clearing up of the obscurity that veils melodic questions in general. Perhaps after this fog has lifted only the short-sighted and the ill-willed will continue to speak of the want of melody in the music which at first seems strange, but of which the bold creators are no sooner dead than they are praised as the singers of divine melodies. Lack of rhythmic imagination and harmonic poverty are greater evils than inferior
melody, and they are much more common. Yet one rarely hears them complained of. These fields are more familiar to the musician and the listener—rhythm because of its direct appeal, and harmony through habit and training; everybody understands more easily what the composer means, so far as these elements are concerned. Once the basic rules of melodic structure are as well known as the simplest practices of harmonic progression, judgements of melodies in a new and unfamiliar style will be more accurate than they have been.

2

Chordal Association

We simplified our study of the harmonic element of music by leaving rhythm so far as possible out of account. It will be useful to do the same in our search for the basic rules of melody. It may be objected that harmonic progressions are conceivable in which the influence of rhythm is reduced to the very minimum trace that cannot be eliminated in harmonic change, while melody is unthinkable without the continuous influence of rhythm. This is true. Every step from one tone to the next involves a duration relationship, and consequently depends on a regular metric beat as a unit of measure. Yet it is not at all impossible to disregard this simple influence of rhythm in our investigation. What is more difficult is to get along without rhythm as the regulator of forms, the connecting factor between time-units of unequal length. Even in the most primitive melodies, the tonal material falls into little pieces of unequal length: motives, for whose rhythmic construction the mere metric beat is no more sufficient than for the construction of larger formal units. If one is to construct melodies with the same sureness that is taken for granted in the setting up of chord-progressions, an exact knowledge of the higher elements of rhythm is indispensable. One should know as much about the form and inner dimensions of motives as about their number and duration. That we are usually satisfied with a more or less developed feeling of this part of melodic construction, instead of knowledge about it, is to be regretted, but, the field being unexplored as it is, understandable. Pleasant as it would be to provide in connection with the present theory of tonal relations a key to the rhythmic part of our work, I must postpone the solution of this problem to some later time. As an excuse rather than as a justification for this shortcoming, I may point out that the present theory thus stops at the same point as its predecessors. Moreover, I am not writing a comprehensive treatise on composition, which would not be complete without an exact treatment of all the elements of musical structure, but am only trying to introduce law and order into the realm of the handling of tones.* The invention of melodies reaches beyond the knowledge that is needed for the simple manipulation of tone, but the rules of melodic procedure outlined in what follows suffice for the theoretical foundation of the art of handling tones. So far as seems necessary for the creation of small melodic forms, the part of melodic work that has to do with the construction of motives is discussed in the later volumes of this work.

We have seen that in the harmonic progressions of a piece of music not only the time-regulating force of rhythm but also forces which regulate space and harmonic relations are operative. We have become acquainted with the effect of harmonic fluctuation and of the relations of the tones in regulating the harmony. We have also encountered the space-dividing energy of melody in the form of tonal successions and of the two-voice framework, but we have had no opportunity to examine the laws which govern these linear developments. These are what we must now investigate.

We shall start from the harmonic point of view, already familiar to us. When we considered the fluctuation in harmonic progressions, we tacitly assumed motion from chord to chord—a melodic phenomenon. Just as there a melodic force operated in the domain of harmony, so harmonic force operates in melodic connections. We have already established the fact that even when tones are sounded successively, a root can be found among them. The connecting

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*In the translation of the title of the original work, *Unterweisung im Tonsatz*, the author was reluctant to see the word Tonsatz (literally, the setting of tones) rendered by "composition", but diligent search failed to reveal any fully satisfactory substitute.—Tr.
force of harmony is thus not confined to the tonal mass lying directly above the root of a chord, for it permits the root-predominance of one tone to be felt even in relation to tones sounding before or after it.

The most obvious form of harmonic connection in melodies is in the breaking of triads or the simplest seventh-chords. Melody of this sort cannot be very expressive, for it has hardly torn itself loose from harmony. On the other hand, it has something compellingly natural about it, which has always served to give the main structural points in a composition the mass and solidity which they require. We know this primitive kind of melody, still entirely dependent on harmonic forces, from the opening themes of hundreds of Classic and Romantic compositions. The symphonies, concertos, and chamber-music works from those of the early Mannheim school to those of Bruckner and Strauss would be unthinkable without this sort of lapidary theme construction. This type of melody shows clearly the fallacy of the idea generally entertained by music-lovers of romantic tendency that they wish to hear nothing but "beautiful" or even "expressive" melodies. The melodies we refer to are neither beautiful nor expressive. The openings of Beethoven's Fifth Symphony and of his C Minor Piano Concerto can hardly have overwhelmed a single listener in history with the beauty and loveliness of their melodic form. What is expressed in them is a will toward clear formal development: they are the counterpart to the harmonic cadence. In these thoroughly harmonic opening themes melody and harmony have not yet conquered the structural force of rhythm: in the cadence, form, having previously lost the upper hand to melodic and harmonic elements, regains it. If against such a harmonic and forcefully natural theme a second theme is contrasted, which exhibits in the most characteristic way the subtle charms of melodic detail, it is the juxtaposition of such different melodic types that permits the melodic structure of the second theme to be appreciated. This explains why so many, composers of the post-Classic period, despite the beauty and often even fascination of their thematic invention, fail to reach the heights attained by the Classic masters. They kill one beautiful theme with another, so that sharp thematic contrasts and consequent melodic tension are lacking—a lack which is brought all the more painfully to the attention of the listener by the faulty proportion between a content which is lacking in tension and a form which is of exaggerated duration.

If in a tone-succession based on a broken-chord formation there is an accumulation of non-chord tones, originating simply as decorations, the melodic element is brought more into the foreground and the harmonic element is subordinated. This process can go so far that in superficial listening one hardly notices any harmonic connection. But that such a connection is always present is proved by the fact that intervals have roots. The composer cannot do away with the harmonic connections of the intervals; but what he can do is to compress or spread out the melodic expanses over which these connections operate. A melodic line which, although it does not have the unfeeling massiveness of a mere broken-chord formation, still holds close to chords that hardly change, despite all its trimmings in the shape of non-chord tones, will produce in the hearer a feeling of repose, or even, at worst, of boredom. On the other hand, frequent changes from one harmonically articulated melodic fragment to another produce a fresh, exciting effect, which can lead, if the roots change too frequently, to utter confusion, to a harmonic and melodic vertigo. The groups
of tones in a melody which are harmonically connected are like the links of a chain; they give the melody color and sheen. They are the real body of the melody, strange as it may seem to speak of body in connection with a linear phenomenon like a melody. It must not be forgotten that a melody is only primarily linear, and that the comparison with a curved line applies only to the most obvious, external aspect of a chain of tones. The melodic thread has an ever-changing but ever-present volume or thickness. How the outlines of this formation, which we have now recognized as having body, are drawn, we shall learn later.

There are extreme puritans who consider possible the construction of a melody without any harmonic connection. Although we know that this is not possible, let us demonstrate its impossibility just the same. If one were to connect only intervals of low harmonic value, such as minor and major seconds, still at some point a major or minor third in relation to one of the tones would be formed, which would give the whole group a harmonic sense. When thirds, or other intervals of strongly harmonic significance, occur directly, they draw the tones that surround them into their own orbits. With a combination of fourths, fifths, and major and minor seconds and sevenths it would be possible to construct a fairly extended succession which would not immediately reveal any inner harmonic connection. But this would only mean that the harmonic connection was not obvious, not that there was none. The power of fourths and fifths is so strong that they attract the entire attention to themselves. If several fourths or fifths occur in succession, the ear is made uncertain by the accumulation of clear harmonic groupings and their variety within a short space of time. The impression of lack of harmonic connection which such a passage gives is based, therefore, on an illusion—on a fatigue of the ear, actually—and not on any real lack of harmonic association. The ear is surfeited with harmonic groups, so that it can no longer follow them. But the harmonic center of such groups made up of successions of seconds, fourths, fifths, and sevenths within a melody can be found according to the given recipe, despite the frequent change of roots. Usually we do not have far to seek, for the ear tries, as we have seen, to discover a broken chord of groups I or II in every tone-succession. In broken forms of chords of groups III and IV, which is what successions of seconds, fourths, fifths, and sevenths make, it often finds hidden a simple triad, which it takes to be the skeleton of the succession. The other tones are then related to this triad as non-chord tones. Often it is satisfied with a single prominent interval—a conspicuously placed fifth, fourth, or third—to which it relates everything else as a melodic (i.e., only secondarily harmonic) addition. But some harmonic connection the ear will always find—if not within two or three tones, then over a wider space. Consequently it is impossible to exclude chordal association as a factor in melody.

Melody Degree-Progression

The tone-groups contained in a melodic line are governed by the same laws that rule tonal combinations of primarily harmonic significance. Accordingly, everything that has been said about harmonic fluctuation and tonal relations applies to melodic groups also, although less strongly, since in them harmony is subordinated to melodic force. The effects of fluctuation, particularly, are obscured, since the ear always seeks triad formations in melodies, and usually succeeds in finding them in some form or other, by accounting for complicating factors as non-chord tones wherever possible. But the values of tonal relationships apply here with undiminished force.

The same device that enables us to establish the logic of a harmonic succession will serve us in good stead here; what tells whether the harmonic construction of a melody is logical and appropriate is the degree-progression. In order to set up the degree-progression of a melody, we shall enclose in a dotted bracket (see Figures 154—158) the notes which can be heard without effort as a harmonically related group. In general, these groups will form broken triads with non-chord tones. But often our analysis will yield more or less than a triad; less if a third or a fifth (or the inversion of one of them)
struction is mainly in accordance with the relationships of Series 1.
Everything that we have said about the degree-progression—the
best intervals to use, the things to avoid—applies here, too. The
only difference is that this new degree-progression, drawn from
the harmonic content of a melody, may show greater activity, and
need not lean so heavily on the strong intervals—those near the
beginning of Series 1.

One thing should be noted: the new degree-progression is
complete in itself, and fully independent of the main degree-progression
upon which the joint harmony of the several voices of a piece rests.
In a piece made up of several simultaneous melodic parts, as many
degree-progressions are possible as there are parts, and it is possible
to imagine a case in which all these degree-progressions would be
fully independent of one another. The independence of the melody
degree-progression goes so far that the harmonic groups of the latter
are in flat disagreement with the harmonic content of the whole
piece or passage. The familiar theme from the Haydn “Surprise”
Symphony

shows very clearly that against the dominant harmony of the whole
(in the last measure) the melody degree-progression may show the
tonic. The last measure, by virtue of its preponderance as the
terminal point of this melody, as well as the $f\rightarrow$ in the measure
before the last, do indeed make possible a feeling of change
toward the dominant, of modulation to G. But this is really true
only for listeners who are not used to comprehending the melody
degree-progression apart from the degree-progression of the whole.
The listener who analyzes this melody precisely would require, for
the assumption of a dominant or leading-tone effect, a $d\downarrow$ ($d'\uparrow$) or $a\downarrow$
in the melodic progression, in the absence of which the $f\rightarrow$ is
nothing but a neighboring tone approached by leap within a widely
extended C-major triad. Thus we see that it makes no difference to
the melody. The only thing that counts is the actual harmonic con-
ten of the melody itself; this appears somewhat grotesque in an
example like the foregoing, but in more complex constructions it
will be found completely convincing. It would naturally be easy to
read simple harmonies into the melody, agreeing with the harmony
of the whole. But this would contradict an analysis that aims solely
to show the harmonic logic of a melody, and does not seek to con-
firm in some other way what it has learned from the degree-
progression of the entire harmony.

It often happens that the degree-progression of the harmony and
the degree-progression of the melody are in full agreement. This
results in a fine, straightforward, but sometimes insignificant clarity.
Just as often, the two progressions are opposed. How wide the gap
between them may be, whether they coincide except in certain de-
tails or go their own brutally independent ways—these are questions
that can be settled only by experience and taste, not by technique.
No one will want to go so far as to say that nowadays the best result
is always attained through opposed degree-progressions. Unques-
tionably even the little-trained listener can tolerate independent
progressions more easily than in former days, but it is still sensible
to produce strong harmonic tensions only when the style and pur-
pose of a piece demand it. Nothing is gained by attaining the con-
trast of the degree-progressions at the expense of the effect of the
whole—that is, by setting a well-developed melody to harmonies
that completely contradict it, just for the sake of this contrast.

4

Seconds

The real building units of melody are seconds. They perform
two functions in melodic space, just as in harmony the harmonic
intervals perform two functions (that of the fluctuation, and that
of tonal relation). The influence of the fluctuation is felt in the
slightest change of a chord, while "the effect of the relationships
requires greater extension in space. Similarly, steps of a second in
melody act on the one hand as the measuring units and content of
the briefest melodic sections, and on the other—like the relation-
ships in harmony—as regulators of the larger melodic connections. They are used to fill out the harmonically stronger intervals, but they are also placed immediately before the first tone of such an interval or after the second one. Often they produce simply non-chord tones (N, V, N', N, etc.), as when the harmony belonging to the main tone does not change with their appearance. But if one of their tones is an essential part of an independent chord, they are no mere melodic decorations but become important structural members of both the harmony and the melody. As in the cases of all melodic intervals, the direction in which a second moves is of the greatest importance to the form and effect of the melodic curve.

The step from a higher tone to a lower is always felt as a relaxation of tension. This motion is undoubtedly the most natural one in music, since the production of a higher tone requires, at least in all instruments in which mechanism does not play a large part, greater energy than that of a lower one, and accordingly a step downwards gives the impression of diminished resistance, of an approach to rest and to the end. The singer, whose instrument is more sensitive than any other to the differences in tension between tones of different pitch, feels this most clearly. But even keyboard instruments, which on account of their mechanism should give the listener the impression that it makes no difference whether one moves up or down, or over how great a distance, do not entirely conceal the feeling of lessened resistance in a downward movement. What other explanation is there for the fact that the very common downward interval of a fifth from the dominant to the tonic, which occurs in the bass in the commonest of all cadences, is felt, irrespective of instrumental questions, as a fall, and even explicitly as a final fall?

The downward interval is, because of its tendency to a decline and resolution of all tension, sterile: nothing grows out of it. In a rising interval, the energy of the performer gathers impulse, and the fact that a certain space has to be traversed and a certain physical resistance overcome frees that energy, and exercises an effect of gathering excitement and tension on the listener. The larger the interval, the greater this effect—particularly, again, in singing, or on instruments which show the necessity for additional physical and mental energy more easily than do the keyboard instruments.

The melodic principle that a rising interval creates tension and a falling interval resolves it is affected by the harmonic tendency to connect different tones. If, for example, the rising or falling interval takes place within a single chord, so that both tones of the interval are members of the same chord, there is no feeling of either rising or falling tension. Even wide leaps are of little effect in these circumstances. The distances here spanned have been marked out already by the presence of the stationary chord, even if the ear has not counted the second tone of the interval as belonging to the chord until this tone actually appears. Consequently, the traversing of this space involves no effort, and it does not produce in the listener the feeling of expectation fulfilled that he gets when the leap is made to a non-chord tone, or when it is accompanied by a change of chord.

It would be impossible to sum up all the possible melodic intervals within our system; it would even lead too far if we were to try to examine the characteristics of every upward and downward interval within the octave. Accordingly, we shall confine ourselves to the space of a fifth. In the wider intervals either we see an intensification of the relations that govern those below the fifth, or else the larger intervals are split up so that there occur in detail the same phenomena that we shall observe among the thirds and fourths. We limit ourselves further to the investigation of falling intervals. If we wish to know the effect of the rising ones, we need only change the minus sign in our result to a plus sign.

The succession e(eb)-d-c, the most common of all downward melodic divisions of the third,

\[ e(eb) - d - c \]

brings the e(eb) into relation with the c, according to Series 2. But the d, acting as axis, balances the forces to the extent of preventing the weight from falling suddenly and heavily on one side. The
e(e₄) retains a certain part of its independence. Not so, however, if we substitute a d₄ for the d:

The leading-tone tendency of this tone makes the c so strong that the e(e₄), now abandoned to its fate, becomes the mere vassal of the c. In the succession e-e₄-c,

the connection with the c is just as strong. Since the third appears in two forms, and the step from the major to a minor third represents a decline in value, according to Series 2, it loses its original power and cannot resist the root-power of the c. The succession e₄(d₄)-e-c embodies a rise in value:

but the relation to the c is still very strong, since the e₄(d₄) has the effect of a neighboring tone of the superior major third, and thus loses its independence. The same is true in lesser degree in the succession d-e(e₄)-c.

In the successions d₄-e-c and d₄-e₄-c, the d₄ has the effect of a neighboring tone of c, with the e or e₄ interpolated between it and its resolution. In all these cases, the e or the e₄ is subordinate to the c. Thus we see that there is no purely melodic way to purge the interval of a third, however it occurs, of its harmonic value. To diminish that value, rhythm must be called upon.

In the following example we see the fourth divided up into three intervals:

The f is hardly more than a neighboring tone of the third e-c or e₄-c; the last four successions can also be looked on as pairs of thirds, which would yield the degree-progression d-c or d₄-c. If the fourth is to be independent, the third must be subordinated by rhythmic means, or omitted altogether. In the successions f-d-c and f-d₄-c, the fourth predominates:

but one must be careful to give the d or the d₄ slight rhythmic value, since otherwise the third f-d or f-d₄ will come to the fore, and produce again the degree-progression d(d₄)-c. The successions d-f-c and d₄-f-c also permit the fourth to prevail, if the d or the d₄ has slight duration. The third becomes almost completely harmless if it is used exclusively to reinforce the fourth, as a neighboring tone before it:

The division of the tritone by seconds presents no problems. We remember the description of its characteristics in Chapter III, according to which it must always occur either in chordal grouping or in subordinate melodic function (as a neighboring tone).

The division of the fifth into a series of descending seconds always gives the effect of a triad with varying emphasis upon its different factors. The succession g-f-e . . . c
makes the third, e, prominent, while g-f₂-e ... c stresses the fifth more, because the f₂ is tied by the half-tone to the g; the same contrast exists in even sharper form between g-f-e₇ ... c and g-f₂-e₇ ... c:

In g-e-_b ... c, the e₇ is important, because the diminution of value between the two thirds makes the e sound like the neighboring tone of the e₇. In the successions g-e-f ... c and g-e₇-f ... c the fifth is liable to sacrifice its value by becoming part of the third e-g (e₇-g) or the neighboring tone of the fourth. If the fifth is to be prominent, it is provided with a neighboring tone (f-g ... c, f₂-g ... c, a₇-g ... c, a-g ... c):

If, on the other hand, the root is to be emphasized, then it is preceded by a neighboring tone d-g ... c, d₇-g ... c.

If the entire interval of the fifth is traversed in minor seconds, then all these fine differences of tension are destroyed:

Accordingly, division of the fifth by chromatic seconds has the lowest value.

Familiarity with the system briefly sketched here for the smaller intervals must be gained through practice and experience. The recipe given will then make it possible, if it is felt desirable, to reckon the effects of seconds in the division of other intervals within the octave. But, combined with experience, a healthy musical instinct will be a more reliable guide through the innumerable possibilities of interval-succession than the most careful reckoning.

5

Step-Progression

Important though the detailed work of seconds as connecting links between the harmonically significant tones of a melody may be, they achieve a really dominant position when they become the guide-posts of the melody. As such they regulate its horizontal and vertical extension, and are thus the complement of the degree-progression, which is the guiding line for its chordal coherence.

Every melody consists of prominent tones and subordinate ones. On the one hand, the roots of the little chord-groups in the melody—that is, of the "body" of the melody—must be considered the more prominent tones. Their chief function is the setting up of the degree-progression, and as the regulators of the degree-progression they have had their just evaluation. But within a melody there are other main tones whose significance is primarily melodic. Among these may be the roots of the chordal groups which are the pearls on the string of the melody, but more important are those tones which are placed at important positions in the two-dimensional structure of the melody: the highest tones, the lowest tones, and tones that stand out particularly because of their metric position or for other reasons. The primary law of melodic construction is that a smooth and convincing melodic outline is achieved only when these important points form a progression in seconds. The line that connects one high point to the next, one low point to the next, and one rhythmically prominent tone to the next, without taking into
consideration the less important parts of the melody lying between
these points, is called the \textit{step-progression}. It is easy to draw. If
we play a melody through slowly, and listen carefully to the points
that mark the pitch limits, the step-progression separates itself
almost without any effort on our part from the rest of the melody:

\begin{center}
\includegraphics[width=\textwidth]{fig174.png}
\end{center}

Melodies of simple construction exhibit a simple step-progression.
In such melodies, the step-progression consists of a single succes-
sion of upward and downward steps of major and minor seconds, to
which we need merely make certain subordinate additions toward
the construction of further step-progressions. The more complicated
the structure of a melody, the greater the accumulation of hidden
harmonic groupings in it, the greater its compass, the richer the
mixture of larger and smaller melodic intervals—the greater the
number of step-progressions will be. Thus in a well-constructed
melody there may be four or more step-progressions going along
simultaneously:

\begin{center}
\includegraphics[width=\textwidth]{fig175.png}
\end{center}

Every one of them may be independent of the next, and without
any connection to it. But that is not necessary. Step-progressions
may be many or few, and may be fully independent or may pass
from one into the other. The less stiff and forced their development,
the smoother and clearer will be the course of the melody. A useful
function in this connection is performed, outside the step-progressions,
by tones which do not move, but repeat themselves at short
intervals and prevent the interplay of the step-progressions from
leading to an over-rich and confusing development. (See the en-
circled notes in Fig. 174.) The distance in time from one of the
prominent melodic points that forms a step-progression to the next
cannot be stated in a rule. The tones forming a step-progression are
sometimes in direct succession and sometimes widely separated.

\begin{center}
\includegraphics[width=\textwidth]{fig176.png}
\end{center}

Like everything else, the construction of step-progressions can be
overdone. A barren creeping up and down, with the high and low
points mostly occurring in close succession, destroys in the listener
any feeling of tension, such as he derives from observing a step-
progression which does not always move just as he expects it to.

In the step-progression, octave transposition may take place, so
that sevenths and ninths may replace seconds.

\begin{center}
\includegraphics[width=\textwidth]{fig177.png}
\end{center}

This occurs in melodies in which the space of one or more octaves
is filled out with chord-groups of strong harmonic coherence. The
cohesive power of the broken chord is such that the connection of
a tone in one octave with a tone in another is at once clear. In fact
a melody full of leaps, even without such chordal organization, in-
vites octave transpositions in the step-progression; but such melo-
dies are not very common.

There are exceptional cases in which the progress of a melody
does not take place according to our rule of seconds. This happens
especially when a melody moves quickly from one register to an­
other by means of a broken chord in either an upward or a down-
ward direction.
Here, too, the harmonic stability of the broken chord assures the coherence of the whole, no matter whether the tone that stands outside the series of seconds is a third, a fourth, or even further distant. Finally, the prominent tones of a melody may not belong to either a chord or a step-progression, when the need for intense expression requires that the attention shall be riveted by the conspicuous strangeness of such tones.

If clearly perceptible broken chords can burst the confines of the space outlined by step-progressions, it follows that step-progressions may conflict with melody degree-progressions. The harmony that is implicit in the melody—the harmonic flowering, so to speak, of the degree-progression—may assume such importance that the setting up of a step-progression becomes unnecessary. In a type of melody which does not go beyond chordal factors and shows scarcely any linear development, the degree-progression is thus the only regulator of melodic growth. If, however, the chordal groups of such a melody permit the erection of a step-progression, the latter enjoys greater freedom than ordinarily: it may contain sharp interruptions, breaking off at one place in a chord and beginning again at another, without obscuring the meaning of such passages.

Conclusion

We have arrived at the end of our reflections on the structure of melody. What services do the melody degree-progression and the step-progression render the composer?

They are indispensable for the analysis of existing melodies, in which one always begins with the determination of the harmonic content as the cruder ingredient, extracting the degree-progression and then seeking for step-progressions. It will be found that there are pleasant, attractive melodies of which the degree-progression is satisfying, but of which the step-progression is faulty, either because of its monotony and lack of the elements of tension and surprise, or because of its planless construction:

Such melodies give listeners no more than a certain pleasant impression. Other melodies, especially those which strive for the most definitely linear character, may have a well worked-out step-progression and a poor degree-progression. Such melodies make the listener restless, since he can follow the vague harmonic connections only with difficulty. Balanced and well-rounded melodies, on the other hand, which give the listener a sense of joyful well-being,
exhibit a beautiful equilibrium of the two progressions. The succession of harmonic formations is convincing because it rests upon a logically developed degree-progression, while the line of the melody carries the listener securely to the desired points because the clear step-progressions do not allow him to wander from the path. And the two kinds of progression are so constructed that they do not conflict.

But in the work of construction as well as in that of analysis the reckoning of degree- and step-progressions is of help to the composer. How often it happens that a theme which is based on a good idea will not assume the form which the composer would like to give it! He tries this and that, but there remain passages which he cannot seem to perfect either by the help of a better melodic idea or by the most conscientious polishing. If these passages are good in themselves, they do not fit the rest of the melody. Or the general outline of the melody is good but the details are poor. To find out what makes the tones so refractory, he need only apply the measures of degree-progression and step-progression. He will learn either from the degree-progression that a poor harmonic succession is obstructing the course of his melody, or from the step-progression that there are holes in his melody—leaps or vague connections that prevent it from growing as it should. If he then changes the tones at these particular places in such a way as to improve his degree- and step-progressions, his theme will suddenly take on more convincing form.

An example will explain this procedure more clearly. Suppose a composer had invented the following melody:

This melody may appeal to some and not to others, but let us completely disregard judgements which depend purely on personal taste: a melody such as this may be encountered often enough nowadays. We have, to be sure, torn it away from its context. We do not know its exact purpose. It is possible that it might have a particular task to fulfill for which it must have just this form; but that is not probable. Judged as a melody, this series of tones is poor. The degree-progression is not good because the tritone-chord formation e-bb-f makes too strongly coherent a section at the beginning. The latter part of the degree-progression is usable, although one may question whether so much space should be devoted to the harmonic center g, which dominates the section from the second to the seventh tone, and whether the strongly harmonic grouping b-g-e-c (6th to 9th tones) should be retained. Only slight suggestions of step-progressions are present. They are not sufficient to give the hearer the feeling of reliable melodic guidance. If now we improve the degree-progression in such manner (we need not go into the individual steps of the process here; they are illustrated in Book II) that it acquires the following form,
and if we build some step-progressions into the structure (the method of doing so here employed is only one of many possible ones), we shall achieve a melody that uses the same motives as the original one, but that is indisputably better constructed from both melodic and harmonic points of view, and is accordingly more convincing.

There is a notion, springing from ignorance of the working-processes of the artist, that the true artist can be as "wrong" as he likes; that if he does something "wrong" it makes sense and is better than much that would be "right". This notion assumes the presence of a special guardian angel that permits liberties in artistic work which are not granted in the other domains of human endeavor (not without their own importance!). According to this idea, composing, writing, and painting would be ideal occupations for all sorts of know-nothings, and one would have to pity those who sullied their fresh, unspoiled point of view with comprehensive technical knowledge. But things are not as simple as that. What is "wrong" in the usual sense is so only with reference to inadequate theories of composition, which apply a narrow measure to the abilities of a composer. But no one can devise and write things which are "wrong" according to the principles of the step- and degree-progressions if he wishes to make his music as intelligible as possible to his listeners. It will not be denied that the theory here put forward is more comprehensive than its predecessors; and any trial will show that it applies just as well to any style of the past as to the music of our own time. The objection that the musicians of the past had no idea of these progressions and yet were great masters is no objection, really; on the contrary, it is the best proof of the natural foundation of this system. If there are composers even today who know how to handle all the tonal materials unerringly without knowledge of the precepts laid down here—yet without simply imitating wiser men—they are to be praised and envied. But others will welcome the help here offered them. If on the other hand, a man lacking in talent attempts to rely entirely on such knowledge, without having any real gift for his work, the most perfect working out of step- and degree-progressions will not help him. Everything he does will be correct, and yet we would gladly do without it. There have always been many rules of the craft, and now come more. When one has mastered them to the extent of being able to use them with the same facility as one uses older precepts, one will find that one has taken a significant step in the direction of clear and wholly satisfactory writing. But no one will be so stupid as to assume that what has been impossible throughout all ages is now possible: to create a work of art without creative impulse, simply by burrowing and calculating.
CHAPTER VI

Analyses

The following examples and their analytical dissections are intended to show that the music of all styles and periods may be analyzed by the methods proposed in this book. The advantages which these methods offer the composer in his creative work cannot, alas, be displayed with the same ease. They may be observed only in one's own work along the lines here suggested; for such work, the practical books of this series will outline the necessary training.

Having read the foregoing chapters, the reader should have no difficulty in studying and appraising the following analyses. Often he will arrive at different results from those here given. There is no harm in that. I have in each instance chosen only one of many possibilities. Moreover, the notation of a piece of music is the mere chemical precipitate of the work itself. The charm of the latter lies not in scientific exactitude, but in the fact that it arouses in the hearer not alone direct emotional enjoyment, but also a pleasure in the recognition and judgement of the impressions received. Even with the closest familiarity with the objective content of a work of art, the judgements of all observers will never completely coincide.

In the musical examples, the harmonic relations are indicated by the addition of the symbols for the non-chord tones. By eliminating the latter, the harmonic fluctuation and the degree-progression are calculated. In the degree-progressions, the guide-tones are included in such manner that the step from the root of a tritone-free chord to the guide-tone, and vice versa, is indicated with a line leading from one to the other. If for reasons of voice-leading the guide-tone has to approach or leave the octave of the root of a tritone-free chord, instead of the root itself, the octave is included in parentheses.

It may seem strange to apply our analytical method to music of which neither the theory nor the practice have ever yielded to attempts of this sort. Yet no one will deny that in these most linear of all compositions chord-groups are hidden, whether with or without the intention of their creators. The search for the logic of these groups justifies us in setting up the degree-progression. The plotting of the step-progression will surely meet with no objection.
The principal voice (the second from the top), which in the original is provided with words, is, with its stepwise motion only occasionally interrupted by leaps, so centered around the tone c', that in its degree-progression the strong harmonic steps of the fourth and fifth alternate in the pleasantest balance with the strongly melodic seconds and the chordal thirds. The step-progression seems at first glance a little sparse. Closer inspection shows, however, that the oft-repeated step of a second d'-c', with its intensification e'-d' (in the tenth and eleventh measures) is based on wise calculation. The melody is thus set in motion only gradually, while in its later development (not given in the quoted passage) it is elaborated with a considerable variety of motives, and in the refrain it reaches full bloom. We thus see included in the step-progression an artistic device which in general is a hindrance to melodic development (the frequent repetition of two tones), here justified by the purpose of the whole structure.

No one will wish to measure the melody of this early music with
the same yardstick as our modern melodies, pregnant with expression as they are. It is extraordinarily simple, and at the same time leaves the greatest possible room for harmonic development. The latter is not expressed in the arrangement of the degrees: the degree-progression of the complete harmony is limited to the establishing of c as the tonal center, by means of sure and unhesitating steps, with emphasis on the subdominant, then a modulation to f, and a return to c. But the conflicts of detail between harmony and melody, above this firm foundation, are worthy of the highest admiration. There are the boldest oblique accumulations of non-chord tones, as well as parallel fifths, sevenths, and seconds—all features which can only today again be felt as correct and beautiful, because we again have the ability, common in Machaut's time, to separate harmonic and melodic elements while listening, and to weigh one against the other. We see in this music a true counterpart of the Gothic style of architecture of the same period, in which the great, central features of the structure are of elementary simplicity, corresponding to the harmony of this Ballade, while the fullness of decorative detail, here represented by the non-chord tones, is almost oppressive.

The harmonic fluctuation made up by the principal chords is hardly noticeable in the maze of decorative lines, and it consists only of the very slight value-differences between chords of groups I₁ and I₂. The two-voice framework shows most clearly the connection of this music with that of later times. It is very subtly constructed, with the intervals cleverly distributed. Observe the feeling of rest produced by the parallel octaves in the fifth and sixth measures, making the sharp cadence, with its parallel ninths, the more prominent. The same effect is seen at the end of the example, where the repose induced by the octave e-e' in measures 13 and 14 is interrupted by the last two quarters of measure 14, forming the cadence, this time with the very intense parallel motion in sevenths.

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* During a rest, the tone preceding the rest must always be regarded as remaining part of the harmony, for the rest interrupts only its actual duration and not its harmonic significance.
This piece is a true Chinese puzzle, from the harmonic point of view. The ear is constantly offered a choice of what it wishes to hear: independent chords, or subordinate, non-chord tones. Only by the latter can formations as striking, in a style of simple tonal relations, as the a-chord in the f minor (or c minor) of the fourth measure, and other similar places in the course of the piece, be explained. This intentional uncertainty goes so far that even in the first measure, in which there are only two voices, the listener does not know exactly what is meant. When he follows the design of the upper voice, he is inclined to hear the highest tone of the three-tone motive as a neighboring tone, and the third tone (g' and a' in the first measure) as its resolution. But the presence of the lower voice shifts the effect of suspension to the fourth eighth-note (though this suspension does not have its full effect, since a condition favorable to it—the placing of the interval of stronger tension in the stronger metric position—is not fulfilled). And it makes the last eighth-note of the measure a returning tone, which on the first eighth of the next measure, despite the rest, becomes a suspension. In the third measure, however, the relations originally expected occur, and the third and seventh eighth-notes can really be heard as neighboring tones. In the seventh measure, the listener has to change his interpretation again, and so it goes throughout the piece.

It is quite possible in listening to sum up the harmonic content as consisting of fewer chords of longer duration, which would result in an even greater number of non-chord tones. Thus the degree-progression for the third and fourth measures would be:

\[
\begin{align*}
\text{third measure:} & \quad \text{VI} \quad \text{I} \quad \text{I} \\
\text{fourth measure:} & \quad \text{I} \quad \text{VI} \quad \text{I} \\
\end{align*}
\]

and for the ninth and tenth:

\[
\begin{align*}
\text{ninth measure:} & \quad \text{VI} \quad \text{I} \\
\text{tenth measure:} & \quad \text{I} \quad \text{VI} \\
\end{align*}
\]

The harmonic fluctuation shows clearly the uncertainty in which the listener is placed. Except for the series of intervals in the first measure all belonging to group I, there is an uninterrupted succession of waves. The differences in tension between the chords are very small; only rarely does the tension rise above group II. (Chords of group VI do not indicate any sudden rise in tension: their indeterminate quality makes them adapt themselves to their context, and produce hardly any more tension than those of group II.) It is the very active degree-progression that creates the necessary tension. Consider how the tonal relations of the center F are exploited in measures 5–9. The ambiguity of the chordal texture, the continual swing of the pendulum back and forth between chords of little difference in tension, and the degree-progression worked out with every resource of tonal relationship—all these are unified by the great repose and purposefulness of the tonal structure. The tonalities succeed each other almost exclusively by steps from one center to another closely related one. The constant, restless flux of all the structural elements that can be directly heard rests upon broad and firm harmonic foundations. The contrast between the harmonic stability of the background and the nervous unrest of the chordal content is one of the greatest charms of the piece.

The two-voice framework partakes of the active nature of the foreground. It corresponds exactly to the two outside voices at any given moment, is easy to follow, and is accordingly not notated separately here.
4. Richard Wagner
Tristan und Isolde, Prelude

Harmonic and Melodic Analysis

1. Fluctuation
   $l_2$  $\text{Db}_2$  $\text{Gb}_1$  $\text{D}_3$  $l_2$

2. Two-Voice Framework

3. Degree-Progression

4. Tonality
The Prelude to Tristan is one of the finest examples of the elaboration of a two-voice framework. The observer of the intervals formed by the outside lines of the harmony will be astonished to see how intervals of varying tension are juxtaposed. The procedure is illustrated beginning with the very first chord: the interval of a minor third (written as an augmented second) is followed by a major third, which represents a decrease of tension; the tension is then sharply increased again in the tritone on the first eighth of the third measure, only to be resolved completely in the fifth which follows. In this admirable way the tensional development of the framework is calculated from beginning to end, as the section here notated illustrates.

No less remarkable is the handling of the harmonic fluctuation and of the degree-progression. The distribution of the harmonic tension produces a beautifully varied succession of sharp and mild chords—chords of Group A and chords of Group B. Yet this ebb and flow dispenses almost entirely with chords of the highest tension—those of group IV. In the degree-progression, both the roots and the guide-tones are admirably treated. The first measure with its up-beat is treated as a broken chord, because the ear relates the two tones; likewise the fifth, eighth, and ninth measures. In measure 9, the d' of measure 8 has to be taken into account, and thus beneath the a' of measure 9 there is a root, d'. The six-four chord in measure 18 is so passing in character that one is justified in taking its bass tone as its root, just as in a six-four chord preceding the dominant in a cadence. The same is true in measure 32.

In the analysis of the tonality it should be noticed that those roots upon which tritone chords are built must be regarded as dominants of tonics lying a fifth below. Thus the tonal center of the first three measures is a, and of measures 5–7, c. If we set out the centers of the various tonalities in succession, we obtain the following series:

\[
\begin{align*}
\text{Center} & : & \text{Tonality} \\
\text{Measure 1} & : & a \\
\text{Measure 2} & : & b \\
\text{Measure 3} & : & c \\
\text{Measure 5} & : & b \\
\text{Measure 6} & : & a \\
\text{Measure 7} & : & a \\
\text{Measure 8} & : & c \\
\end{align*}
\]
The analysis of the opening of this work produces such simple results that it seems unnecessary to add any explanation. The tonal construction is revealed by the degree-progression. It is a broadly developed group around c as a center. Since this one tone dominates the entire section quoted, it is not notated in the example.
After the foregoing analyses, the dissection of the example on pages 217-218 should also be clear. The reader is now in a position to appraise the harmonic fluctuation, the two-voice framework, the degree-progression, and the tonal scheme without further guidance. To make the analysis of the chordal relations clearer, I have reproduced the piece, immediately below the original notation, in the version which results from the ear's gathering together of the units of broken-chord formations and delayed sections of chords and its exclusion of non-chord tones from the harmonic combinations. I have analyzed the piece only from the harmonic point of view because the melodic element seems to me to have retreated far into the background in this piece. Those who disagree are free to undertake the melodic analysis for themselves. The tonal ordering of this fragment springs from the desire to group in the analysis as many chords as possible around one tonal center, so far as that is possible at all in this case. Subdivision of the longer sections would result in shorter and frequently changing groups, which would perhaps reveal the harmonic content of the example better than the tonal analysis given here.

It will be objected that no analysis of the present sort was in the mind of the composer when he wrote this piece. Although this objection applies to all music, since this type of analysis has never been in use before, let the piece be divided, in order to illuminate the viewpoint of the technique according to which it was written, into the sections into which it falls by the rules of the twelve-tone system. These sections are indicated by roman numerals, and bounded by dotted lines. In almost every one of them, all the twelve tones are conscientiously included, although obviously individual tones may be repeated. So far as I am able to judge this technique, group II seems to have been badly slighted, for it must get along without the tones $e_b$, $f$, $a_b$, and $b_b$. 
Melodic Analysis of the Upper Voice (the other moving parts can be dissected in similar fashion).

1. Degree-Progression
2. Step-Progression

Harmonic Analysis
3. Two-Voice Framework
4. Fluctuation
5. Degree-Progression
6. Tonality

*) The organ-point is disregarded in the analysis.
The strongly chordal design of the degree-progression is based upon the effort to organize chord-groups as closely as possible around a tonal center, while leaving the greatest freedom to the individual voices. The fact that the tones of the degree-progression (measures 9-13) form a broken chord of group VI results in a

le but very noticeable cadencing toward the B of measures 16. The tonal scheme shows the same effort. Here, too, a large number of tonal centers is chordally related, so that great activity details takes place against a smooth and gently restful back­

round. At three points in the example there are organ-points. The first and last of these are left out of the reckoning. If one includes in, the degree-progression becomes simpler, but the harmonic situation more complicated, while the harmonic construction is unchanged. In the second case (measures 9-12) the exclusion of stationary c simplifies the reckoning; and here, too, the harmonic picture is unchanged.
THE CRAFT OF MUSICAL COMPOSITION

by

PAUL HINDEMITH

BOOK II

Exercises in Two-part Writing

English Translation by

OTTO ORTMANN

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B. SCHOTT’S SÖHNE, MAINZ
PREFACE

In this book I follow the theoretical part (Book I) * of my textbook with the first eleven chapters of the practical part. They deal only with two-voice setting **, but this narrow field of work is treated here in a more detailed and thorough manner than has been the case in other books. Although the training in understanding and applying tonal phenomena, especially the harmonic, can be but insufficiently developed with the aid of only two voices, nevertheless the two-voice exercises, with their easily surveyed tone-material, with their limited possibilities of tonal motion and combination, give the best opportunity for understanding the hidden principles and activating forces of tone-setting itself. Let it not be said that it is too soon to acquaint a student, at this point of his ability, with the principles of tone-setting, since these are difficult to comprehend and are not on the surface. This is just the time to direct his attention to a broad perspective. Later on, his thinking and feeling are too readily entwined with the richness of the auditory material and the numerous rules for its use.

My experience has been that the early realization of these activating forces will easily prevent the formation of those “dead points” which one finds in the work of any advanced student. This frequently is not the case if, later, we have to go back to these necessary first principles. Only the teacher or student who, after an extended trial, is convinced of the weakness of the order which is here maintained could raise a valid objection. This, however, would not be possible for him, even after a thorough use of the present exercise book, for how could he, after these earlier exercises, give a final judgment on a similar procedure through the entire tonal domain! I ask him to trust my experience of many years, and to believe that nothing has been written in this book without trial and verification in actual instruction.

Until I can find time to complete the continuation of this book, with instruction in the higher, polyphonic art of tone-setting, those who desire to use the two-voice exercises in their teaching are thus forced to use them as complementing the usual instruction; or else, after working them

*English version in preparation.
**The German word *Satz*, which means composition, particularly in its more detailed and technical aspects (harmony, counterpoint, etc.) has been rendered throughout this volume by its English cognate: “setting”.—Translator.
through, to find a connection with the practice of harmony and counterpoint. This is entirely possible. When this work is completed, the present exercises will be found to have served as foundation for all settings. They address themselves to the beginner, from whom no knowledge of older methods is expected. It is, therefore, not necessary, before attacking the work-material here offered, to practice harmonic or contrapuntal studies. However, a thorough pre-schooling in the elementary theory of music and in the rudiments of ear-training is presupposed; in addition, complete clearness as to intervals and the structure of the simplest three- and more-voice chords must exist. In spite of a readily understandable presentation, and an easily surveyed order of procedure—each of the eleven chapters sets forth the particular material needed, and contains a detailed description of the work-procedure, with some model examples—a beginner would still find it difficult to labor through it without any help whatever.

The book counts on the explanatory activity of the teacher, who should adapt the material to the needs of the individual student. For the teacher the division into numbered rules and problems should in no sense be a hindrance in his work; instead he should find therein the challenge to create new work-material, as elaboration of that already presented. In this respect no limit is set to his creative gift. Should he prefer to instruct the pupil on the basis of traditional tone-setting methods, he will be able to use the technical helps here given as well as if he were to explore tonal domains which have not yet revealed themselves in any practical way to him or to his pupils. He will notice that he retains complete freedom in the forming of an independent style of writing (which is definitely not the case with the older methods); that he is in no way forced to move in a predetermined stylistic direction—a concern of which I heard frequently after the publication of the theoretical part (Volume I) of this work; but that, instead, he receives an aid which he can apply to the solution of technical and stylistic problems of any kind whatever. In this connection, a valuable aid can be found in the pre-study of the first volume, the theoretical part, especially if he desires to acquaint the pupil with the proofs of the statements made in the course of the work. This, however, is not absolutely necessary, since the main principles of the first volume, in so far as they directly affect the practical work, occur again in the description of the material and in the work-procedures of this exercise book, where they are adapted to other aims.

Paul Hindemith

Hindemith

Exercises in Two-part Writing
CHAPTER I

Construction of the Simplest One-Voice Melodic Patterns

The pupil connects a few tones to make a linear pattern in which the melodic element appears with the least possible admixture of metric and harmonic elements. In these very modest tone-successions he is to learn the effects of melody. For the time being the examples are practically free of all expression. The material with which he works is so scant, and the field of application is so narrow, that the results can be neither artistic nor impressive. These are purely laboratory studies, which do not occur in practical music as independent melodies because it is neither possible nor desirable to separate melodic lines constantly from the influence of rhythm and harmony. At the same time, these apparently very insignificant patterns must be considered the germ-cells of even the most complicated melodies.

In external appearance such melodies correspond approximately to the cantus firmi used in contrapuntal exercises. However, whereas the cantus firmus serves as a meagre pattern for the exercises of the beginner, and, in this form, has no significance for the later practical art of writing of the accomplished musician, the tone-successions in these exercises are constructed according to the most rigid demands of pure melody. And they are retained later—although in somewhat changed form—as support and basic form of all writing.

A. Work-Material

1. Our work-material consists of the twelve half-tones of the chromatic scale, which we use not merely in the single octave range given in Figure 1,

but also beginning at any desired pitch and extending throughout the ranges of the human voices. The limiting of work-material to the diatonic major or minor scale, or to the old church modes—as has been done in textbooks up to the present time—would, it is true, materially simplify
the exercises of the student in his first attempts at writing; but he would then have to pay a high price for this deceptive gain. Experience shows, again and again, how difficult it is for even the most talented and instinctively sure musicians to leave a beaten track which, though at first scarcely noticed, yet later markedly restricts the free, forward urge. But they must leave it in order to know all the manifold directions which to some extent the free, broad art of writing has always followed, and to some extent it has learned to follow in the last decades. Without a knowledge of these directions, we can scarcely imagine entering the innermost regions of artistic composition. The beginner, accordingly, shall make his first swimming attempts in the freely flowing stream of chromatic richness. This does not mean freedom in grouping the tones into daring clusters of auditory novelty. We shall, instead, begin our very first attempts within clearly marked borders, the narrowness of which exceeds the demands of even the most confirmed defenders of a strict academic cantus firmus style. In this elementary period, in which the tonal motion is severely restricted, the student notices chromaticism only to the extent that from any first tone a greater number of other tones is available than would be the case with the older instruction methods. But the greater choice need not trouble him—a series of rules will prevent this. He will neither be smothered by an overabundance of material nor be lost in an open sea. Only in the course of considerable advancement will he more and more freely enjoy the advantages offered by the chromatic tone-supply.

2. In the first exercises we consider metre and note values only in so far as change of tones and uniform progression within an exercise depend upon them. We shall use only whole notes, omitting metre signatures and bar-lines.

The whole note here serves for a tone of any desired duration, without metrical relationship. Within an exercise, all notes are given a uniform duration, a value which we shall take as approximately the time of two to three pulse-beats. At this tempo no single tone can separate itself from other tones by longer or shorter duration; it cannot become superordinated or subordinated; and we have an opportunity to sense and understand each tone and each tone-progression in its full significance. In such an arrangement rhythmic energy has the least possible influence on the pattern of the melody; it is restricted to fixing the boundaries among the various parts of the melody. Since an element as important as rhythm is thus ignored, it is obvious that dynamics and other aids to expression are entirely eliminated. They have no meaning for the essential progressions in sound and in motion with which we are exclusively concerned in these tonal settings.

3. The attention of the beginner will be so occupied with what happens in this unfamiliar field—which will considerably tax his reasoning—that it would be unwise to burden him with extraneous difficulties which do not affect the content of the present exercises. Every teacher knows the struggles which the learner undergoes in coping for the first time with the various clefs. Through wrong training we have arrived at a point where a C-clef (to say nothing of several C-clefs simultaneously used) offers a serious obstacle even to capable students. Deplorable and worthy of condemnation as this condition is, we must nevertheless take it into consideration. Accordingly, we shall write all two-part exercises in the two most familiar clefs: violin (treble) and bass, and shall reserve the use of the remaining clefs for later three-part writing.

4. We shall write the two-part exercises exclusively for pairs of the four voices: soprano, alto, tenor, and bass. Moreover, they should be written so that the student can sing them without difficulty. Female students, therefore, should write in the treble clef, for soprano and alto; male students, in the bass clef or in the tenor form of the treble clef (indicated with an 8). Not until later (beginning with Chapter II) are the students permitted to write for voices of other ranges than their own; but even then they should always concern themselves with the living sound, by utilizing the vocal abilities (mostly rather scant) of their classmates or those of the teacher; they should never merely write notes on paper. The exercises are to be sung without text, on “la-la” or some similar neutral syllable. Text is introduced into the work in only the last two chapters. The final proof of the value of what has been written is always determined by singing each exercise.

B. Work-Procedure

A melody consists of tone-steps and tone-skips, in so far as the purely melodic activity of the interval progression is concerned, apart from its rhythmic and harmonic contents. The pitch distance between two auditory points which embraces just the distance of a major or a minor second is
perceived as a tone-step; all pitch distances exceeding this, beginning with the minor third, are covered by means of skips. It is possible to construct highly contrasting melodic lines in which long extents of melody consist only of steps or only of skips. These, however, do not belong to the most desirable forms of melodic expression; instead, such forms are found rather in those instances in which steps and skips are combined. In such cases their rich tensional peculiarities are mixed in an intelligent manner, and unite in regard to form, sound, and content to produce a single total effect. This order, caused and developed by the inner nature of the single tone, and influenced by training, experience, and personal taste, rules even in the smallest, self-sufficient melodic patterns which we are about to construct. Attention to the following regulations will lead us toward this goal.

**RULE 1.**

The pitch range of any one voice of an exercise should embrace approximately one octave.

![Pitch Range Example](image)

The word “approximately” means that this range is not to be retained too conscientiously. When a larger range seems urgently necessary, the octave range may, as an exception, be extended. By restricting the pitch-range, we prevent the use of larger melodic curves, which, as valuable means of expression in the grand style, would tend to destroy the simple clarity to which our exercises are directed. This is most satisfactory when the least amount of expression is introduced. Moreover, the limited pitch-range assures the possibility of singing by the pupil.

**RULE 2.**

No binding regulation can be given for the length of the exercises. The student will notice, however, that consideration of all the given regulations will itself insure exercises of approximately uniform length. Fewer than seven tones can scarcely awaken the feeling of melodic development; with double this number the frequently necessary return to a tone already present would result in a certain monotony.

**RULE 3.**

The first note is the same as the last note. By returning at the end to the tone of beginning, we give the hearer the feeling of formal and tonal rounding-off and completeness.

**RULE 4.**

The direction of melodic motion should be changed after four tones, at the most, in order to avoid too pronounced an ascent or descent of the tone-line.

**RULE 5.**

Only the tones here given may precede the final tone:
- its second (major or minor) from below or above,
- its third (major or minor) from above,
- its fourth from below,
- its fifth from above.

All others weaken its closing effect.

---

**EXERCISE 1**

Construct in whole notes, without bar-lines, several melodies which are restricted to the given regulations and which you can sing with difficulty. What is difficult to sing, cannot be correct! Keep on improving your work until you are thoroughly satisfied with it.

The student should train himself never to proceed until he has fully understood all that serves as preparation for the exercise, and until he has solved the problem itself.

---

**EXERCISE 2**

See if the results of Exercise 1 reveal points which are touched upon in the following rules, and, if so, remember these points.

---
Our melodies should form their curves in even, regular, quiet progression. This demands that all tonal sub-grouping within a melody which might retard the steady flow should be eliminated. If, for example, a tone or a tone-group were given emphasis through its duration value or through its close connection with other tones, such an accent in the tonal environment would disturb the even melodic flow. Such devices are intentionally used in styles of writing less restricted than the one here employed.

The following instructions apply to such disturbing factors:

**RULE 6.**

Immediate repetition of a tone is prohibited.

![Diagram 1](image1)

If a tone sounds immediately a second time, without relief from other intervening tones, its position is strengthened in relation to the other tones. Such emphasis hinders the flow of the melody.

Even the return to a tone after the interposition of a different tone tends to base the melody too strongly on the tone that is repeated.

![Diagram 2](image2)

The group: tone—auxiliary-tone—tone is therefore to be avoided in the earliest exercises. The danger of too strong a grouping around a tone appearing several times naturally diminishes as the tones between a tone and its repetition increase in number.

**RULE 7.**

Avoid broken chords. Several successive tones must not form a tone-group which can be perceived as a broken triad.

![Diagram 3](image3)

Such tone-groups would, through their compactness, focus the attention on the chord unit and would thus devaluate the surrounding tones. Steady melodic progression also would be disturbed.

With only two tones the chord feeling is not definitely awakened, although the interval of a major or a minor third already clearly suggests it. At least three tones are necessary to decide the exact chord. The most common examples of broken chords are those containing an augmented sixth or a diminished fifth; these, especially, are to be avoided.

![Diagram 4](image4)

e designation tritone, strictly speaking, applies only to the augmented sixth (embracing three successive whole steps); for the diminished fifth there is no special term. The word tritone, for the sake of simplicity, I use to include intervals.

Groups such as those in Figure 8a, consisting of three tones, are not considered triads in the sense of our musical terminology. Later on (in the complicated three-voice setting) we shall use them as independent combinations, but they do not meet the conditions demanded at the beginning of Rule 7 ("broken triad" in its narrow sense), so they may be used in their broken (melodic) form:

![Diagram 5](image5)

The chordal effect of broken triads and of tritone chords can be mutually weakened by the use of intervening tones making seconds with the chord tones; but it cannot be entirely eliminated by this means.

![Diagram 6](image6)

I cannot give an exact rule which would enable the student to define, unequivocally, the disturbing or the favorable character of such tone-chord figures. In judging such tone-groups he must rely on his ear, so that at other times. If, in spite of the insertion, the ear hears the grouping as a retardation of the melodic flow, the grouping should be avoided. If, on the other hand, the melodic urge of a tone-line is sufficiently strong to carry along the melody and thus overcome the chord
figure with its intervening tones, such figures (though in other cases they are of doubtful value) may then be used.

RULE 8.

Avoid sequences (repetition of the same note-patterns at different pitch levels).

Sequences also create melodic units. Even when the first pattern of a sequence is constructed entirely in accordance with the rules, its repetition at a higher or lower pitch-level will emphasize for the listener the pattern rather than the separate tones. The smallest of all sequences, the repetition of a two-tone pattern at another pitch, is not disturbing so long as it is not repeated more than once, and so long as it does not give the exercise an obvious metrical feeling. Frequently, however, a sequence by inversion is disturbing, especially when the sequential pattern contains a skip.

When I say “frequently” this means that even in these smallest exercises rules and regulations are not to be applied without thought. There will always be instances in which taste will decide between two equally correct solutions; in certain instances, even, preference may be given to a not entirely correct form over a strictly correct form. The student will do well, however, not to rely too often on this statement! He will notice, in any case, that the rules and instructions are to restrict him only to the extent to which they are needed to reach the exactness and clearness which are constantly demanded. No rule exists which functions with uniform validity throughout a course of study; instead, it must always be adapted to the particular demands of a specific case. The directions given are, therefore, in the following exercises, already broadened according to need; they will at times be replaced by others, or even declared simply invalid.

The preceding rules guarantee, to a certain degree, the smooth flow of the melody by prohibiting the use of retarding tone-groups. However, they eliminate the opposite danger of an inappropriate acceleration of by the use of too striking skips.

RULE 9.

skips than that of a fifth (ascending or descending) may not be either skips of sixths and sevenths create group-units—since the following are felt as a kind of satisfying goal (resolution) thus cause sixths and sevenths to appear as subordinate members of a com- tone-succession

:ord patterns are formed (covering greater duration distances) may be interrupted by other tones, but the tones of which, therefor clearly to belong together.

noticed in Rule 7 that such “suspended” chord patterns cannot be eliminated if we do not wish to restrict too much the development of smoothly flowing melodic lines. If they are or must be employed, the less obvious forms should be used; their conspicuousness increases with the skips contained within the group. notation used in examples such as 14b and c, should cause no con the notation itself does not indicate a chord; the sound, however, per- to hear a sixth chord (b) and a six-four chord (c). We must always be sound, just as in language we decide according to the spoken word than to the orthography of the written symbol. But this does not mean correct notation should be neglected! This has its own logic which must cely followed in writing. As to the sound, however, the ear is the sole not the eye.

illy, through the use of such large intervals our melody becomes too ted and, as a result, acquires a too pronounced affective character-hich conflicts with the desired normal flow.

leaps beyond an octave violate Rule 1. Even the other-less skip of a fifth can inject an unpleasant sudden forward into an otherwise smoothly flowing melody. It is thus advisable to
soften the effect of such an interval by allowing not more than one tone in the same direction to follow it, after which the pitch direction should change.

By this procedure, however, we almost invariably produce one of the dispersed broken-chord patterns which we have discussed, but which may be used here in order to avoid more conspicuous errors of construction.

RULE 10.

One skip may not be followed by a second skip in the same direction. Two such leaps, following each other, likewise produce self-contained tone-groups. When three tones appear in a single pitch direction and embrace two skips either they violate Rule 7 because they themselves form a chord unit (broken chord)

or the tone following them combines with the first two tones to form a chord which cannot fail to be heard.

Tone-successions consisting of a tone, its octave, and a skip between, are likewise in this connection to be considered chords.

Skips in the same direction tend to restrict a free linear development even if they are delayed by a tone between.

Formations such as these

cannot be avoided, but they should be used as sparingly as possible. The succession of two thirds, in the same direction, with a tone between,
RULE 12.

Avoid augmented and diminished intervals. If, after an augmented or a diminished interval, the third tone is taken by skip, a chord group will result

or the tone-succession will contain a forceful and easily recognized interval (indicated in Figures 21 and 22 by a bracket) to which the remaining tone then acts as subordinated auxiliary tone.

The same thing happens when the third tone is taken stepwise after the augmented or diminished interval.

The binding force of the augmented and of the diminished intervals extends not only to the tones which are immediately involved in such a progression. The most striking interval among them, the tritone, exercises its binding force over longer extents. It is noticeable after even four or five tones in passages that progress in small intervals.

Although in most cases such successions are automatically excluded in view of the preceding prohibitions, nevertheless it is advisable at the beginning to become thoroughly acquainted with the peculiar effect of the tritone interval. The unifying effect of the tritone can be overcome by adding a tone to the tritone figure which makes with the preceding or following tone an interval of a perfect fifth or of a perfect fourth. These strong skips are the safest and most immediately effective means of avoiding the tritone. In patterns such as these

the tritone is almost entirely without effect. We may argue that in many cases the diminished or augmented intervals can be avoided simply by changing the spelling.

The following rule, however, will prevent this attempt.

RULE 13.

Chromaticism is inappropriate. By chromaticism we here understand a succession of at least three tones which are linked by half-step intervals; that is to say, two minor-second steps in immediate succession.

Even with but two tones—a single half-tone step—chromaticism can creep in: when the note pattern shows a tone and its alteration by a # or a b.

Do we not here grant notation a right which we have just (page 9) denied it? No, for it is here not at all a question of notation. We merely are using the orthographic picture as an entirely extraneous aid. It indicates, in the written chromatic alteration of a tone, that an incorrect group-formation exists with the preceding or following notes, of which the chromatically written progression is but a part. Accordingly, the incorrect leading here too is first to be noticed from the auditory impression; in addition to this we accept the warning cry of the notation as an additional, welcome aid.

Chromatic progressions bind the tones too closely together and do not lend themselves to free linear development, which we here require of our exercises. Moreover, a chromatic progression separated by single tones is not permitted.
With more than two intervening tones it is possible that chromatic steps are no longer disturbing; with three or more intervening tones they are almost always acceptable, so long as their use does not produce other errors.

EXERCISE 5

Determine to what extent the melodies written for Exercise 4 conflict with the new rules. Improve the exercises.

C. Model Examples

EXAMPLE 1.

This example illustrates, in the smallest frame, as much melodic development as can be obtained from our limited building material. It frees itself from the first tone in an increasing gradation, steers goal-conscious to the climax, and then rounds out, with the final skip of a fifth, to a complete bit of music—in so far as we can apply the word “music” to this purely intellectually constructed pattern. The close restriction demanded by so many rules naturally does not permit invention to come to its rightful place; the student will notice, however, in the course of his work that even in this narrowest frame and even by following all regulations, attractive and less attractive solutions are possible. Accordingly, there exists a small, scarcely noticeable place for the development of personal expression, from which, later, accessible paths can be taken into free composition, once the building materials have been increased and the restrictions have been relaxed.

EXAMPLE 2.

This is a more complicated form. The upward leap of a fifth at the beginning is later counterbalanced by that of the descending fifth a\(^1\)-d\(^1\); at the middle, balance is maintained by the repeated a\(^1\) and its supporting ones at the interval of a second.

EXAMPLE 3.

This is only moderately interesting in its pyramid-like structure, in which the single ascent and descent seem more banal on account of the ascending second f-g and its later inversion g-f. A little improvement results if e-f is substituted for f-g:

By this change the chromatic move e-e\(_b\) results, which is not disturbing, however, because too many other tones are between; as a matter of fact, it adds a bit of spice to the meagre fare.

EXAMPLE 4.

The careful preparation of the climax through the two tones at the beginning, and the strong descending impulse, lend a particular charm to this bit, which before the close is augmented by the lowering of the earlier a to e\(_b\). The change of c to c\# would add nothing, for the tones c\#-e-f-b\(_b\) would be heard as a b\(_b\) minor triad, with e as neighboring tone to f, and the entire melody would then be fettered to this chord mass.

Here this disadvantage is smoothed out, at the expense of tension; the latter is far less marked than in the first version (Figure 33).
This solution is poor because a chord is formed of the tones e–f#–a
(with neighboring tone b) which, on account of its tritone e–f# is especially marked. The following version would be better.

The effect of this example is about as good as that of Example 33. Note the use of chromaticism. At the beginning we have, in ascending, an a♭; at the close we have, in descending, an a. This is peculiar in so far as ascending progressions normally use the upward-striving tones, and descending progressions use the lowered tones, in keeping with their descending tendency.

---

EXERCISE 6

Construct melodies similar to the preceding examples, taking into consideration all rules thus far given. After writing them, sing them, and in the most detailed way study them as to their form and the impression they make.

A condensed summary of rules governing these exercises is the following:
1. Pitch range about an octave;
2. Length not less than seven notes;
3. First and last tones the same;
4. Pitch direction to be changed after four tones at the most;
5. Only certain tones may precede the final tone;
6. No tone-repetition;
7. No broken chords;
8. No sequences;
9. No skip larger than a fifth;
10. No more than one skip in the same direction;
11. No scale-passages;
12. No augmented or diminished progressions;
13. No chromaticism.

Attention must be given also to the location of the highest and the lowest points, which on account of their emphasis through pitch ex-
tremes can influence an otherwise correct setting, favorably or unfavorably.

I must admit that only narrow paths, difficult to find, can lead to the goal demanded in this exercise. The student who finds these paths and becomes better acquainted with the unyielding material, has already gained much. First of all he learns to obtain the best possible effect with the least material—a principle of work which can be carried over even into the most remote heights of composition itself. He learns also, in these early attempts at writing, how firm and resistant, and, at the same time, how pliable and elastic, tones are. He notices in which direction the melodic energy of tone-combinations extends and attempts to guide this to whatever point he desires; but he sees, also, how little a single element suffices when this is not supported by the other elements. Accordingly, the main result of this first chapter is, perhaps, that we learn and profit more from the notes which may not be written on account of the many restrictions than from the few which, finally, we put on paper.
CHAPTER II

Beginning of Two-Voice Setting *

One-voice melodies, constructed according to the rules of Chapter I, will now be supplied with a second voice. Up to this point our problem has consisted simply in training melodic thinking and hearing. In Chapter II, in contrast, we aim for the construction of harmonic progressions in their simplest, clearest, and most definite forms. We shall start from melodic construction, which, to some extent, we have learned through our work with monodic lines in Chapter I, and which consequently serves as a firmly grounded form of tonal activity within the narrow limits to which, for the time being, we must adhere. Using this as a guide line, we feel our way cautiously, by small steps, into the new field. We still do without the rhythmic element in our new ventures.

Like Chapter I, Chapter II resembles an exercise of patience rather than of musical work. The solution of the following problems, which are markedly restrictive despite their incomparably richer building material, demands patience and good will; later on, greater freedom will be permitted; the pleasure then derived will be proportionately keener and will compensate for much earlier trouble.

A. Work-Material

1. The tone-equipment of Chapter I and the notation rules (whole tones, no bar-lines) hold also for this chapter. We use two staves with different clefs, which are adapted respectively to the pitch levels used. The one voice is written as before, so that the pupil can sing it himself without difficulty; the other voice is to be written so as to be sung with equal ease by a second singer (another student or teacher).

2. Up to this point we have used intervals entirely as tone-progressions, the temporal succession of two single tones. From now on, we shall employ them as units of sound, composed of two simultaneous tones. We shall use only those intervals which lend themselves to two-voice treatment without much difficulty. Within the confines of an octave, these are: unison, octave, fifth, fourth, major and minor third, major and minor sixth. Intervals exceeding the octave are considered the equivalents of their counterparts within the octave: the tenth counts as a third, the eleventh as a fourth, the twelfth as a fifth. All other intervals are not available to us for the present, because their use demands knowledge which we can gain only as the work progresses.

It is too cumbersome to utilize always the full names of the intervals in mentioning them—major third, augmented fifth, etc. Accordingly, in the future we shall use the numbers 1 to 8, which, following the model of the piano keys, stand for the intervals within the octave c-c' which are formed by c and the white keys above it, and any desired transpositions of these intervals (1 = unison, 2 = major second, 3 = major third, ..., 8 = octave).

The intervals which lie between these, corresponding to those formed by c with the black keys, are represented by two figures separated by an oblique line, slanting in the opposite direction to that of a fraction:

\[ \frac{1}{2} \] therefore indicates the interval between 1 (unison) and 2 (major second), namely the augmented prime as well as the minor second. \( \frac{2}{3} \) indicates the augmented second and the minor third; \( \frac{4}{5} \) the augmented fourth and the diminished fifth; \( \frac{6}{5} \), the augmented fifth and the minor sixth; \( \frac{7}{6} \), the augmented sixth and the minor seventh. When necessary the number system can be continued beyond the octave (\( \frac{10}{9} \); 9; \( \frac{12}{10} \); 10 . . . ).

The number notation given indicates broken intervals (two tones in succession); that is, it indicates a tone-progression.

This, however, still does not give us a symbol for the sounding together
to be slightly relaxed. Accordingly, in the 2d voice the following may occur:

a) Broken triads, but not broken tritone chords or augmented triads. This relaxes Rule 10 somewhat: two successive skips in the same direction may occur if they make some permitted form of a broken chord.

b) Skips up to a sixth and an octave, ascending or descending. After a skip of a fifth, several other tones may be used stepwise in the same direction. (But be careful!) In applying these liberties the restrictions of Rule 10 must be observed governing skips in the same direction with inserted tones.

c) More than two successive seconds progressing stepwise in the same direction.

d) Auxiliary tones (for instance: \(c-bb-c; e-g\#-e\)).

e) In addition to the approaches to the last tone permitted by Rule 5, also the skip of a fifth from below and that of a fourth from above.

f) The first and last tone of the 2d voice, if this be the upper voice, need not be the same; but when it is the lower voice, Rule 3 applies.

In addition, the following rules still hold for the 2d voice:

1. (Pitch range about an octave)
2. (No tone-repetitions)
3. (No sequences)
4. (No two successive skips in the same direction; but see Rule 15a1)
5. (No augmented or diminished progressions)
6. (No chromaticism).

These rules teach us about the construction of each of the two voices, but they tell us nothing about their combined effect. It is rather obvious that two independent things, linked in a limited space, whether they be living beings, physical objects, or moving tone-lines, cannot move with the same freedom as a single thing alone using the entire space without restriction. The constantly varying new claim upon the available space, as well as the attraction and repulsion existing between the two moving units, demand carefully considered rules of interrelationship if an intelligible and convincing progression is to result. Since, in addition to the characteristics of the conflict for room to move around in and the mutual relationship encountered in such two-voice tone-lines, the picture is further enriched by the constant shift of the centre of gravity between intervals with root below and their inversions, a large number of rules is necessary to bring such tone-setting into equilibrium.

RULE 16.

Crossing of voices is prohibited; it destroys the perception of the actual two-voice setting.

RULE 17.

The distance between the two voices is determined:

a) according to the pitch level of the two voices used. For tessituras of small pitch difference (soprano and contralto, contralto and tenor, tenor and bass) the interval 10 should usually serve as the widest distance; for voices further removed (soprano and tenor, alto and bass, soprano and bass) a correspondingly wider pitch range may be used.

b) according to the nature of the model itself. If this moves along quiet lines of relatively little activity, the two voices may move more closely together. If the pitch range of the model is wide, the 2d voice will naturally remain somewhat further away in order that the two voices may not interfere.

RULE 18.

The first and the last interval of the two-voice setting, must be either \(1\) or \(8\) or an interval with root below (\(5\), \(3\), \(6\)).

RULE 19.

The use of intervals with root above demands some care. They may not be used for beginning and ending, and they are ineffective at points of marked importance or prominence.

RULE 20.

If the last tone of the model is approached from a fifth above or a fourth below, the 2d voice must move into its last tone by a \(1/2\) or a 2 progression.
Conversely, the 2d voice may use the final progressions given in Rule 15e only if the model moves into the last tone by a 3\(^{\text{rd}}\) or a 2 progression.

If we are certain that a 2 or a 3\(^{\text{rd}}\) step may be used in the 2d voice between the next-to-the-last and the last tone, then the closing tone of the model may be approached by a skip of a fourth from above or by the skip of a fifth, a major third, or a minor third from below. (Compare Rule 5.) Condensed and in a simpler form: If one of the two voices reaches its final tone by skip, the other voice must reach its final tone by step.

We shall begin with exercises in which the 2d voice lies above the model; later the reverse procedure will be used.

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**EXERCISE 8**

Complete the 2d voices of the following examples according to the given regulations.

---

**RULE 21.**

Care should be taken with triad or tritone-chord formations the tones of which are distributed among the four tones of two successive intervals.
Broken, more complicated tetrads such as

\[
\begin{array}{c}
\text{\textbackslash{}textbackslash{}textbackslash{}textbackslash{}textbackslash{}textbackslash{}
\end{array}
\]

do not count as broken seventh-chords and may, therefore, be used with impunity.

**RULE 22.**

The two voices may not skip in the same direction at the same time unless it be in one of the chord formations previously mentioned as conditionally permitted.

**RULE 23.**

Cross-relations must be avoided:

These are nothing but octave transpositions of chromatic progressions, and, accordingly, are entirely governed by the rule forbidding chromaticism (Chapter I, Rule 13); this holds also when other tones are interspersed which simply delay the chromatic or cross-relation effect.

**RULE 24.**

Parallels of \(1 + 1\), \(3 + 3\), \(5 + 5\), \(7 + 7\), and \(4 + 4\) are prohibited.

The successions \(4 + 4\) and \(5 + 5\) completely destroy dual-voicing; \(8 + 8\) and \(6 + 6\) are voice combinations which have harmonic value, to be sure, but represent only thickening and coloring of a single melodic line. The successions \(4 + 5\) and \(3 + 1\) are disguised parallel unisons and are always forbidden.

**RULE 25.**

Parallel major thirds \(3 + 3\) and minor sixths \(5\) are permitted when the two voices move in half-steps.

These cannot disturb the tonal setting so long as other errors are not made.

All other progressions (whole-step or skip) major third and minor sixth parallels are forbidden. They produce chordal formations through the tritone chord formed among their tones which cannot be made inaudible, although an added fourth tone does take away a part of the characteristic quality of the tritone.

Cross-relations (in addition to which the simultaneous skip violates Rule 22).

Parallel minor thirds \(5\) and major sixths \(5\) are not objectionable and are therefore permitted where their use does not involve an infraction of other rules.
RULE 26.

Besides the open unison and octave parallels, so-called covered octaves and unisons are prohibited. They result when the two voices move in the same direction from another interval into an octave or unison. These progressions create the impression of reckless forward pitching toward a goal and to that extent disturb the steady movement of the passage. As closing formulae, progressions in the same direction into the closing interval (or ) are freely admitted, because they lend an effective harmonic support to the formal urge toward the end. But even in such cases progressions from an interval smaller than an octave into an octave, if they move from lower to higher pitches, are of indefinite effect and are, therefore, to be avoided.

RULE 27.

Motion in the same direction into a fifth or a fourth (forming covered fifths and fourths) is prohibited when the progression is from an interval smaller than the goal interval. (If, instead of a fifth or a fourth, an eleventh (11) or a twelfth (12) is used, the prohibition holds also for these octave transpositions of the intervals.)

This rule, however, applies only to ascending progressions; covered fifths and fourths resulting from descending progressions are not objectionable.

RULE 28.

The highest and the lowest tones of one voice should not, if possible, occur at the same point or points at which they occur in the other voice, in order that the tension in both melodies toward these points of emphasis shall not disturb the independence of melodic progression in the two voices.

EXERCISE 9

Review the examples of Exercise 8, to see if the added tones follow the preceding rules. Improve the exercises if and where necessary.

If we write the added melody as lower voice instead of writing it above the model, as we have thus far done, the 2d voice receives a somewhat different significance, and, at times, also a slightly altered appearance. (See Rule 15, e and f.) For now the 2d voice, as lower melody, must support the tonal structure. It changes from a more or less ornamental and complementary addition into a structural part, upon whose stability and value the construction of the entire exercise depends.

The model, on the other hand, loses a little of its original importance. It is true that our rules are so formulated that they assign practically equal movement and independence to both voices (a condition which cannot be maintained in three-voice and more-voice settings); nevertheless the difference in volume or weight between high and low tones and the resulting difference between the sound of upper and lower voices are clearly discernible in even our simplest two-voice settings.

EXERCISE 10

Find all possible tones which may be set, in the 2d voice, against the first tone of each of the following three model fragments:
The 2d voices should be used both as upper and as lower voices. After this, continue the 2d voices with the remaining three tones of the models. (This will materially reduce the possibilities of combination with the first tones, on account of the voice-leading of the models.)

---

**EXERCISE 11**

Complete the 2d voices in the following exercises, 60 a–f.

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Add a 2d voice to these examples, first as lower voice. Then transpose the models to a practicable pitch and invent an upper voice for them.

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**EXERCISE 12**

Add a 2d voice to these examples, first as lower voice. Then transpose the models to a practicable pitch and invent an upper voice for them.

---

**EXERCISE 13**

Take the results of Exercise 6 of Chapter I, in so far as they are acceptable, and add to each an upper and then a lower voice.

This procedure will show that only those melody models submit readily to the two-voice treatment, which, although they utilize the scope permitted by the rules, yet do not do so to the fullest degree. The augmented, diminished, and chromatic leadings, especially, which are conditionally permitted by Rules 12 and 13 of Chapter I and whose effect may last over even fairly long passages, can often force the 2d voice into a constricted area, sometimes even making impossible a two-voice treatment according to the given rules. For in these exercises, as well as in mathematical problems in general, solutions may be found which leave a remainder, and from these the student can learn at least as much as from those which he can solve completely. Above all, the student will realize how the simultaneous progression of several voices reacts upon the construction of a melody itself, and to what degree a single melody of a multi-voiced texture must adapt itself to the other melodies.

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**C. Model Examples**

The following examples will show how one of the melodies taken from the models of Chapter I can be arranged for two voices in various ways. The model is first used as upper voice; then as lower voice, in which case it carries the tonal structure.

**EXAMPLE 1.**

The indicated chord formation could be avoided if the $d'$ were substituted for the $b\flat$. But then we should be using the $d'$ four times in the lower voice; whereas, otherwise the $b\flat$ occurs but three times. In either case the lower voice is barren. Beginning with the lower third in this case prevents a more attractive development. We cannot begin with the major third ($d\flat$) because it forms a cross-relation with the third tone of the model.
EXAMPLE 2.

This solution is better even if it is not entirely convincing. The two voices lead a sort of quarrelsome existence together.

EXAMPLE 3.

The cross-relation $b - b^1$ is not disturbing because the two intervening tones do not permit this to be noticed, except faintly. If, nevertheless, we wish to avoid it, we have merely to lower the $e^1$ to $e^1b^1$ and the $b$ to $bb$. When the indicated four-toned chord formation is eliminated, the insertion of the corresponding place in Figure 62 produces a much smoother and richer solution.

EXAMPLE 4.

The upper voice blends so well with the model that it has not at all the effect of a mere addition. The impression is given, far more, that both voices have been invented simultaneously. This very desirable end cannot always be reached under our strict working conditions; but in these exercises beauty (although most desirable) is less important than consistency of thought and control of the material.

EXAMPLE 5.

The two descents from the $c^2$ lame the free movement of the upper voice; $a^1$ at the beginning would be better.

EXAMPLE 6.

The parallel octaves $g - g^1$ to $a - a^1$, interrupted by another interval ($\mathfrak{c}$) are not disturbing, since we assume a very broad tempo. Nevertheless, they can be avoided if we introduce the four closing tones of Figure 66. The higher voice thus receives a more attractive upward swing. Moreover, the indicated chord formation is eliminated.

EXERCISE 14

As a check on the problem, in the light of the experience thus far gained, invent several additional melody models and add upper or lower voices to them.
A summary of the important regulations for such two-voice writing is the following:

Rule 16: no crossing of voices;
Rule 17: pitch-distance determined by the voices used;
Rule 18: the first and the last interval must have their lower tones as roots;
Rule 19: intervals with upper tone as root must be used carefully;
Rule 20: as a close, a skip in one voice requires a half-step or a whole-step progression in the other voice;
Rule 21: no chord-formations of tritone chords or augmented triads; no interchange of intervals;
Rule 22: no simultaneous leaps in the same direction;
Rule 23: no cross-relations;
Rule 24: no unison, octave, fifth or fourth parallels;
Rule 25: parallel major thirds or minor sixths only with half-step progressions;
Rule 26: no covered unisons or octaves;
Rule 27: no covered fifths or fourths from smaller intervals in an ascending direction;
Rule 28: no simultaneous highest or lowest pitch points.

CHAPTER III

Elaborated Melody

We now turn our attention again to melodic activities. As a basis for the following exercises we shall take the firm structure of the two-voice exercises worked out in the preceding chapter. The linearities of these are bound by the harmonies developing between them. We give melodic life to the two-voice examples, note against note, by treating the added voices rhythmically and working them into a metric scheme. Although here too, we are bound by definite restrictions, we have nevertheless outgrown the almost entirely mechanical setting of tones of the first two chapters. We can now at least let our fancy have play to the point of creating patterns which, in spite of their meagre material, already have some appreciative appeal and sometimes function even as practically useful music.

A. Work-Material

1. Two-voice settings as they have been produced in Chapter II, or as they can be written according to the given rules.

2. Whole notes of indefinite duration now no longer suffice. Our new melodies should not be judged as the earlier models were judged, moving without expression; instead, within the still restricted limits they should move as expressive bits of musical writing, alive and free. In order to lend them this necessary motion all note-values are available. In this broad field of metric freedom, the student will do well to follow only the easier procedures; otherwise his work will become needlessly difficult. The combining of extreme lengths and brevities, the interplay of duple and triple note-values (\(\frac{3}{4}\) against \(\frac{2}{4}\), etc.) will give the student but little help in understanding melodic flow; accordingly, he should use tone-groups which are simpler and more easily comprehended.

3. The tone-groups with rhythm, through the various lengths of their individual tones, also lend various agogic values to these tones. We sense the difference between accented and unaccented tones. Out of the pure
time demarcation has grown a distribution of values according to measure rhythm.

The sign which tells us about the position of accented and unaccented tones is the bar-line. By using bar-lines we also obtain definite metres. We can utilize all typical metrical signatures \( \frac{3}{4}, \frac{5}{8}, \frac{7}{8}, \cdot \cdot \cdot \) but here, too, the student will soon realize that he can gain more by using the simple duple or triple metres than by worrying along with the more "interesting" combined metres \( \frac{3}{8}, \frac{5}{8}, \cdot \cdot \cdot \), or the subdivided metres \( \frac{5}{2}, \frac{15}{8}, \cdot \cdot \cdot \). These demand much effort and time. The same holds for a change in the metre; this may be used. However, what we express in these exercises can almost always be said as well, or even better, without the change.

4. Note-values and metric division require further that we decide on the tempi of our little compositions. From the very beginning we shall invent the melodies with a definite character or mood and indicate whether they are to be taken at a slow, a moderate, or a rapid tempo. In the preceding exercises the tempo could not exert any differentiating influence; we intentionally prevented any retarding or accelerating tendency through the prohibitions against tonal groups and skipping melodies, and through the rule to use only tones of equal duration.

In the future we shall have to consider the changes in importance which tone-groups undergo with a change in tempo. A slow tempo gives the ear time to perceive and interpret each detail of the setting; whereas a more rapid tempo frequently makes impossible the perception of the details of its organization. Thus a cursory reaction may result which occasionally deviates widely from the first mentioned reaction to each detail.

5. The two-voice sound units, described at the beginning of Chapter II, would be but crude harmonic work-material for our gradually more refined technique, if they did not contain significant characteristics other than the inversions of their two components and the root-function of one of their tones—things we have already discussed. We have not yet considered the characteristic which alone enables us so to play off the intervals, one against the other, that a harmonic activity results which is based upon heaviness and lightness, upon percussion and repercussion, upon tension and release. It is their particular place in a scale of values that assures them the most varied application.

Of those intervals possible within the span of an octave, \( \frac{3}{2} \) and \( 6 \) are so close in value to a single tone that they can scarcely be distinguished from the latter. They stand above and apart from the series of dual-toned intervals beginning with \( \frac{5}{2} \). After this, follow the remaining five intervals used as work-material in Chapter II: \( \frac{3}{4}, \frac{5}{8}, \frac{7}{8}, \cdot \cdot \cdot \), in the order of decreasing value, as a complete group of the most valuable intervals. These six intervals from \( \frac{5}{2} \) to \( \frac{3}{2} \) will be designated collectively as "Group A."

"Group B" follows, with an interval scale of values which thus far we have not been able to use; the order of which, however, we must now note for future work: \( \frac{5}{2}, \frac{3}{2}, \frac{7}{8}, \frac{3}{4}, \frac{5}{8}, \cdot \cdot \cdot \). At the extreme end of this series, separated from the other intervals in the same way in which the \( \frac{3}{4} \) and \( \frac{7}{8} \) stand apart from Group A, is the tritone \( \frac{5}{2} \), the diminished fifth or augmented fourth. This frequently mentioned interval contains definite characteristics which we shall learn to know in detail as our work progresses. The even gradation of this series of decreasing values is somewhat disturbed, however, by the fact—already known to us—that intervals with lower root have a different value from that of intervals with upper root. This fact causes a greater decrease in value from \( \frac{3}{4} \) to \( \frac{5}{2} \) than we should expect from the harmonic aspect alone. \( \frac{3}{4} \), a strong interval with root below appears in full strength; \( \frac{5}{2} \), on account of its root being above, loses some of its expected strength. \( \frac{7}{8} \), again, stands unweakened at its place in the scale of values, while the next interval \( \frac{5}{2} \), like \( \frac{3}{4} \), does not attain its full expected force. If we conceive the decrease in interval value from \( \cdot \cdot \cdot \) to \( \cdot \cdot \cdot \) as represented by a straight line descending obliquely from left to right, \( \cdot \cdot \cdot \), \( \cdot \cdot \cdot \), \( \cdot \cdot \cdot \), and \( \cdot \cdot \cdot \) fall at their proper points, and the remaining intervals, \( \cdot \cdot \cdot \), \( \cdot \cdot \cdot \), \( \cdot \cdot \cdot \), and \( \cdot \cdot \cdot \) fall slightly below their assigned places in the line.

[ 36 ]
The general descent thus remains, but follows a broken course: the descent from a "good" to the next "inverted" interval is so marked that the following step, from the inverted to the next good interval, seems almost horizontal. That is to say, an inverted interval has but very little greater value than the following strong interval with root below.

As a dry statement, without practical application, all this seems merely clever captiousness. However, we shall soon realize what influence these determinations have on the style of writing.

B. Work-Procedure

We shall approach a more musical style by moving at least the added voice of our examples in a more melodic manner than the model. (Heretofore the two voices of our examples circled about each other steadily, definitely, and unconcerned, in almost starlike detachment.) In the realm of intervals just described as usable, there exists an effective means for such greater motion. We have merely to add, in the second voice, two or more tones against a single tone of the model melody, instead of restricting ourselves to note against note, as in the preceding chapter. These added tones follow the same rules as the single tone, especially in their harmonic relation to the tones of the model. They should, in connection with the given melody, produce only intervals of Group A, regardless of whether the connections of one tone of the second voice to the next occur by step or by skip. For the progression by skip an important rule follows:

RULE 29.

Skips may be taken from only such tones, or into only such tones, as make intervals of Group A with the tones of the other voice. (Compare also Rule 22!)

Another rule is important because it prevents a restlessness from usurping the field, which readily creeps into the exercises through their enriched motion:

RULE 30.

With freely moving melodies care must be taken to avoid any clearly noticeable seventh or ninth intervals along the melodic line:

![Image](image.png)

which, even if they are interspersed with other tones, would create a too great tension for these modest tone lines. (Compare Rule 15b.) Exceptions to this rule are those instances in which seventh or ninth intervals are clearly perceived as sixths and octaves, respectively, the entrance of which is intentionally obscured by the neighboring, delaying tones.

We may choose the duration values of the added tones in the second melody as we wish. However, in order not to overload the exercises with tones, we shall restrict their number to from three to five in each measure. Each note of the model fills an entire measure, according to the metre signature chosen (\( \text{\textbullet}_1 \text{\textbullet}_1 \text{\textbullet}_1 \text{\textbullet}_1 \text{\textbullet}_1 \text{\textbullet}_1 \)), and the notes are separated by bar-lines. In the second voice the original tone must always be clearly recognizable. It forms also the main tone of the rhythmically and melodically enriched measure, and in this way it appears either as first tone in a measure or as the tone of longest duration in the measure. It may happen, however, that in the curve of melodic progression such a tone is eclipsed by a tone of higher pitch or by one otherwise prominent through value or position. This is permissible so long as the setting otherwise follows all rules.

EXERCISE 15

Select several of the two-voice settings of Chapter II and rework their added voices into more lively, active melodies, according to the following illustration:
The main constituent of such melodies is the broken triad. This adds a strong activating impulse to the stiff melody lines, but at the same time also binds rapidly moving tone-groups of short duration into harmonic units.

The characteristic determinant of melodic progression, the step of a second, can come to the fore only to a moderate degree against the controlling force of the broken triad. If our rhythmically enlivened melodies are to show the stronger lines of melodic progression rather than the pretty but deceptive appearance of harmonic chord waves, we must use more effective means.

We know the diatonic step as an integral component of melody; it was already a main structural element in even our earliest exercises. Nevertheless, at that time the voice leading was so limited through numerous rules that step-wise progression could not produce a disturbance either of the single melodic line or of the progression of the two voices together. In examples with the more pronounced movement of the second voice, as we are now constructing them, the diatonic progressions resulting from the shorter note values frequently produce with the other voice the intervals which we have not yet used, namely intervals of Group B (2, 6, 3, 7) and the tritone (6). Their introduction requires some care; we shall, therefore, approach these sturdier, less tractable sounds indirectly, through a discussion of melodic functions.

In the melodies of all periods and styles a number of melodic formulae are found. They are caused by a fundamental manipulation of the raw material for melodic construction: the interval that separates one tone from the next. As in languages we frequently find phonetic combinations which are constantly mixed in countless possibilities, and thus build words and sentences, so the formulae mentioned occur in melodies in constantly changing interplay.

Melodies are not built solely by means of these formulae—other forces, too, are at work; forces which aid in the construction of the melodic lines, sometimes in a subordinate, at other times in a dominating manner. By them, as the smallest formed melodic building stone, we can, however, best learn how melodic force works. Above all we can study, step for step, how melody pushes into the firm structure of harmonic masses and gives them motion. Harmonic mass in our narrow domain means: the six intervals ([3], [6], [3], [6], [3], [6]). If we disturb these intervals with foreign tones which we set against them, wedge in between them, or drive through them, we experience the first unpretentious attempts of melody to lift itself into the position of a dominating force.

The simplest of these melodic elaborations or “disturbances” we have already learned to know in a somewhat different connection. In the first exercise we saw a pattern consisting of: tone—auxiliary-tone—tone.

\[ \begin{align*}
&\text{\begin{tikzpicture}
&\draw[thick, fill=white] (0,0) circle (0.5cm);
&\draw[thick, fill=white] (0,0.5) circle (0.5cm);
&\draw[thick, fill=white] (0,1) circle (0.5cm);
&\draw[thick, fill=white] (0,1.5) circle (0.5cm);
&\draw[thick, fill=white] (0,2) circle (0.5cm);
&\draw[thick, fill=white] (0,2.5) circle (0.5cm);
&\end{tikzpicture}}
\end{align*} \]

It is true that at that point it remained in the air, as it were. Since we did not even reckon with any harmonic relationship in these simplest one-voice melodic models, the second tone of such a group lacked the resistance, the harmonic relation, to a tone of a second voice, from which alone it could take its real significance. We now implant our chief harmonic intervals with the group: tone—returning-tone—tone in which, for the time being, the returning-tone may not be further removed from the first tone than a 1\frac{1}{2} or a 2. (The terms “auxiliary-tone” and “returning-tone” are interchangeable.)

\[ \begin{align*}
&\text{\begin{tikzpicture}
&\draw[thick, fill=white] (0,0) circle (0.5cm);
&\draw[thick, fill=white] (0,0.5) circle (0.5cm);
&\draw[thick, fill=white] (0,1) circle (0.5cm);
&\draw[thick, fill=white] (0,1.5) circle (0.5cm);
&\draw[thick, fill=white] (0,2) circle (0.5cm);
&\draw[thick, fill=white] (0,2.5) circle (0.5cm);
&\end{tikzpicture}}
\end{align*} \]

We then see that the auxiliary-tone in most examples produces a sound which is lower in value than that produced by the main tone because it makes an interval of Group B, or sometimes a tritone, with the sustained tone of the model.

Or it belongs to Group A, as does the first interval, but stands lower in the scale of values assigned to these intervals. An exception occurs with only seven returning-tones, of which we do not yet use the last two:

\[ \begin{align*}
&\text{\begin{tikzpicture}
&\draw[thick, fill=white] (0,0) circle (0.5cm);
&\draw[thick, fill=white] (0,0.5) circle (0.5cm);
&\draw[thick, fill=white] (0,1) circle (0.5cm);
&\draw[thick, fill=white] (0,1.5) circle (0.5cm);
&\draw[thick, fill=white] (0,2) circle (0.5cm);
&\draw[thick, fill=white] (0,2.5) circle (0.5cm);
&\end{tikzpicture}}
\end{align*} \]

The danger exists in all these cases that the returning-tone with its more valuable harmonic interval may become the important element and force
the rest of the group into subordinate positions. We can guard against this by giving the returning-tone a shorter time-value or an inferior position in the measure. The determination of time-values is important not only with such pseudo returning-tones (as in Figure 76), but with others also. If we give a “real” returning-tone (Figure 75) the greatest time-value, or if we place it on an accented point of the measure, it, too, will lose its auxiliary character, will become a chief tone, and will dominate its surroundings.

These forms we should avoid for the present. Hence the following rule:

RULE 31.

The returning-tone may have at most the same value as, or less value than, the main tone, and must fall on a weaker beat. (We exclude syncopation for the time being, for in syncopation these relationships are reversed.) We shall designate the returning-tone in our exercises with a W.*

Besides the returning-tone just described, a second species exists in which the auxiliary-tone and the two original tones are combined into a three-voice chord (a triad, or a tritone chord comprehensible with only three voices).

(The following returning-tones also belong to this species.)

The disturbing effect of such chordal returning-tones, in the sense here illustrated, is weak indeed. In fact they are not really W, but, instead, they belong—apart from the two given in Figure 79—in the domain of melodic construction by means of intervals of Group A, which we used in Exercise 15. At any rate the concept “chordal returning-tone” simplifies in a great many cases the determination of the harmonic value of auditory progressions. We shall therefore let it stand, although we shall always be confronted with the question, whenever we meet such a tone, whether to acknowledge its harmonic independence or to consider it as an auxiliary-tone. If we wish to strengthen its melodic significance—that is to say, its melodic character—at the expense of its too great harmonic content, the shorter note-value and the placing of the note on a weak part of the measure are even more urgently necessary than in the case of the step-wise returning-tone.

A third species of returning-tone, which by skips produces chords that go beyond the boundary of broken triads or simple tritone chords, will appear later under a different name.

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EXERCISE 16

Add to each note of the 2d voice of the following example either melodic or chordal auxiliary-tones, and name them.

For the explanation of the returning-tone, the most primitive of all melodic ornamentation, only a single good interval was needed, to which the returning-tone was added as a passing “clouding.” The same holds also for the simplest type of another melodic pattern. In this, instead of returning to the original tone, we lead the auxiliary-tone step-wise into a tone of the next good interval. We then have the simplest form of passing-tone progression. This progression may contain two or more tones if the goal tone is more than a 7\( \frac{3}{2} \) or a 3 from the first tone.

A more complicated type of passing-tone formation results when the progression is from one interval to a different interval.

* = Wechselton, the German word for returning-tone.
The tone preceding the passing-tone then belongs to the first interval, the goal tone to the second interval. Between these, according to the distance involved, one passing-tone or several such tones may be placed. A passing-tone is designated $D$. The following directions are given for the application of the passing-tone principle.

**RULE 32.**

Chromatic progressions are permitted in passing-tone formations.

![Chromatic progressions](image)

**RULE 33.**

The passing-tones create interval-values equal to or less than, but seldom greater than, the values of the intervals from which and into which they lead.

**RULE 34.**

If, within a series of passing-tones, one of these should form a good interval of Group A with the tone of the other voice, this interval must have relatively little rhythmic value, in order not to lose its passing character.

**RULE 35.**

As a rule, a $D$ falls on a weak part of the measure. It may occupy an accented part or the greatest time value in the measure only if the other voice retains the same tone which it had before the $D$.

![Tones marked + are not passing-tones](image)

* $D_{urchgang}$, the German word for passing-tone.

**RULE 36.**

A considerable number of passing-tones in succession readily awakens the impression of diatonic or chromatic scale exercises. Such patterns have but little value in melody, hence they should be used with care.

![Add as many passing-tones as possible](image)

**EXERCISE 17**

Add as many passing-tones as possible to the second voice of the following example:

An actively moving 2d voice which, through the greater number of its tones and rhythms already well exceeds the melodic lines which served as a 2d voice in Chapter II, can no longer be restricted to the limits which there held; we must now grant this voice greater freedom. The rules governing the construction of the 2d voice are modified, therefore; whereas those applying to the model melody remain unaltered.

Certain rules are eliminated:

- Rule 6: Tone repetitions are permitted
- Rule 8: Sequences are permitted

The following rules are extended:

- Rule 10: Two skips in the same direction in immediate succession may be used if they follow Rules 29 and 30.
- Rule 13: Chromaticism may be used to a restricted extent (compare Rule 32).
- Rule 15a: Broken chords of all kinds are permitted if they follow Rule 29.
- Rule 15f: Any desired tone may precede the final tone if it follows the rules governing skips and the regulations concerning intervals.
I repeat that these liberties refer to only the 2d voice elaborated with melody formulae. For the construction of the original 2d voice, in which but one note is set against each note of the model, the previously given rules for such a setting obviously hold.

A newly added rule is the following:

**RULE 37.**

An easily comprehensible melodic line will be attained only if the movement of the 2d voice takes advantage of a certain balance of motives. It is well, therefore, neither to smother the just awakened life by sequentially repeating the duration pattern of a single rhythmic motive,

\[ \text{not} \]

nor to exaggerate the motion by a too great piling up of non-coordinated, varied patterns.

\[ \text{not} \]

The livelier movement of the 2d voice influences also the relation of the two voices to each other. A few of the strict rules for simultaneous progression and for intervals cannot longer be maintained; they must be given up. In their place several new rules now function.

Those no longer effective are:

**Rule 21:** Broken chords, which are divided between the two voices, may now be used without restriction. Care must be taken, now as then, with tritone formations! The broken augmented triad still had better be avoided.

**Rule 22:** Simultaneous skips in the same direction, in both voices, are permitted if they do not disturb the smooth progression of the setting through their striking character.

**Rule 23:** Cross-relation may occur if the cross-related note occurring as D is of relatively short value and falls on a weak part of the measure.

**Rule 25:** The parallels \( 9 + 3 \) and \( 69 + 39 \) are permitted without restriction.

**Rule 28:** Highest and lowest points may occur simultaneously in both voices.

These modifications also refer only to the two-voice settings elaborated with melody formulae. Note-against-note settings follow the rules for such settings given in Chapter II.

Rules 16 to 20 and Rule 24 continue to hold. One could believe that with the aid of passing-tones it would be possible to cover the parallels prohibited by Rule 24. Actually, the reverse is the case. Passing-tones, as well as all other melodic formulae yet to be discussed, operate chiefly in such a manner that a parallelism covered by them really forces itself into consciousness more strongly than the non-covered, open, parallels. Therefore, \( 9, 3, 4 \) parallels which are covered by passing-tones of short duration, as well as open parallels, are to be avoided.

If we wish to “cover” the parallels to such an extent that they would no longer be heard as parallels, we should have to give the passing-tones (and other melodic formulae) so much space and time-value that they could scarcely count as “passing” formations.

Rule 26 must especially be observed with actively moving voices, because a tonally enriched setting is much more sensitive to similar motion of the two voices into an \( 9 \) or \( 3 \) than a setting of note against note. Covered octaves are to be avoided entirely, except in the progression into the final interval.

Also, Rule 27 is of great importance with regard to very active voices. Covered \( 9 \) and \( 3 \) are permitted only in the sense of this rule. Passing formations can readily produce the following forms, which are always to be considered faulty:
The stepwise progressions $\frac{5}{4}-\frac{3}{2}$; $\frac{3}{2}-1$; $1-\frac{5}{4}$; $\frac{5}{4}-\frac{7}{4}$; with the two voices moving in the same direction, are forbidden without exception, even in later instances with melody formulae which have yet to be learned.

**C. Model Examples**

**EXAMPLE 1.**

 Tranquilly

 All notes not designated W or D make Group A intervals with the notes of the model. In the fifth measure the $b^1$ is designated W although it stands in this favorable relationship to the lower voice; its short duration, however, the position on a weak beat, and the decrease in interval-value (first $c^1$ then $b^1$) permit its appearance as a W.

**EXAMPLE 2.**

 Lively

 The same holds for the interval of the $c^1$ in the second measure. In the fourth measure, even the interval of greater value, the fifth ($e^1-b^1$), is so far submerged on account of duration and metric position, that the $b^1$ functions only as a W. The D $a^1$ of the third measure and the D $c^1$ of the seventh measure fall into the same category. The last $d^1$ of the seventh measure can be conceived either as completing the chord with the $g-g^1$ or, on the other hand, as a D.

**EXAMPLE 3.**

 In the second measure, the last note $a^1$, may count as D or as an integral part of an independent $D$. The same holds for the third measure ($a^1$ on the fifth beat) and for the sixth measure, second beat, where the $a^1$ may be either a W or an independent tone.

**EXAMPLE 4.**

 In the elaborated lower voice: first measure, $d^2$, chordal W; ninth measure $a^2$, chromatic D. The fifth measure, in relation to the original non-elaborated 2d voice, is transposed an octave—an artifice that may readily be employed in order to make the voice leading of the active voice smoother.

**EXERCISE 18**

 Select several satisfactory solutions of two-voice settings in Chapter II. Divide them into measures. Provide their 2d voices with WW and DD, and explain and designate these.
Even if the pupil does not actually find it more difficult to ornament the 2d voice when this is the lower voice than when it is the rather accessory upper voice, he nevertheless, in many cases, will notice that an inner aversion makes the former relationship between active and passive voices seem less natural than the reverse order, in which the passive voice remains the lower, with the active voice above. That is quite understandable, for since tones, in spite of their apparent lack of individual substance, have not identical weight—the lower tones, with their longer wave-lengths, as we have already seen, are weightier (of greater volume) than the higher tones, with their shorter wave-lengths—they also obey the building laws of heavier fixed objects. In the pitch levels of the various tones, as in the height levels of stone, wood, or metal, we like to have the ponderous and weightier material below, as foundation, on which the smaller, lighter building material rises, getting smaller and finer as we ascend. A very active bass voice, therefore, even if it could present its “rouglier” tones to the ear with the same clearness as does the piccolo, with its lightly flowing, readily heard tone-lines, would none the less be opposed to the nature of tone-volume and of audition.

Of course, our lower voices, as here used, are never so low that their volume would prohibit movement; nevertheless, we should follow the general principle: the lower a voice, the less its movement. For us this means that, although theoretically the lower voices are entirely free in their movement possibilities, yet, in actual practice, they receive less elaboration or activation than that which, under the same conditions, would be given to an upper voice.

This apparently full measure of varied descriptions, rules, and restrictions will explain to the student what he may vaguely sense and, to a great extent, may correctly but unconsciously write. One is tempted to say that all rules would be superfluous if each pupil would write only what he can sing without effort and without mistakes, and without the help of an instrument. This would not materially differ from our exercises, guided by the comprehensive system of rules which we have given. Unfortunately, among the pupils today we scarcely find such unspoiled souls; almost all have reached a level of music understanding, either through frequent hearing of complicated music, through playing instrumental music, or through advanced vocal instruction, at which it is easier for them to comprehend the form and content of ambitious compositions than the more strictly linear and auditory progressions in strict and clearly directed one-voice and two-voice settings. The natural responsiveness to the simplest linear and harmonic relationships must then first be reawakened through exercises such as the foregoing. It is, therefore, absolutely necessary (let it be said again) that the pupil adapt all exercises to his own vocal capabilities. In that case neither the melodies nor the harmonies can become more complicated than the development of his writing ability. The procedure to sing constantly the written score can readily be retained throughout the two-voice work. The exercises will be the more effective the less they are worked out at an instrument and the more they are sung without an instrument. The pianoforte, especially, more than other instruments, is the source of much trouble in teaching such tonal settings.

**EXERCISE 19**

Write new two-voice examples, note against note, and elaborate their added voices by means of WW and DD into freely moving melodies.

In order to save the student unnecessary work and errors he is again cautioned to construct the 2d voice strictly according to the rules of Chapter II and to let the freedom which was allowed in the 2d voices used in Chapter III enter only with the more active melody tones (WW, DD). It is true that we could from the beginning also plan the 2d voice more freely, but, in further ornamenting the melody, we should then be confronted with places which could be solved only with great difficulty or with much greater freedom than that acquired up to this point. Reference back to the rules of Chapter II is obligatory in all exercises originating in note-against-note settings, up to and including Chapter IX.
CHAPTER IV
Elaborated Melody (Continuation)

Now that we have learned how the melodic element is linked with the harmonic, through returning- and passing-tones, forming a close texture with it, we shall, in Chapter IV, deal with additional melodic formulae which lead to a type of interweaving thus far not used.

A. Work-Material
The material developed in Chapter III is taken unchanged.

B. Work-Procedure

\[ \text{\includegraphics[width=0.5\textwidth]{diagram.png}} \]

In the preceding example the note indicated \( V \) is a so-called suspension. This designation, as used in this example, expresses the following:

a) At A, immediately preceding an accented part of a measure, one of the six good intervals of Group A is used. This is free of tension and with the immediately following tension (B) serves as preparation for the latter.

b) While the one voice moves by step or by skip, the prepared tone in the other voice is held over into the next accented beat (B). At this point the two voices form a less good interval, of Group B.

c) The tension contained within such an interval strives for a "resolution"; that is to say, for a leading back into one of the "good" intervals. In the given example this occurs through a 2 or a \( 1\frac{1}{2} \) step descendingly in the voice held over, indicated at C. The now newly entering tone has thus been delayed. The feeling of resolution, it is true, is already aroused somewhat if only intervals of Group A are used (see Figure 97) so long as the resolution interval is a better interval of this group than the interval containing the suspension itself.

Here we should add that the urge toward a resolution is inherent in intervals of Group B (\( 2, 6, 3, 7 \)) and in the tritone 5. Their more complicated structure (which I have discussed in the "Theoretical Part" of this work, Book I) readily causes them to yield to the attractive force of the simple, self-contained intervals of Group A. If we bear in mind how harmony and melody are mutually influenced as complementary forces, it is obvious that all intervals have a twofold value, since they must serve both forces. This value is determined according to their harmonic purpose, where both tones are used simultaneously, or according to their melodic purpose, where the two tones are used in succession. The intervals which are more valuable harmonically, as we have already learned, are \( 5, 4, 3, 6, 2, 5 \), and 5. Accordingly, when they are used melodically as tone-progressions, they must be less effective for melodic purposes than the intervals of Group B. These, in turn, used harmonically, fall far short of the values of the intervals of Group A.

The proof of this statement is found in the facts that steps of a second (dispersed interval of Group B) urge melodies forward; that after sevenths, which also are intervals of Group B, or skips of a tritone, stepwise progressions must always follow if we do not wish to produce rather obvious chordal groups; that a melody remains without tension if it contains only the "good" intervals of Group A—in other words, if it utilizes only broken triads (see Figure 73). It is precisely in the suspension that the operation of the two forces, and the relationship between the harmonic and the melodic intervals, can be studied. At A, Figure 96, we have a static sound; this, by the progression of the lower voice, is changed into an interval of harmonic tension, at the extreme point now available to us (B). This strong weighting of the sound compels the held part of the interval to resolve, and it does this by assuming a melodic function in place of the former, predominantly harmonic function; that is to say, it progresses descendingly by the step of a second, making an interval of Group B. This analysis will suffice, for the time being, for the understanding of the har-
monic and the melodic activities of the intervals. We shall learn more about this later.

RULE 38.

The suspension (V) falls as a rule on an accented part of the measure; in any case it must fall on a more accented part than its resolution. Its duration depends upon the leading of the other voice, but within these limits it can be applied at will. Its preparation should embrace, either entirely or partly, the preceding metrical beat. The preparation may be tied to the suspension, or the suspension may sound the tone again. The metric entry of the resolution, and its duration, may be chosen at will.

In addition, for the present, we shall also follow certain other rules in dealing with suspensions.

RULE 39.

The resolution occurs descendingly, either by a whole step or by a half-step. Ascending resolutions, for the present, are not permitted.

RULE 40.

The duration of the preparation should not be less than half of that of the suspension itself. Consequently, only the following duration groups may occur:

a) preparation = 1 duration unit; V = 1 duration unit

\[\text{etc.}\]

b) preparation = \( \frac{1}{2} \) duration unit; V = 1 duration unit

\[\text{etc.}\]

but not:

\[\text{etc.}\]

RULE 41.

Delayed parallel octaves, fifths, and fourths, resulting from the use of VV, are considered real parallels and are therefore prohibited.

Also, delayed covered octave, fifth, and fourth parallels are to be avoided. However, the interpretation of these characteristics is largely dependent upon tempo. It is quite possible that in slow progressions the relatively long tension of the suspension will dominate the entire attention field, and will thus not permit the parallelism to become evident; whereas, in a rapid tempo, where the metric units are closely compressed, the individual members of a parallel pattern are separated by a short time interval, and consequently are perceived as parallel, despite the V effect.

In Figure 99 we have noted all the V constructions possible within an octave and with two voices. For the sake of simplicity the complementary voice is not indicated in the preparation of the V. It can readily be supplied at any time by using a tone which forms an interval of Group A with the given voice.

The examples marked + do not meet our demands for the resolution of the V tension; for in these cases the active voice moves from a V into a tone of an interval which has less harmonic value than the V-interval itself, either because an interval of Group B follows an interval of Group A, or because, within the limits of a single group, the less valuable follows the greater. These patterns, therefore, are of no help to us. The forms a, b, k, l, p, q, r, s, t, u, on the other hand, are genuine suspensions, in complete agreement with our demands. The form i is of a dual nature. According to our rules it may not be considered a V, since in this case the succession V-resolution makes an order good-poor; whereas in a genuine V, the order must be poor-good. The small difference in value between the fourth and the major third, does not, in progressing from the V, permit either an increase in tension or a resolution: the tension is approximately maintained, the sounds remain "hovering." In three-voice or more-voice settings this ambiguous V occurs frequently, but through the addition...
of the other intervals it is changed into a real and entirely acceptable $V$. In order to avoid a different treatment between two-voice and more-voice settings, we may here conceive the form of the $V$ as genuine. The same holds for form $h$, although here we notice not even a maintenance of tension but actually a decrease in value from $V$ to resolution. It is entirely to prepare for its later use in three-voice settings and for a consequent saving in labor that we conceive and use it in our two-voice work as a typical $V$.

The form $r$ is not to be used. It meets our requirements, it is true; but since it overloads the setting with superfluous chromaticism, we shall use it only after we have learned to employ the notes with greater assurance.

We shall also dispense with the forms $a$ and $b$, for the present, because they bring the voices into too close proximity, from which their release is often very difficult. In addition, they introduce into our quiet, carefully adjusted two-voice setting a relatively harsh sound, the effective use of which demands additional knowledge.

If the $V$ is situated in the lower voice, all forms are obviously eliminated which reveal in progressing from $V$ to resolution an interval progression good to poor (the inversions of the forms, $d$, $e$, $f$, $g$, $n$, $o$, $w$, and $x$ of Figure 99), or which consist exclusively of B-intervals (inversions of $c$ and $v$). The form $m$ in its inversion becomes a $V$ which fully meets the rule and is, therefore, admissible.

Forms $hh$ and $ii$ are treated as real $VV$, as inversions of forms $h$ and $i$, and for the same reasons that applied to those forms.

The three forms $pp$, $qq$, and $rr$ are, for the present, to be avoided:

form $rr$ on account of its leaning toward chromaticism, and the other two because in two-voice setting they do not permit any pronounced $V$ effect. Only in three-voice or more-voice settings is a clearly discernible $V$ possible with these forms, by opposing the weak $V$-resolution progression $\text{[56]}$

$\text{Exercise 20}$

Add as many $VV$ as possible to the 2d voices of the following examples. Begin with a half-rest and then divide each whole note into two half-notes, as indicated in the first example.
of the other intervals it is changed into a real and entirely acceptable V.
In order to avoid a different treatment between two-voice and more-voice
settings, we may here conceive the form of the V as genuine. The same
holds for form h, although here we notice not even a maintenance of tension
but actually a decrease in value from V to resolution. It is entirely to
prepare for its later use in three-voice settings and for a consequent saving
in labor that we conceive and use it in our two-voice work as a typical V.
The form r is not to be used. It meets our requirements, it is true; but
since it overloads the setting with superfluous chromaticism, we shall use
it only after we have learned to employ the notes with greater assurance.
We shall also dispense with the forms a and b, for the present, because
they bring the voices into too close proximity, from which their release is
often very difficult. In addition, they introduce into our quiet, carefully
adjusted two-voice setting a relatively harsh sound, the effective use of
which demands additional knowledge.
If the V is situated in the lower voice, all forms are obviously eliminated
which reveal in progressing from V to resolution an interval progression
good to poor (the inversions of the forms, d, e, f, g, n, o, w, and x of Figure
99), or which consist exclusively of B-intervals (inversions of c and v).
The form m in its inversion becomes a V which fully meets the rule and is,
therefore, admissible.

Forms hh and ii are treated as real VV, as inversions of forms h and i,
and for the same reasons that applied to those forms.

The three forms pp, qq, and rr are, for the present, to be avoided:

form rr on account of its leaning toward chromaticism, and the other
two because in two-voice setting they do not permit any pronounced V
effect. Only in three-voice or more-voice settings is a clearly discernible V
possible with these forms, by opposing the weak V-resolution progression

EXERCISE 20

Add as many VV as possible to the 2d voices of the following examples. Begin with a half-rest and then divide each whole note into
two half-notes, as indicated in the first example.
In Figure 105 we see the counterpart of the V. With a V the new tone of the active voice was delayed; here it is sounded before its real time of entry. In other words, it is anticipated. For this reason this melodic device is called an anticipation (V).* For the V the following instruction holds:

**RULE 42.**

The V falls always on a weak beat and is of short duration. Figure 105 illustrates the danger that an V may no longer be heard as such when its duration is too long, but instead a V may be heard in the lower voice.

The application of an V is the least difficult of all melodic formulae. To be sure, it is also one of the least valuable (standing approximately on a par with the W) since it allows the tension introduced to disappear prematurely, and thus leads to the setting a sort of slippery instability. As charming as an occasional V can be, it becomes offensive and inartistic when used too frequently.

**EXERCISE 21**

Add as many VV as possible to the 2d voices of the following examples.

The offensiveness just mentioned need not trouble us in these exercises. We should, however, remember these successions of numerous VV as a horrible example.

At first sight it may seem superfluous to assign two names to two such markedly similar forms as V and N. Nevertheless, it must be done. The

* = Vorausein, the German word for anticipation.

This melodic formula is called an unprepared or free suspension; (N).* It is, in contrast to W and V, as important as D and V. Since its full keenness enters immediately with the first highly tensed interval, not relying upon the usual preparation of the V, its effect is more concise, harsher, and more clear-cut than the latter. With NN, which may be used (without any disturbing effect) in the most varied arrangements, a marked fluidity and effectiveness can be lent to the writing when this is capably done. Indeed, in this manner the harmonic texture is greatly broadened; however, it is still kept within understandable limits on account of the necessary resolution of the N.

The N possesses all the characteristics, without the preparation, of a true V. By determining the common attributes of V and N we at once determine the use of N; this is the same, except for the rules governing the preparation of the V. All the VV in Figure 103 become our material for NN after omitting the preparation. The N, like the V, is dependent for its time-value upon the other voice, but, within this limitation, it can be resolved at any convenient point. The N, also, invariably resolves, for the time being, by a descending whole- or half-step; moreover, in using this progression, delayed V parallels (either open or covered) are prohibited. (Compare the V, Rule 41.) NN with relatively short time-values have a more incisive effect than more tranquil, broader ones. With long and equal time-values the N effect is at times questionable. Like the V, the N normally falls on an accented part of a measure; in any case it falls on a stronger beat than that of its resolution. (For NN in syncopated patterns, refer to Chapter IX.) The normal position for the N, therefore, in any duple metre is on any odd-numbered beat (with resolution into the following even-numbered beat); in triple metre it is on the first of the three beats (the resolution on the second or third), or it is on the second beat (the resolution on the third). Relatively rare exceptions occur when an N, after a rest, falls on an unaccented beat.

* = Nebenton, the German word for neighboring tone.
similarity is marked, it is true; especially so long as we continue to work with our still very restricted melodic and harmonic means; but when we learn to know the field of advanced harmony, the differences will become more and more evident. The \( V \) which, at present, appears largely to overshadow the \( N \) in importance, then steps into the background; the \( N \), on the other hand, becomes an extremely important melodic aid.

There are cases in which an \( N \) can readily be confused with a \( D \). In Rule 35 we learned about the normal position of \( D \) on an unaccented metrical point, whereas \( N \) demands an accented beat. If, now, we find step-wise progressions in an active voice,

\[
\text{\( D \) \( \rightarrow \) \( D \)}
\]

then the tones which fall on weak metrical points, if they do not belong to independent intervals of Group A, invariably are considered \( D D \); tones also, which during the duration of a tone of the given melody fall on relatively “good” metrical points, may be considered \( D D \). But those tones of a step-wise progression which enter with a new tone of the model melody are primarily to be considered in relation to this tone and not as a continuation of the scale passage in the 2d voice. Therefore, they are to be considered \( N N \).

This explanation makes unnecessary the assumption of an accented passing tone, which in the teaching of harmony and counterpoint ordinarily plays the important rôle of emergency aid in otherwise hopeless cases.

**EXERCISE 22**

In the following examples, add as many \( N N \) as possible to the 2d voices, even to the point where repeated and uninteresting patterns may result.

The pupil, in singing such exercises, will learn that the \( N N \), on account of their abrupt entry, are often difficult to sing. If, therefore, an easier setting is desired, the \( N N \) must be carefully selected, or else only the milder forms must be chosen. In the preceding exercise, of course, we have no freedom of choice.

**C. Model Examples**
EXERCISE 23

Above the notes to which the symbols apply write W D \(V \ V\) or \( \mathcal{N}\) in the preceding exercises.

EXERCISE 24

Work out complete two-voice settings, note against note (as in Chapter II), or take those of some preceding exercises, and change their 2d voices to an active form. Add the symbols W D \(V \ V\) and \( \mathcal{N}\) at the proper points and sing the examples. Improve them wherever the setting seems vague or unclear, or wherever the melodic lines and intervals are difficult to sing.

From this point on, take the following fundamental working principle to heart: Never write anything which you cannot completely explain.

CHAPTER V

Principles of Melodic Construction

With the mastery of the exercises in the preceding chapters we have advanced rather far into the secrets of melodic construction. However, we have depended almost entirely upon an expressionless basic melody, without individuality; and we seem to have crept behind the mechanism of the melodies in a none too straightforward manner, by adding tones and figures to the intervals resulting from the simultaneous progression of two voices, instead of beginning with the melodic formations themselves.

We are in a position analogous to that of a man, who, in a strange city, observes here and there a house, a tower, a garden, or a wall, without knowing whence or whither the streets lead, or what form and order the city as a whole takes. He thus knows many separate things, yet does not know anything about their function in the total plan. This perspective of the whole, thus far missing, we shall try to acquire in the present chapter and in later chapters. We shall learn how melodies themselves are built, how their parts are held together, and how they can be guided over longer extents.

A. Work-Material

From the results of the preceding exercises we shall take as a point of departure for our new work those in which the 2d voices are already supplied with various melodic formulae \(W, D, V, V, \mathcal{N}\). For a short time the model melodies, which thus far have served us so well, are entirely excluded from consideration. We now study the melodic procedures in a single tone-line without being disturbed by melodic progressions in an added voice.


B. Work-Procedure

It cannot be denied that this melody, even separated from its leader (the model melody), has an independent outline and an expression of its own. It forms a completely comprehensible entity in itself, without further addition. When we add melodic patterns to the original 2d voice, which was closely bound to the model, the enriched voice-line must acquire melodic motion of a higher order which still points to the original added voice but which, also, in its essential content, follows other laws. I do not assume that even the most painstaking student will have carried his diligence to the point of memorizing the above melody in the form in which it first occurred in Chapter IV. He can, therefore, simply conceive it as a single voice-line, without considering a second, supporting or complementing voice.

If he lets it work upon him freely, in this manner, he will soon notice how the tone-line, like the folds of a cloth, separates itself into heavy and light, raised and depressed, bright and shaded, portions. There is first the rough division into accented and unaccented metric points, indicated by the bar-lines. Then we sense a more subtle rhythmic grouping: the natural progression of the separate motives, each complete in itself and overlapping like the individual links of a chain; thus making a smooth whole out of a series of separate units. We are not here concerned with the two kinds of grouping, since these apply mainly to the rhythmic and formal content of our little piece; instead, we wish to trace only the characteristics of the manner in which the exercise is written.

We have already considered the intertwining of harmonic and melodic elements. We saw, also, how our harmonic knowledge, developed mainly in Chapter II, was arrived at through melodic approaches; that the harmonies used were, in fact, completely bound up with the progression of several voices—in other words, with melodic outlines. Moreover, we proved that intervals served harmonic purposes as well as melodic. Now, if we can prove the derivation of harmonic intervals from melodic progressions in single tones, this double significance (harmonic and melodic) of each interval must also enable us to hear harmonic groups in melodic outlines.

In the first three measures of the present little trial melody, we hear somewhat as follows: with the first two tones we are as yet undecided as to the meaning of what is heard; with the third tone our ear recalls the first g₁, joins this with the second g₁ into a group and subordinates the a₁ to this as a less important tone (W). If, in the meantime, the e₁ appears, the ear links the entire group g₁ (a₁) g₁ with e₁, since the ear can never actually hear in advance, but can only compare the most recent auditory impression with earlier impressions. Here a very small auditory rest-point is found: e₁–g₁ is an interval (e₁) from group A, an independent sound, self-contained, demanding neither resolution nor fixed progression.

It is true we do not hear the tones of the interval sounding simultaneously (harmonically); but the broken (melodic) interval is just as strong. We therefore experience a combination: a harmonic cell extending from the first tone of the melody to the fourth. No harmonic coalescing is noticeable with the following f₁, on account of the very weak harmonic significance of the half-step e₁–f₁. On the other hand, the ear again associates the last tone of the second measure with the preceding e₁, and finally even with the entire previous tone progression. When the a₁ (third measure) enters, the attempt is made to compare this new tone with all preceding tones. No harmonic link can be formed with the immediately preceding tone (poor harmonic value of a 2: g₁–a₁); whereas with the f₁, the a₁ forms a major third. But just as the ear has made this link, it recalls the e₁ and finds therein a still better harmonic combination, a 4: e₁–a₁. This is better because a perfect fourth surpasses a major third in harmonic value. But, in addition, the fourth consists of two tones both of which fall on accented parts of the measures, and the time-values of which are likewise better, since the root f₁ of the third f₁–a₁ is an eighth-note on a weak beat. The tones preceding the e₁ stand, partly, in no harmonic relationship to a₁; yet among them the a₁ has already occurred, which but underscores the importance of this tone as root of the best interval (4).

These facts, concerning the first three measures of our trial example, we can now combine into a generally applicable rule:

RULE 43.

In any melody, tones combine into harmonic cells which consist of broken intervals of Group A. The cells may be sharply separated from each other, but they may also be so arranged that they overlap, or so that smaller cells are imbedded in larger ones. The importance of the cells is influenced by the metric position and the time-values of the elements involved.
and imbedding of cells, with their multiple meaning, is further elaborated through the various degrees of talent, dexterity, and readiness with which the listeners perceive the melodies. Our ear can determine the harmonic interval of an octave or a fifth with unfailing certainty. For the harmonic grouping of successive tones of a melodic line, however, it reserves a certain freedom. It cannot hear cells where none exist; but it is not obliged to register all possible cell structures in a melody. If it were merely a question of doing this, no assistance of the ear would be needed simply to label each third, fourth, or fifth interval contained in the melody, by omitting the intervening steps. By this procedure we should achieve both too much and too little. The ear would not concede cellular structure to a great many of the pseudo-cells thus formed, because their short duration or their poor position in the measure would not permit them to function as independent auditory patterns.

On the other hand, by this procedure those combinations would not be perceived which call forth the feeling of a cell structure only after the appearance of two or more A-intervals. In so far as the raw material of a setting is concerned—the single tones and the single intervals—we can depend entirely upon the sensorial impression which we get from its attributes. This is sharply delineated, real, and as specific as the building material of any other art or craft. But if, instead, we wish to grasp the essence of the smallest units of melodic linearity, which are created by the serial arrangement of the raw material and are thus active in successive (melodic) as well as in simultaneous (harmonic) use, we must, if we are to understand their characteristics, rely rather upon our internal, subjective reaction than upon their external, objective appearance.

It may seem to be risky, in learning the devices of tonal setting, to rely in part upon the auditory perception and in part upon higher psychological interpretations. Yet no treatise on tone-setting can avoid this conflict, whether or not it is aware of its existence, and whether it admits it or denies it. That is inherent in the musical building material itself, which, in spite of its obvious and ready accessibility, nevertheless exercises entirely different and deeper effects—more directly addressing the soul—than do the building materials of the other arts.

It is not our problem to decide to what extent—in the creation and in the enjoyment of an art-work—credit should go to the sensorial impression and to what extent to the more complex psychological interpretation. It is for the psychologist to say whether or not he will grant to the creator and the interpreter of artistic values the permission to divide the entirety of an impression into separate work-procedures. We, however, call upon the experience retained in theoretical instruction through two thousand years, so long as the tones and intervals, in their variegated combinations, serve almost entirely as practice material for our practical schooling. This instruction masters the truly mosaic texture of its creative domain, piece by piece, just as the singer and the instrumentalist can create the indivisible unity of an expressive, technically and aurally perfect tone only if they make smooth all component parts of their mechanism through special exercises. In the art of the perfect singer or player who has completely mastered his instrument, the remnants of part-learning are as little recognizable as are the separate work-procedures of the attempts at tone-setting in an excellently written composition.

Thus the possible varied interpretation of harmonic cells is not a liability. Their constantly shifting harmonic play, with its mostly not sharply differentiated values, forms, rather, one of the main charms of melodic progression.

It will now be instructive to consider the melodies of Chapter I in relation to their cellular content. In even these melodies with very scant rhythm we find cellular patterns, whether it be because two successive tones form an A-interval or because a combination results only after a third tone is heard with step-progression (B-intervals) between. We thus learn clearly why it is impossible to invent a melody entirely free of all harmonic content. We may have ever so many B-intervals in succession—nevertheless, after two or three tones, taken from any starting point, we shall get some harmonic combination into an A-interval, hence into a harmonic cell. Although we cannot eliminate this natural urge of the tones, we can direct it. We need not permit the tones to group themselves merely through weight and succession haphazardly into cells; instead, the place and condition of cellular formation should rather be determined by us. Of course, we saw that cell boundaries cannot always be fixed unequivocally, and that among the total possible cells some are always more important than others and thus call forth a more definite boundary. In melodic construction, therefore, we should try to bring these high-points to the attention of the hearer, so that the non-defined borders and multiple meaning remain for only the less important portions of the melody.

The phenomenon of cell-building in melodies now completely explains Rule 5, according to which only a few definite tones could precede the final tone of a melody model progressing evenly in whole notes without

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the harmonic support of a 2d voice. If, before the final tone, the lower fifth or upper fourth appears, the cell formed between either of these and the final tone may cause the next to the last tone (root of the cell) to be heard as main tone, with the final tone merely completing the cell. The feeling of formal tonal close is called forth definitely only if the closing tone may cause the next to the last tone (root of the cell) to be final. The final tone may cause the next to the last tone (root of the cell) to be finality.

Through an added 2d voice, the harmonic content of a setting gains so much in importance, in comparison with the purely melodic content of the melody model alone, that a skip may be used in the model, which binds the final tone of the model into a cell with a foreign root-tone. This, as we have seen, may occur in special instances when the aim is not to utilize the model independently and when the added 2d voice moves by step into its closing tone.

Let us consider the further development of Example 113 and let us follow once again the relation of the ear to it. The c⁵ of measure three with the first tone of measure four completes the harmonic cell (c⁵–a¹); but upon hearing the very next tone the ear must readjust itself, for now it hears a better combination, namely, the fourth: c⁵–g¹. With the next to the last tone of measure four (f') the ear, having determined the cell a¹–f', makes a further discovery: it not only hears a broken interval but a whole chord at once, the broken triad f'–a¹–c². When the d¹ of measure five is heard, the ear finds the following order: the cell d¹–f'; another cell d¹–g²; the broken triad d¹–f¹–a¹; and, finally, the broken seventh chord d¹–f¹–a¹–c². This seventh chord, auditorially, is the main combination, since it is bounded by the first and the last tone of the entire group. The last tone is on an accented point of the measure, and stands before a caesura, which lends it special emphasis. Moreover, the a¹ falls on a good metrical point and this note is an integral part of the seventh chord.

From this analysis we can formulate the following rule:

**RULE 44.**

In addition to the harmonic cells, larger harmonic units occur. They consist of broken triads or other readily recognizable broken chords. These harmonic groups we shall call *harmonic fields*.

Details of harmonic fields are given in Chapter VII. In order to avoid any possible misunderstanding it should be said that harmonic fields are concerned entirely with harmonies formed of the tones of the melody itself; in no case are the harmonies meant which are added below a melody or which are formed by the presence of several other melodies.

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**EXERCISE 25**

Indicate the harmonic cells and harmonic fields in all melodies (the active 2d voices of the exercises) written in Chapters III and IV.

Whenever in the present chapter we speak of "melodics," we always mean the added voices, ornamented with W, D, V, V, N, and never the original models.

Since the tendency of harmonic cells and of harmonic fields is to bind or link several tones into a unit, they also tend to disturb the evenness or steadiness of melodic flow. Within the constant, steady, forward movement of the melodic progressions, they become parties to a pleasant lingering, a contemplative beauty, even if these lingerings are ever so short. The forward striving tone-groups which operate against these delays are those of W, D, V, V, and N. Later, we shall meet several others.

Let us constantly keep in mind that in melodies, two kinds of tone-grouping occur:

- **a) a retarding grouping:** harmonic cells, harmonic fields;
- **b) an accelerating grouping:** W, D, V, V, N, and other melodic formulae discussed in later chapters.

Like the W and the D, the N also can be clearly discerned in a single voice without the harmonic counter-pressure of a 2d voice. These formulae as melodic subdivisions are added to the complete harmonic groups of cells and fields; they enlarge these harmonic groups as subordinate parts, before and between the cell boundaries and the chord tones of a field. Through the addition of a 2d voice, however, the harmonic significance of these attachments can be completely altered. In most cases, nevertheless, the N also needs the harmonic opposition of a 2d voice, in which case it acts entirely like a V, which, without a 2d voice, cannot at all be perceived as a V, but functions merely as a rhythmic characteristic of the melody.

Cells and fields on one side, W, D, V, V, N, on the other side, yield, in the best instances, a more or less attractive combining of tone-groups; but the power to bring their sequence, their distances, or even their pitch levels into a unified order is not contained within them. For attaining such an order we have two other devices: one again of a retarding nature, the other of an accelerating nature.
The first of these is as readily comprehensible as it is usable. It consists of the frequent return of a tone, with several other tones intervening. It is clear that such a tone, unifying, as it does, the various cells, fields, and other formulae around itself as an axis, must call forth a very close grouping which refers chiefly to the pitch-level of the melody. The danger existing in the very marked centripetal force of such a recurring tone is equally clear: it can inhibit the free sweep of the melody and can neutralize all the development obtained through other means. Therefore, in using this unifying device of melodic construction, the tone-repetition, we must exercise great care. Its effects can be magnificent when, in a melody, the expression of quiet, of firm rest, or of dull fixation is desired, or when the structure of a piece demands founding it upon a specific pitch-level. Its effects are horrible and deadly if tone-repetition is used without taste, or if it creeps unnoticed into the tone-groups, and, like a slow poison, kills the motion in them. As early as Chapter I we avoided the returning-tone because it would have disturbed the development on account of the long tone-durations there used. (When short values are used, as we already know, it is harmless.) On the other hand, we unified the melodies by keeping the first and the last tone the same. We can now fully understand the need for both precautions: they aim to avoid the bad effects of recurring tones and at the same time assure the advantages in their use.

For using this device no special rule is needed. We need merely mention that its significance can be increased or decreased according to the time-values and metric positions of the tones involved.

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**EXERCISE 26**

Locate the repeated tones in the exercises of Chapters III and IV and study their good or poor effects.

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tending from the first into the second measure, which, independent of measure and motive grouping, independent also of harmonic and melodic formulae, connects the highest points of the melody. This combination passes from a¹ to b⁷, to c⁶, then back to b⁷. In this progression, ascending and descending in major and minor seconds, which surpasses all other linear aspects of this passage, we have already, in a very small degree, recognized the ordering principle: stepwise progression.

Its function, however, is not exhausted with the linking of tones situated in close pitch-proximity into narrow chains of seconds; its real effect extends to combinations of a higher form. Over the small step-progression (a¹–b⁷–c⁷–b⁷) a larger bond (a¹–b⁷–c⁷–d⁷–c⁷) extends, joining the accented first beats of measures 1, 2, 4, and 5, and ending with the syncopated c⁷ of measure 6. And we can also determine another step-progression, which, it is true, does not embrace the tones marked through their rhythmic position, but which in place thereof connects the “peak-tones” of the melody and thus is particularly noticeable. (The short, subsidiary step-progressions, indicated by dotted lines, do not in any way disturb the movement of the more important progressions; the close proximity of their members lends them but moderate emphasis; moreover, they often do not occupy prominent melodic points.)

Finally, we note another important step-progression which connects the lowest tones of the melody, from the f¹ of measure one over the g¹ of measure three to the a¹ of measure four, descending from there over the g¹ of measure six to the final tone of the melody.

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**RULE 45.**

In order to organize a melodic progression so that its structure is recognizable even with the most complicated use of tones, progressions, and rhythms, its high-points are placed in a series of ascending and descending step-wise relationships (step-progression). These can begin and end at any point of the melody; nor need they be continued uninterruptedly.

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**RULE 46.**

If several step-progressions can be determined, the more important are those the notes of which fall on the most important points of the melody or upon the most important points of the measure.
RULE 47.

Usually a step-progression will be built from the row of upper pitch­extremes; a second one will embrace the row of lowest melody points. Between the two, other step-progressions may extend or may lead into the main progressions.

RULE 48.

The temporal distance between the tones of a step-progression can be as great as desired. At one place the progression can be formed of three successive tones; at another, several measures may intervene between two of its tones. Too long a succession of equidistant spacings deprives the melody of all tension; too many steps in immediate succession have the effect of a scale and not that of a step-progression.

As premise for the development of good step-progressions, it is obvious that we retain the previous rules for melodic construction. In order not to become confused by the mass of new experiences, we shall not write new melodies for the present, but, as basis for the new work, shall use exclusively the melodies written in the previous chapters.

Step-progression is in no sense a panacea, the presence of which guarantees the value of a melody; nor can an unsatisfactory melodic line always be changed into a satisfactory one by means of step-progression—although this can often be done. It is even possible that strong accentuation of harmonic fields restricts the appearance of step-units to small groups which remain relatively unnoticed (we shall learn to know such instances). Also, in sequential melodic patterns a step-progression often cannot be determined; the unification in such cases is guaranteed by other means, namely, through the actual sequential repetition of tone-groups.

If step-units are plainly present in a melody, and if, moreover, its development is not retarded through too many recurrent tones, we have at least the guarantee of straightforward and definite melodic progressions. Step-progression, therefore, is to be considered entirely as a means checking up on the purely melodic forward urge of a tone-succession.

Since neither the dissection into step-progressions nor the determination of harmonic cells and fields is ever a fixed and immovable measuring rule the personal taste of the listener frequently decides those cases in which clear and unequivocal judgment as to the presence and course of such progressions is not possible. But whatever the decision: whether it establishes one single, short progression, or five extended step-progressions, the lines of tones must always be heard as logical and comprehensible.

EXERCISE 27

Indicate the step-progressions in the melodies which have already been used for analysis in the two preceding chapters.

C. Model Examples

The following three examples are intended to show how the ear attunes itself to the harmonic and melodic aspects of a melody; how it constantly strives to form coherent groups out of the melody tones, whether these groups result from harmonic grouping (cells or fields) or from melodic grouping (step-progression). For the sake of greater clearness, the melodies of these examples are projected, above and below the regular staff patterns, on a linear system which uses a separate line for each pitch-level (half-step interval) within the entire range of the melody.

The projection above shows the harmonic cells and fields. A line between two note-points indicates the formation of a harmonic cell between these notes. The harmonic fields are further indicated in letter names above the head of the system. The projection below the staff notation shows the analysis into repeated tones and step-progressions. The most important step-progression is indicated by a solid line; less important ones by dashed lines (-----). The grouping through tone-repetition is indicated by a dotted line (.........).

These examples serve merely to make clear to the student, through inspection, the nature of harmonic and melodic groupings in melody. He does not need to sing them, nor should he be tempted to construct equally complicated examples. These are intentionally somewhat overloaded with all sorts of attachments in order to bring out clearly the variegated character of tone-relationships.

After the given analyses have been carefully checked, each harmonic relationship and each step-progression should then be tested by playing them very slowly at the piano. After that the pieces should be played at the correct tempo (Figure 115, allegretto; Figure 116, moderato; Figure...
ure 117, allegro); whereupon we shall notice that the ear no longer hears all the indicated relationships. The more rapid tempo does not permit analysis into all details; the rhythm, the pulsations of which were less noticeable in the slow tempo, becomes more emphatic and draws the attention away from the harmonic and melodic aspects. Moreover, the attention of the ear is directed by the will. It bears those relationships as dominating which are at the focal point of attention; the others become subordinated in the fringe of the attention field. And, in a rapid tempo, even the keenest intelligence consciously reacts to only the main relationships. The attentive player or listener will now realize the chief harmonic and melodic characteristics and he will understand how they can proceed with and alongside each other in a meaningful and correct order.

If, perhaps, he has believed, up to this point, that step-progression and harmonic fields can be picked out of any meaningless and stupidly mixed "tone-soup," by fishing out tones and placing them in appropriate order, he will now notice that, although a certain choice does remain, only a few possibilities for field- and for step-formations exist which show the necessary logical affiliation in themselves and in the connections with their neighboring groups. The ear hears step-progressions and harmonic connections only where they are actually present, not where we should like to hear them. Quite true, the ear is sufficiently amenable to note things in slow, careful listening which it has missed in hasty perusal; but it cannot be deceived.

Although the learner may have recognized the logic of melodic construction, in which the correct consequence of step-progression is readily understood but in which the connections of harmonic cells and fields require further study, he must not suppose that, with an intentional employment of harmonic cells and of step-progression, talent can be replaced by diligence, or that inspiration can be supplanted by clever calculation.

A melody constructed strictly according to all the rules still need not speak to the heart. On the other hand, any convincingly effective melody will always show logical harmonic and step-wise relationships. The implantation of the knowledge here gained can be made in original creative work without undue forcing. It is not necessary, from now on, to plan each melody from the beginning on the bases of harmonic fields and step-progressions. On the other hand, later reexamination and improvement are always desirable. Above all, music of all kinds with which we come into daily contact should be analyzed as to its melodic construction. After
even a few such attempts we shall be surprised to learn how beauty and logical development are verified by beautiful and logical progressions; and how, conversely, in poor music, dullness and illogical content are unsparedly revealed in the dull and awkward step-progressions and in the harmonic cells and fields.

After one has had this experience several times, one's own work, without further help, naturally directs itself toward the goal of logical melodic construction. The feeling for the best and most appropriate melodic procedure becomes so sure, in time, that the ideas, from the very beginning, comply with all demands of the logic of melody.

CHAPTER VI

Elaborated Melody (Conclusion)

A few further additions must be made to the chapters on melodic formulae. Not all has been said that is to be said about the devices already discussed; moreover, there are several formulae which we have not yet learned. Both problems will be dealt with in this chapter. In contrast to Chapter V, which was intended primarily to provoke thought by its fullness of theoretical considerations rather than to supply practical work material, we shall return, in Chapter VI, to the working out of many exercises themselves.

A. Work-Material

Once again we shall begin with two-voice settings as these were given in Chapter II. In Chapters III and IV we inserted \( W, D, V, V', \) and \( N \) into the original patterns; in this chapter we shall supply these patterns with new melodic formulae.

B. Work-Procedure

Suspensions may occur in all values, provided that the relationships of accent given in Rules 38 and 40 remain intact.

The \( V \) may be resolved ascendingly as well as descendingly; with that extension Rule 39 no longer holds.
RULE 49.

If a V in the upper voice resolves ascendingly, the resolution interval may be a 1, 5, 6, 8, or 9. In all cases the resolution must be made by a whole step or by a half-step.

The forms a, b, k sound rather harsh in a two-voice setting, because with only two voices we have no way of softening the harsh sound of 9 or 9. Nothing, however, can be said against their use. If we wish to construct a setting entirely with pleasant, inactive sounds, such suspensions are not appropriate.

These four VV are prohibited by Rule 24 (1 and 5 parallels) only when the tempo is rapid. In slow tempo the keenly active sound of a V does not permit the parallelism to become effective.

RULE 50.

VV in the lower voice which resolve ascendingly through a whole or a half-step may have 1, 5, 6, 9, or 9 as resolution intervals.

One or more tones may be inserted between the V and its resolution (whether the V be ascending or descending). These insertions usually stand in a step-wise relationship to the V itself (a) or to the resolution (b). With more than one inserted tone either the V is repeated (c) or the resolution tone is anticipated (d)—devices which weaken both. Such inserted tones, therefore, in order not to deprive the formula V-resolution of its effect, should be of short value, especially when they form A-intervals with the other voice. If the inserted tone-group contains a skip (Figure 123e) this should follow the restriction of Rule 29.

Should the student wish to determine the significance of each inserted tone, he will find that several analyses are often possible. In the preceding example, for instance, the notes indicated with a + may be interpreted as follows:

a) the d^2 is an insertion between the V c^2 and its resolution b^1, but, on account of its favorable position in relation to the lower voice, it has independent harmonic value; or, the V c^2 resolves ascendingly into the d^2, in which case the following b^1 as separate tone helps to build the independent interval 9. On account of the short value of the d^2 the first analysis is the more convincing.
e) the $d'$ is an anticipation of the resolution of the $V$ with following $W$ ($c'$); or the $d'$ may itself be considered the resolution; this, however, on account of its poor position (time-value and metric point), is not very convincing.

This multiple meaning of the melody formulae, which will not narrow down in any way with the addition of the remaining categories, makes the application of any one analysis more difficult. Nevertheless, it is always a sign of the richness, plasticity, and poignancy of melody. The student must admit the fact of various interpretations; but in his written work he must always decide in favor of a single interpretation, and this should be the one that is most convincing.

To reassure him, let it be said that the aids given in Chapter VII will not make this choice too difficult for him.

EXERCISE 29

a) Insert one or more notes into the 2d voice of the following example between $VV$ and resolutions and designate with its appropriate symbol ($W$, $D$, $V$, $V'$, $N$) each note which does not make an interval of Group A with the model.
b) In several measures there are no $VV$. Which measures are these? Why are these various notes not $VV$?

Since the $N$ is to be considered a $V$ without preparation, the supplementary rules given for the $V$ apply also to the $N$: It can resolve ascendingly (in which case it must progress to the intervals prescribed for the ascending resolutions of the $V$); and between it and its resolution inserted tones may occur, which are to be treated in exactly the same manner as those inserted between the $V$ and its resolution.

EXERCISE 30

Insert notes between the $NN$ and their resolutions in the 2d voices of the following exercise, and designate them as in the preceding exercise.

All the melody formulae thus far considered have stood, each in its own way, in step-relationship to one of the chief intervals of Group A (with the $D$, however, the possibility has existed of extending this narrow band by several successive step-wise intervals; and the $V$ could be reached by skip). But with these tones not all conceivable step-wise groupings are exhausted. If we consider the following example we again find two patterns, in which, besides an interval of Group A, a harsher interval occurs (one from Group B or a less valuable one from Group A). This leads, by step, either from or into a more satisfactory interval. Both patterns are derivatives of $N$; forms a to c show neighboring tones left by skip ($N'$), and the other forms illustrate such tones approached by skip ($N$).
For these the following rules hold:

**RULE 51.**

The \( N' \) occurs a half- or a whole step away from an interval of Group A, following it on a weak part of the measure. The tone following it may then be taken only by skip.

**RULE 52.**

The \( N \) comes on a weak metrical point, following an interval of Group A, separated from this by a skip. The note following it may then be taken only by a half- or a whole step.

Both \( N' \) and \( N \) are truly effective only in relatively short note-values. When their values are too long, these neighboring tones, like all other melodic formulae, either become integral parts of independent intervals and must then be treated according to the rules governing such intervals, or for the present (if they belong to Group B intervals) are not to be used. In their mildest form, when they make Group A intervals with the other voice, they lose much of their auxiliary-tone character, even when the values are short; they can then, if they are conceived as parts of the following harmony, become confused with the anticipation (\( V \)). But even when they make the best intervals, \( \frac{5}{4} \) or \( \frac{4}{3} \) of Group A, with the other voice, it is advisable to consider them \( N' \) or \( N \) instead of independent formations (if the duration of the note is not opposed to it). This view materially simplifies the harmonic analysis of a tone-setting (see the remarks applying to this in the section on \( W \) in Chapter III). In the most pronounced forms of \( N' \) and \( N \), in which their characteristics are most clearly defined, they are constituent parts of an interval of Group B, or of a tritone. They then obviate Rule 29 (which, otherwise, functions unaltered) and can readily make unstable the firm structure of a setting. Care should be taken with these incisive, unobscured, challenging sounds. They should not be used too frequently and should be given short note-values. \( N' \) and \( N \) can also occur as parts of tone-groups between a \( V \) or an \( N \) and its resolution. In Figure 123 a and b, the notes occurring between \( V \) and \( N \) resolution can thus be considered \( N' \) or \( N \).

**EXERCISE 31**

Supply the 2d voice of the following example with \( N \) and \( N' \). (Guard carefully against \( \frac{5}{3} \) and \( \frac{5}{5} \) parallels.)

Finally, two patterns follow in which step-wise connection with adjoining tones is partly or entirely absent. These formulae are the **accented free tone** (\( \tilde{F} \)) and the **unaccented free tone** (\( F \)).

**RULE 53.**

The \( F \) is used on a better metric point than the tone which follows it (which belongs to an interval of Group A); it is of short duration (important!) and it is left by a skip. In this pattern the \( F \) can at least be approached by step.

In the case of the \( F \) (unaccented free tone), even this step-wise approach disappears. The \( F \) falls always on a weaker metrical point than does the tone following it (which belongs to an interval of Group A); it is approached by a skip and it is left by a skip.
\( F \) and \( F \) form mostly Group B intervals or tritones with the other voice.

The accented free tone is a derivative of the \( N \); it differs from the latter in the skip between it and its resolution. This skip is also the distinguishing mark between the \( F \) and the \( N \) or \( N' \). We could say that the \( F \) results from a coinciding of \( N \) and \( N' \). In many respects it is also like a \( W \), especially when the tone following it is the same as the tone preceding it. This form of \( F \) (as was mentioned in Chapter III, p. 43) differs from a \( W \) with skip, because through it combinations result other than broken triads.

\( F \) and \( F \) as well as \( N \) and \( N' \) obviate Rule 29 concerning skips. Rule 30 also is entirely useless in relation to these two free melodic formulae.

Some skill is needed in handling these two formulae, so that they do not unduly disturb the flow of the melody. Fortunately, their use is restricted; by using many \( FF \) and \( FF \), it is difficult to have melodic balance come to the fore. They are almost always more strikingly characteristic than attractive. They are described at this early point of instruction chiefly to complete the list of melody formulae. This does not mean that they are to be used frequently. The student, therefore, should write them only where they fit naturally and readily into the tonal environment. Moreover, the student must be able to explain them unambiguously without confusing them with other melodic patterns.

Since these two formulae are “free”—that is to say, they do not adapt themselves without opposition into simple triad or seventh chord harmonies—they often fall outside the harmonic fields. In addition to their function as \( F \) or as \( F \), it is thus important to justify them in the melodic line as belonging to one of the step-progressions or to the axis of the frequently recurring tone.

Finally, we should mention that it is not absolutely necessary that these formulae be preceded and followed by independent Group A intervals. We have already seen how several \( DD \) fill in free places between “good” tones. Moreover, scale-like mixed progressions of \( DD \) and \( NN \), as well as those occurring between \( V \) (\( N \)) and their resolutions, have frequently freed themselves from the narrow limits of the surrounding A-intervals. There are still other cases, in which several formulae closely support one another; frequently \( WW \) are mixed with \( N \), \( N' \) or \( N' \):

\[ \text{DD appear in close relation to the \( N' \):} \]

\[ \text{\( N \) and \( N \) follow each other in immediate succession.} \]

If the \( N \), and more especially the \( N' \), \( N \), \( F \) and \( F \), each one alone, can, under certain conditions, disturb the purely melodic and harmonic structure of our two-voice little pieces, it is obvious that a piling up of these formulae may result in a complete degeneration into vagueness, into an unfathomable morass of tone. The student is advised, therefore, to use mixtures of these formulae only in so far as he can explain them satisfactorily.

We have now discussed all possible melodic formulae or patterns. The conditions which hold for our strict two-voice settings do not hold for all forms of writing. We shall see, in a more complicated two-voice style, working with more unyielding material, and especially in three- and more-voice settings, how although the formulae do not alter their nature or essence, they yet accommodate themselves to different environments.

\[ \text{C. Model Examples} \]

\[ \text{EXERCISE 32} \]

Explain the melody formulae contained in the following examples and add the symbols \( W, D, V, V' \), \( N, N', \), \( F, F \).
EXERCISE 33

Take the unelaborated 2d voices of the preceding examples and activate them by inserting various melodic formulae in a manner other than the one given. Add to each formula its appropriate symbol.

EXERCISE 34

Take the 2d voices of the exercises in Chapter II and add melodic formulae with their symbols.

EXERCISE 35

Write new two-voice settings, note against note, and supply their 2d voices with melodic formulae. Name these.

CHAPTER VII

Tonal Higher-Units

In the last four chapters, we have gone so deeply into the study of melodic functions that it would be advisable in this chapter to turn our attention once again to the harmonic aspects, if only for the sake of change. But, in addition, we must do this because we have now arrived at a point where we can follow the operation of the melodic element in two-voice settings further, and to its conclusion, only if we call additional harmonic experiences to our aid. We now touch the point where the melodic and harmonic forces, pressing from various directions, so intertwine their matrices that we pull one thread along with the other if we analyze the tonal web into its separate strands. If we consider harmonic perceptions we discover thereby new points for melodic construction as well; and, conversely, we can use the melodic experiences which we have had to further our harmonic work.

A. Work-Material

1. The analyses and problems of Chapter VII are still based upon the linear and harmonic vocabulary with which we are now well acquainted. Once again we begin with two-voice settings, note against note, as produced in Chapter II.

2. To this, however, must be added an important extension. We shall use a characteristic of tones which has not yet been mentioned. To explain this I must deviate somewhat, in order to make it comprehensible to the student who is reluctant to go beyond our safe field of tone-relations, which are easily recognized, as easily systematized, and, above all, are unambiguous. A fifth, for us, has been thus far a non-alterable, independent concept regardless of the precise root upon which it stood, regardless of whether its tones appeared in succession (as 5) or simultaneously (as 5). The same conditions have held for all other intervals. In the harmonic
interval table of Chapter III, we arranged intervals for our use in such a way that they all stood on the same bass-tone (c). We could, just as well, have arranged them in another order, for example,

\[
\begin{align*}
\{ & a^1, B, d^2, c^1, d^2 \\
& d^1, F^\# , b^2, e^b, b \\
\end{align*}
\]

the value order of the intervals [5, 4, 5], etc., would have remained precisely the same. The beginnings of a third order were given in Chapter II, where in Figure 42 all intervals indicated by encircled figures had the same root-tone. A little simile may serve to clarify these various interval series.

We all know people around whom a common first name throws a mild bond of association for us. The individuals, who themselves are independent of each other, are linked into distinguishable groups by means of names: Henry, John, Mary, and others, without thereby changing a single member of such a group or influencing his relationship with the environment. In just the same way we group the separate fifths, thirds, etc., on all pitches, whether their tones be sounded successively or simultaneously. These are the "persons" of musical experience; each of them has its own form, its individual characteristics, and its desires to be used in its own appropriate way. Their individuality as fifth, third, etc., permits them to be like other fifths, thirds, etc., built on any pitch level. They are grouped together solely through this external similarity. However, the numerous Henrys, Johns, Marys, may be united among themselves through many bonds; business activities, common needs and goals, friendships and loves, may integrate them into newly stratified groups—as a common bass-tone forces the most diversified intervals onto a common level. And now, finally, comes the strongest bond to which a person is subject: the family tie. All the above mentioned Henrys, Johns, and Marys have parents, brothers and sisters, and other relatives of varied names and appearances. We cannot judge the kind or degree of their relationship through our sense impressions, and even with people whose relationship we know we see nothing in their acts or words which would indicate the nature of such a strong bond. Yet we know that it exists, and that through its force it keeps people together, without asking their opinion or consent. In the domain of intervals the family relationship of people is paralleled by the tonal relationship to a common tonal center. This is the source-tone, the father, around which the intervals group themselves like a much-branched family of children, grandchildren, and great-grandchildren. The force of relationship, which flows from the common center and coheres intervals of all sizes and kinds, which governs the progression of sounds without itself being directly heard, is in essence neither the same as the melodic nor the same as the harmonic force which operates in tone-connections. Nor is it to be conceived as summation of tensions resulting from all these forces—although it has often been confused with harmonic energy and, as a matter of fact, can readily be so confused. The common source-tone rules over all other forces; in all tone-progressions we experience the effect of the mysterious, concealed ferment, tonal coherence. This is so all-persuasive that we can never succeed in repressing it. We can create tone-lines in which it appears repressed; we can veil it, apply it incorrectly, or mishandle it; but we cannot extinguish it. If we should succeed in making it unnoticeable at one point, it would assert its authority the more strongly at another point. We can fly ever so high with balloons and airplanes, and delude ourselves into escaping from the earth; in spite of everything, however, gravity will always force us back upon the ground. Tonal coherence, or tonal "binding," is nothing more than gravity in its most refined form.

How does the source-tone of a tonal family appear and in which way does it govern its subjects? Let us take C as tonal chieftain of a group.

The remaining tones of the chromatic scale then arrange themselves in the following order of subordination to C: G, F, A, E, E\#, A\#, D, B\#, Gb, B, F\# (Gb). Other governing tones than C rule over similar other series, which are transpositions of this model series.

I know the objection which every reader and every student will offer to this proof: "We know that already; it is the series of harmonic (simultaneous) intervals with slight changes in the region of thirds and sixths." Com-
pletely wrong! We are not at all concerned here with harmonic intervals, intervals the tones of which sound simultaneously. Whoever at this point does not realize that the tangible fragments of simultaneous and successively sounding intervals are related to the abstract relationships of the tones only in so far as our system of notation, which is insufficient for such subtleties, is compelled to portray them in similar patterns, should attempt without fail to familiarize himself with this new conception.

He may, perhaps, succeed more quickly if he pictures the intervals and their values as physical or material quantities representing various values in a series (dice, coins), but conceives the family relationships as mathematical or chemical formulae. The $G$ of the model series thus represents, in its relationship to the $C$, neither a $5$ nor a $2$, but merely the expression of the degree of attraction in which any tone, at the distance of a perfect fifth, stands to its main tone. All tones of this series, regardless of how they follow each other, are constantly referred back, by the ear, to the governing source-tone—in this case $C$, in so far as this has the chance to exercise its binding or cohering power. We thus no longer hear only the successive or simultaneous tones of an interval, but sense how a kind of magnetic force organizes them with respect to a common center. The source $C$ is reflected constantly through all tone-connections so long as we move among the tones belonging to its series; in fact, they receive harmonic significance only through this tonal coherence.

The relationships to $C$ could readily be traced further, beginning with $G$ and extending beyond the last tone $F\# (G\#)$; however, we should thus obtain merely tones which deviate but slightly from better degrees of relationship ($F\#$, $G\#$, $D\#$, etc.). That would multiply our work material without producing any practical gain. We therefore use the simpler relationships, instead of the more remote or the non-relationships. (For a more detailed treatment see Book I, the theoretical part of this work.)

The governing power of the source-tone is not exhausted in cohering the separate tones of its series of relations. It at the same time draws everything into its controlling field which is built upon these tones belonging to its series: in two-voice work the harmonic intervals built upon the common root-tone; in polyphonic settings, chords of all kinds with as many voices as desired. Such a mutual existence and interactivity of a family of tones, centering around a source-tone, or tonal center, results in what is generally called "key." This concept, however, is so non-inclusive that it embraces the broad domain only with the help of complicated evaluations, alterations, and transpositions; a domain which, according to our series of relationships, is subordinated from the beginning to the source-tone. We, therefore, speak rather of "tonality" when we mean the total series of relationships, with all that is built upon it, and designate the source-tone of a tone family as "tonal center." It will be symbolized thus: $\Phi$.

The scale of tone-relations is a scale of values just like the scale of the harmonic intervals with their value groups $A$ and $B$ (see Figure 69). The closer a member lies to the tonal center, the more closely is it related to it and the more strongly does the binding force of this relationship manifest itself in an extended, tonally rich setting whenever this member appears. The first degree of relationship, through its close family connection, is the strongest support and confirmation of the source-tone. But it also possesses so much power of its own that, of all relatives, it can make itself most readily independent, founding its own tone family if it is not forced to support the original tonal center. On account of its prominent position in the tone family, this first relative is called "Dominant." We shall assign to it the following symbol: $\Phi$.

The next relative at once stands in a weaker relationship to the source-tone; none the less it, too, is such a strong support of the tone family that it carries the name: "Subdominant" (symbol: $\Phi$).

After the subdominant the value of relationship is gradually lessened to the last tone of the series, standing in a tritone relationship to the source-tone. Here the bond is very loose and is noticed only when specially emphasized.

These remarks will suffice to clarify the nature of tonality. Much could still be said about it, especially as to its inner construction and about the important function therein of third-relationships and that of the leading-tones. In the narrow range of two-voice setting, the simple tonal groupings suffice; the more so because the rules governing progression and intervals prevent us from violating the purpose and content of tonal coherence.

From this point on, we shall call Series 1 the group of decreasing relationships which center around a source-tone, on account of their controlling cohering power over all harmonic activity, and on account of their basic importance for the auditory progressions of a tonal setting. We shall call Series 2 the group of decreasing harmonic interval values which are subordinated, governed, and directed by Series 1. We are already well acquainted with the two groups $A$ and $B$ of Series 2, and from now on we
call it Series 2 to show its dependence upon the value order of Series 1.

Note, therefore,

\[ \text{Degree of relationship: 1} \]

which procedure we may use octave transpositions in order to secure a less broken line—see the seventh interval of this example).

we shall obtain a tone-succession consisting partly of tones of the lower and partly of tones of the upper voice. We call the resulting melody, built of the root-tones of the separate intervals, degree-progression (Stufen-gang). Since in two voices the root of an interval can have but two possible positions, the degree-progression of a two-voice setting cannot develop any great independence. In the extreme case of dependency it may occur as the true reproduction of either of the two voices (in the given example, Figure 139, it does this with the exception of a single tone). But it may also skip constantly from one voice to the other; in which case, however, leaps larger than a fifth can be avoided by transposing an octave downwards in order to produce the less broken tone-line. The degree-progression is to be considered the basic progression of a musical setting. It shows clearly that even behind harmonic procedures, step-wise progression stands as the controlling melodic phenomenon; that, therefore, all auditory activity is anchored to the natural basis of melodic motion.

RULE 54.

All harmonic progressions may be traced back to a melodic line which consists of the root-tones of the separate intervals, and this constitutes the degree-progression.

**EXERCISE 37**

Extract the degree-progressions from the two-voice examples of Chapter II.

The degree-progression is a melody of the kind developed in the melodic models of Chapter I. The degree-progression can be extracted from [95]
even the most daring and cleverly constructed many-toned chord progressions, in the same simple and unambiguous manner, and, therefore, these models are to be considered as the visual projection of the basic foundation of all auditory progressions. However, the degree-progression will differ in details from a melody-model because it serves other purposes and, above all, because it is an extract of the auditory experience in freely progressing music; whereas our melody-models, in their utmost distilled purity and "germ-freedom," have scarcely anything to do with living music. The degree-progression does not follow with unalterable will the unyielding linearity possessed by the melodic model. It expresses in a much stronger way than the latter the coherence to a tonal center (Φ) and it utilizes means for this which would markedly restrict the progression of a model. These means, however, on account of this very restriction, adapt themselves well to determining certain tones (centers, dominants) definitely. They are: tone-repetitions; auxiliary tones (W), in fact any tones recurring several times; sequences and broken triads, under certain conditions; long successions of step-progressions (but omitting, for the present, chromaticism); long retention of a single pitch direction. Broken tritone chords are to be avoided; the one exception to this is yet to be mentioned.

Let us now, in this sense, consider Figure 139. A two-fold appearance of the tone-group bb–a (tones 6–9) would have been impossible in a melodic model on account of its melodic redundancy. Here, on the contrary, it is not only permissible but also desirable because it helps to determine the Φ with the aid of the Φ. Degree-progression, accordingly, is to be conceived as a pre-stage of melodic life, a budding something before the birth of melody, a pre-pattern of melodic motion, not in itself developed to an independent linearity. On the other hand, it possesses a mobility which is not appropriate to the melody-models; it is entirely dependent in its rhythmic structure upon the sounds which occur above it, and thus, like these, utilizes all note-values. We should not demand, in spite of this, an independent melodic existence of a degree-progression, since this should gain its effect neither through beauty and power of expression nor through interesting voice-leading. It serves entirely as a re-check on the value of the harmonic flow; if it is a clear-cut, well built, and logically developed linear pattern, then the harmonic successions must necessarily be equally convincing (only harmonic successions; other errors of writing and awkward progressions are not thereby eliminated).

We can recognize correctness and logic of the degree-progression, in

spite of the intentional elaborations, by the extent to which it accords with our strict demands for constructing melodic models.

The degree-progression is the practical development of the rules of relationship as formulated in Series I. If a harmonic progression is to be comprehensible, then the degree-progression underlying it must use the relationships to a source-tone in an understandable manner.

RULE 55.

The degree-progression groups itself around a tonal center or source-tone (Φ), which is determined:

a) through several appearances of a tone
b) through support of the Φ, and in second place through support of the Φ of the source-tone.

If only the subdominant is the support, the danger exists that the tone representing it in the degree-progression will gain in importance and increase the Φ to a Φ by using the original Φ as its own supporting dominant. The intended Φ must, therefore, be strengthened sufficiently to neutralize the effect of the Φ. The related tones which in Series I follow the Φ have but little significance in our two-part setting as support of the Φ. Thus we use them merely as parts of the melodic line built by the tones of the degree-progression.

RULE 56.

The first and last tones of a degree-progression are particularly significant. The formal weight of both is even more important for the coherence of the tones than is the confirmation of the Φ by means of recurring tones within the degree-progression.

For this reason, in the two-voice exercises, the first and the last tone of a degree-progression should always be the same. The degree-progression should be so arranged that these tones form the Φ.

In Figure 139 we note that the d¹ occurs three times in the degree-progression; the bb also occurs three times. But since the d¹ is emphasized as the first and the last tone, it is more important than the bb, and it thus becomes the Φ of the degree-progression and, consequently, the Φ also of the entire setting built over it. The piece is in d¹. The two notes a (tones 7 and 9 in the example), appearing twice as next related tones to d¹, are the strongest dominant support for the Φ. They, in turn, are supported by the re-
motely related two $b^7$ (tones 6 and 8) which, in this capacity, serve good melodic purposes (as neighboring tones).

The $\Phi$ of Figure 140 is $f$, since this tone is the first and the last tone and is further strengthened by the $\Phi$ (second tone of the example) and the $\Phi$ (eighth tone). The $a$ which occurs three times does not operate against this, since the $a$ stands in a less favorable position and is not supported by either its $\Phi$ or its $\Phi$.

In Figure 141, $f$ is likewise the $\Phi$, best supported by its $\Phi$. This example teaches us something new:

**RULE 57.**

The tritone progression may occur in a degree-progression if it appears as a constituent part of a sequence (Figure 141, tones 2 and 3), or if one of its tones appears as neighboring tone of a 5 or a 4 progression.

In Figure 141 we note an especially important and effective tone succession in the last three tones of the degree-progression. By means of this the $\Phi$ is determined with remarkable definiteness. This is one of several patterns functioning in the construction of degree-progressions and the harmonic progressions built upon them. They are similar to the melody formulae used in melodic progressions. They are chiefly adapted to the creation of endings, since they definitely determine the $\Phi$, and we call them cadences. A cadence in a degree-progression consists of at least three tones, of which the last is always the $\Phi$. The other two tones drive forward into this last tone. For the closing effect of a cadence, the relationship among the three tones (of its degree-progression) is of the utmost importance. If the $\Phi$ precedes the $\Phi$, and either the $\Phi$ precedes the $\Phi$ or else the $\Phi$ is preceded by its own $\Phi$, we obtain the strongest possible cadence.

The further the relationship between the next-to-last tone and the $\Phi$ is removed, the weaker does this final cadencing progression become. The strength of the cadence-beginning, on the other hand, is in the highest degree dependent upon the relationships existing between it and the remaining two tones of the cadence pattern. The interplay of this relationship among the three cadence tones permits the construction of the most diverse closing formulae. Besides the formula already mentioned, $\Phi \Phi \Phi$, which strives accurately and directly toward its goal, there are formulae which begin very weakly and then suddenly pitch strongly toward the final tone, such as:

or others, which reach the next to the last tone with the full strength of a descending fifth (or ascending fourth) and then proceed with a harmonically meek, feeble step to the final tone.

In Figure 146 we have all possibilities of cadences with the $\Phi$ before the $\Phi$.

For practice we shall now use four tones in constructing cadences, and shall make the first and the last tone the same, in order that the source-tone
may be more clearly recognized. The tonality is thus revealed to the student unmistakably through this double appearance of the θ.

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**EXERCISE 38**

Write, in similar manner:

a) on the θ Eb all cadences which have the θ before the final tone,
b) on the θ F# all cadences with the 3d-related tone before the final tone,
c) on the θ B all cadences with the 4th-related tone before the final tone,
d) on the θ Db all cadences with the 5th-related tone before the final tone,
e) on the θ A all cadences with the 6th-related tone before the final tone,
f) on the θ F all cadences with the 7th-related tone before the final tone,
g) on the θ Ab all cadences with the 8th-related tone before the final tone,
h) on the θ Bb all cadences with the 9th-related tone before the final tone,
i) on the θ G all cadences with the 10th-related tone before the final tone.

The cadences which show the eleventh tone-relationship before the final tone are to be avoided until later.

---

The cadence is a device of tone-setting in which harmonic energy is most intimately linked with rhythmic-formal energy. These two forces, without regard for other factors, strive directly toward their goal, compelling all others to pass into the background. The melodic energy, above all, must yield to them. Thus, in the cadences, we cannot be concerned too much with the demands of the most careful voice-leading. We have already seen that covered octaves and fifths in cadences may be advantageous (Rule 26); whereas in free and non-cadencing progressions they are poor and undesirable. The same condition holds for other setting “errors.” In three-voice and more-voice settings the cadence can assert itself so strongly that all rules of voice-leading are suspended. For the present, however, it will suffice to help the cadences to assert their rights by making several things easier. Thus, in the degree-progressions of the three-tone cadences we shall permit: broken tritone chords, diminished and augmented steps into the first cadence tone, and diminished or augmented steps between first and second cadence tones. We always assume, of course, that the two-voice setting built upon these tones follows its rules.

The statement is often made that all harmonic progression is nothing more than an extended or elaborated cadence. This, like all such statements, is only partly true. Nevertheless, the cadence is such an important part of the supply of materials for tone-setting that by linking several cadences, entire pieces can be filled out harmonically; moreover, in its formal integrity the cadence is a dependable architectural part, always ready at hand to help round out difficult and unpolished sections. Above all, the student can always lean and depend upon it. For this reason, cadences expressed by means of the degree-progression are here granted relatively full treatment, although in a two-voice setting a cadence cannot be developed to full auditory and harmonic effectiveness.

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**EXERCISE 39**

According to the preceding models (these are the two-voice forms of the cadences a and b of Figure 146) add to the degree-progressions (cadences) of the preceding exercise (38) an appropriate two-voice setting. It will be sufficient if only the first two cadences of the exercises a to i are worked out. It is not necessary, this time, to distinguish between the model and the 2d voice in this two-voice work. The final interval of each cadence should be considered as the ending of a two-voice setting; it must, therefore, follow the familiar rules for an ending. The first interval, on the other hand, is treated as if it occurred in the course of a setting; it may thus appear as (1), (2), or (4).

If one attempts to execute in a two-voice setting all the cadence step-progressions mentioned in Exercise 38, one soon realizes that a large number of them cannot be formed with our limited material of note against note without violating rules 6, 10, 12, 13, 20, 22, or 23. These are those which contain: (a) a chromatic progression; (b) a tritone; or (c) another augmented or diminished interval in their
four-toned degree-progression. Several among these can be solved according to rule; others, especially those under (b), will usually result in the formation of a four-toned seventh chord divided between the two voices, which, following Rule 21, is to be dispersed over separate octaves.

**EXERCISE 40**

Construct degree-progressions in whole notes (without working them out in two voices) of which the $\#$ is determined at least by the first and the last tone, and end them with a three-toned cadencing progression.

The cadence may consist also of more than three tones or harmonies. That occurs in more extended settings than ours, when the approach to an end of a section demands an extended verification of a close. Such a longer cadence moves more and more from its predominantly harmonic significance with the increase in the number of its degree-progression tones to a stronger formal function (the technical mastery of which, however, we do not attempt in the present work); none the less, even then, one of the three-tone successions of the degree-progression, such as we have learned and practiced in Exercise 38, will always form the close. We shall therefore restrict ourselves to these three-tone cadences.

**EXERCISE 41**

Work out the degree-progressions of Exercise 40 into two-voice settings, note against note.

One of the two voices in this case is to be considered as melody-model, and, accordingly, must follow the rules applying thereto. The other voice meets the rules governing a 2d voice. For some degree-progressions, even after diligent search, no two-voice setting which meets all rules can be developed. In such a case the degree-progression should be altered at the impossible points. The importance of this exercise consists less in the absolute two-voice execution of the degree-progression than in the experience, acquired in working it out, of the mutual dependence and influence of the degree-progression and the developed setting.

**C. Model Examples**

The work with simple degree-progressions can be completed by extracting these successions from settings in which one voice has been made active through the use of melodic formulae. This is not difficult if we first ascertain which are the formulae in the active voice of a two-voice setting.

These formulae have no significance for calculating the degree-progression, since, as mere additions, they stand beyond the chief and significant intervals. Hence they are not considered. Thus we derive the following rule.

**RULE 58.**

Degree-progression and designation of the melodic formulae are mutually exclusive. Each tone not provided with a formula symbol belongs to an independent interval, the root-tone of which must appear in the degree-progression.

Thus we can realize how far it is advantageous, in analyzing ambiguous cases, to use the $N, N', N$, and other formulae to simplify and shorten the calculation, instead of assuming too many independent intervals. The degree-progression thereby receives a simpler rhythmic form, and thus its harmonic relationships become simpler and are more easily surveyed. The degree-progression of Figure 148 thus assumes the following appearance.
EXERCISE 42

a) What is the $\Theta$ of Figure 148?
b) Why is it the $\Theta$?
c) How often is it supported by the $\delta$?
d) How often by the $\varphi$?
e) Why has the third measure of the degree-progression a rhythm different from that of the other measures?
f) What would the $g'$, measure 3, have to be called if the $b_b$ of the degree-progression were held unchanged?

In formations such as measure three of the preceding example one can facilitate the work by representing all tones of both voices which are grouped by the ear as belonging to a triad or simple seventh chord by a single tone of the degree-progression. In measure five, in this manner, the $g$ of the lower voice and the $d^2$ and $b_b^1$ of the upper voice can be combined into a triad; the $g$ then remains as the tone of the degree-progression. In measure six the same holds for the tones $b_b^1$, $d^2$, and $f'$, with the tone $b_b$ of the degree-progression. In measure three, the tones $d^1$, $g^1$, and $b_b^1$ produce a triad harmony with the new root-tone $g$.

If we take this tone as the tone for the degree-progression for the entire third measure, the more complicated calculation of the degree-progression which we have just applied does not hold. The question whether or not it is always appropriate to indicate triad- and seventh-chord harmonies in the degree-progression by their root-tones, or whether one should prefer to draw solely upon the root-tones of A-intervals, cannot be decided completely. In general it is advisable to choose chord groups as main carriers of the harmonic content; only where more complicated melodic or harmonic progressions make a more detailed degree-progression desirable, should the consideration of the smaller details be applied. Needless to say, in both cases the degree-progression must show the familiar logical development. In the following example we find chord formations of this kind, with the accompanying simplified degree-progression in measures five and seven; and the same in measure six, if the $c^\#$ of the lower voice is conceived as the harmonic complement of $f^\#=a^1$ and not as a part of the detached A-interval $c^\#-a^1$.

In this example our entire work up to this point passes in review. The first two lines show the two-voice setting, note against note. In line C the 2d voice is supplied with melody formulae and is appropriately marked. Line D shows the harmonic fields contained in the active voice (of the cells only the more important are indicated, since the others are already contained in the fields). In line E we see the step-progressions indicated. The last line, F, is the degree-progression.

EXERCISE 43

a) Name the $\Theta$ of Figure 150.
b) Is it supported by the $\delta$? How often?
c) By the $\varphi$? How often?
d) Could $b$ also be the $\Theta$?
e) Change the fifth measure of the active voice in such a way that the degree-progression could hold a whole note.
f) In the seventh measure, in case the $b$ of the degree-progression, since this is the third appearance of the $\delta$ support, seems to appear too frequently, $d$ could appear in the degree-progression. What course would the active voice then have to take?
EXERCISE 44

a) Take the two-voice settings, note against note, of Exercises 42 and 43, and write active 2d voices by means of melody formulae, producing melodies other than those given.

b) Supply the new melodies with the appropriate symbols.

c) Designate the harmonic fields; the step progressions.

d) Extract the degree-progression.

e) Judge each detail; improve, when necessary; sing the whole exercise through.

Two more examples follow, from which we can learn how the degree-progression can develop from a means for ascertaining the purity of a setting into a highly useful help in practical writing.

The 2d voice of this example is stupid and bare. Nevertheless, by the singing of both voices we shall not be as much offended as we might expect with such an upper voice. That is caused by the degree-progression, which is well developed. In spite of its feeble cadence (eb-g-a) it fixes the Θ unequivocally, and shows the near and the remote relations of the tonal center in well balanced distribution. Only the θ is not represented. If we wish to give the restricted setting more strength by introducing the θ, this can readily be done with a slight change.

This form is decidedly more alive and beautiful. If we construct the upper voice according to the demands of this progression (the lower voice needs to substitute only one note) we get a usable setting.

In this manner any two-voice or more-voice setting can be examined and improved even when it appears in rhythm and is supplied with melody formulae and rapidly changing harmonies. In the last notes of the example we see the extent to which a logical degree-progression can influence the total progression of a setting: the cross-relation ab-a1 is possible and even effective because it is carried by the leading of the degree-progression and because (as in the cross-relation of Figure 152) the two sensitive tones have different functions: the one is root-tone of the interval; the other solely the tone completing the interval.
CHAPTER VIII

Tonality of the Melodies

If we have understood well the nature and the manipulation of the degree-progression, Chapter VIII should offer but little difficulty. In it we shall attempt to ascertain how the harmonic groups contained in the melodies regulate their order, and, in doing this, we shall use the determination of the degree-progression. This will lift the last veil from melodic and harmonic procedures in two-voice settings in so far as we can comprehend them in the technique of tone-setting.

A. Work-Material

An example from Chapter V will serve as a study model; later on we shall consider others of the already completed melodies. The melody-models are superfluous in this chapter and they are not used.

B. Work-Procedure

We have extracted the degree-progression from two-voice settings. We know already that the two successive tones of a broken interval have the same harmonic value as the same two tones sounded simultaneously. It follows, therefore, if it be a question of the broken intervals of Group A of Series II, that we can extract a degree-progression also from them, and that this degree-progression, like the one drawn from the intervals the tones of which sound together, must indicate whether or not the tensed harmonic values contained within the broken intervals of the melody follow in logical order. The premises for establishing such a degree-progression are found in the harmonic cells of the melodies. To learn whether or not the extracted tone succession meets the demands of logical linear development and can serve as indication of the harmonic logic in the melodic progression, we have only to select the root-tones and align these in succession. It would be very troublesome, however (and, as we saw in the first study of cells, also misleading), to collect all possible cell structures according to root-tones, in the course of an entire melody. That is not necessary, for the cells are often contained in the harmonic fields. It suffices, therefore, to study the latter and to select the cells only where no further grouping into a harmonic field occurs.

But how are we to find the root-tone of a harmonic field? Harmonic fields are formations of three or more tones, the separate tones of which sound successively instead of simultaneously. We must, therefore, first learn how the root-tone can be found in these harmonic formations before we work with them. This is done according to a very simple rule:

RULE 59.

In triads or polyads the root-tone of the best interval contained within them is the root-tone of the entire formation.

The value of the intervals, as we have long since learned, is determined according to the order of Series II; and to determine the best interval of a chord, each two-tone combination contained within it is considered, not merely those intervals made with the root-tone or the bass-tone. The major triad, accordingly, contains: 5, 3, 2. Its best interval, according to the values of Series II, is the 5; therefore the lower tone of this interval is also the root-tone of the triad.

"In order to learn this, do we need such a complicated calculation? We knew it already. The position of a triad in the diatonic scale gives us quicker and more dependable information." We grant that our explanation for the major triad seems circumstantial to the inexperienced—so long as he is not used to it! As a matter of fact, it is really simpler, since it neither considers the relationships to tonally central tones as points of departure, nor works with inversions of the chord tones or with their multiple meanings. The determination of the root on the basis of "best interval" is unchanged for all forms and positions of simultaneous sounds, and only because it fits all the numerous "polyads" can we employ these intelligently and purposefully. Many of these are far removed from the normal consonance of the triad, and no other text-book contains any practical suggestion as to the application of these (non-triad) forms.

For the minor sixth-chord—as an example, e-g#-c#—the following interval relationships hold: ① (e-g#); ② (g#-c#); ⑥ (e-c#). The best interval is g#-c# and, accordingly, the root-tone is c#. (which, of course, in order to fit into a degree-progression may be transposed an octave, if desired).

For the determination of the best interval of a sound-pattern, it is im
material whether its two tones are in the closest pitch position, or are separated by one or more octaves. Thus, in the three major triads of Figure 156 the twelfth (♯12) or even its higher octave, counts as a ♭5.

and the ♭5 g♯-c♯1 in the above mentioned sixth-chord can occur as G♯-c♯, G♯-c♯♭, g♯-c♯, or in other octave transpositions; it will always be figured as a ♭5. The octave transposition of all other intervals contained in a chord are figured, for the sake of simplification, as if they occurred in the closest position.

If the best interval occurs twice in a chord, whether as true octave doubling of two tones (for example, the repetition of the ♭5 A-e as a1-e1) or if it is transposed to other scale degrees (the two fifths A-e, c1-g), the root of the chord will be the root of the lower interval.

EXERCISE 45

Determine the root-tones of the following tone-combinations.

It is evident that broken chords in widely dispersed positions cannot occur in our melodies. They are given here merely to illustrate further the principle of the root-tone.

Formations such as

![Formation](image)

even with a considerable number of tones are not to be considered chords, but merely intervals with one or more of their tones doubled.

RULE 60.

For the following four combinations

![Formation](image)

and their broken forms (with or without doublings of one or more of their tones) no root-tone exists. When they are used in harmonic work (where they are still prohibited to us) or in melodies, we may select any of the tones for the degree-progression. Naturally, that tone should be chosen which best fits into the surrounding tones of the degree-progression.

We can understand the absence of a root-tone in these tone-combinations if we keep in mind the peculiarity of the tritone which has already been mentioned, and the separation of this interval from other intervals. No root-tone can be discovered in the tritone. Either it is considered neutral, without a root-tone, or we concede root-tone position to one or the other of its two tones. All other intervals can be inverted into other intervals with oppositely placed roots. Inversion of the tritone produces merely another tritone. Do what we will with this interval, it will always remain ambiguous, indefinite, vacillating. Only when it leans upon other intervals, when, for example, it occurs as a ♪ to a 5 or a 4, does it gain in definiteness. But if we go further and give to this half-genuine, shifting interval a definite place among chord-formations, we experience the full unbridled character of its barbaric, untamed nature, which usurps the whole field, instead of taking its appropriate little corner, and then lives in the tonal field with a delusion of grandeur. It lends goal and direction.
to the polyclangs which contain it, makes them keen and stimulating, robs them of all rest and self-assurance, and furnishes them, in spite of its incisiveness, with a flexibility which may be shifted into the most risky paths or the closest narrows, without fear or hesitancy.

The tritone operates in the polyads like a fermenting sour dough. All chords harboring it are opposed to the remaining chords, partly through their tension toward a goal, and partly through their lack of self-sufficiency. They are completely different in their nature. Since the diminished chords in question (Figure 160) contain the tritone as their chief component, it is not surprising that they detach themselves from the remaining “normal” chords. In the exercises for three-voice setting, further remarks about the tritone and the diminished chords will be found. Here it is sufficient to learn the most important points in employing these lone wanderers among the other sounds.

We come now to the treatment of the polyads distributed in the melodies. Even the smallest of these, the cells, often cannot be exactly or clearly bounded. Naturally, then, it is even more difficult to differentiate sharply the harmonic fields, these larger dispersions or broken forms of polyads. For one hearer a certain group may combine into a harmonic field; for a second hearer another group may do so; yes, even the same listener will not always decide in the same way. However, one almost always finds the grouping into broken triads sufficient; seventh chords can always be subdivided into several triads, and if a certain tone-figure is ill-adapted to harmonic grouping, the subdivision into cells always remains. By this means the group is always grasped with certainty.

RULE 61.

The degree-progressions extracted from the harmonic fields, or, where necessary, the cells, must produce a meaningful musical line. In order to distinguish this line from the former degree-progression (produced by the roots of the intervals with their tones sounding simultaneously) we shall call it melody degree-progression.

Meaningful here means again: in accordance with our first fundamental melodic laws, account being taken of the amendments mentioned in connection with the degree-progression of the harmonic intervals.

It may happen also that the sole content of a part of a melody is a step of a second; or that, because of the metrically favorable position of such a progression, a clear perception of harmonic cells or fields is made very difficult, if not impossible. The step-progression, in such cases, is so strong and unambiguous that the degree-progression cannot effectively oppose it. Then we simply take over the tones of the step-progression into the degree-progression.

If we extract the root-tones of the harmonic fields in Model Example I of Chapter V, and then supply the remaining places with root-tones of the cells, we shall produce the following degree-progression, which, in view of the preceding remarks, may appear different in regard to some details, but, even then, should show a logical progression.

The small note-heads indicate where, besides the main cell- and field-groupings—the root-tones of which are given in the whole notes—other less important cell structures are to be heard. The tonal center, with or without these insertions, is $g^1$; although the melody degree-progression does not begin with this tone. Nevertheless, the $g^1$ is $\Phi$ and comes at an important middle point. Above all, it is twice reinforced by its $\delta$ and once by its $\varphi$. One must not be misled, in considering such tonal bonds, by the tonality concepts growing out of the diatonic major and minor scales. Such a concept would assume several modulations, but even then it could not completely take care of this harmless little melody. Tonality, as we understand it, grows out of the chromatic scale as building material. A melody is in $G$ not because an $f^\#$ occurs therein, and a melody must not be in $C$ because the tritone $f-b$ occurs significantly in it. The degree-progression gives a much better knowledge than any key-signature or chord contrasts. Of course, it teaches us also that tonal formations vary widely in the definiteness of their construction. Thus the tonal center $g^1$, at the beginning, where the actual $\Phi$ does not appear, is but weakly identified; it develops only in the course of the melody. If we wished a stronger center ($g^1$), we should merely have to adapt the melody degree-progression more to this tone.
and then to alter the melody accordingly. (With this procedure, however, the step-progression and certain changes in it would also have to be considered.) For example

\[ \text{Example 1 (from Chapter III).} \]

We know that the degree-progression of this melody is developed properly; we know the same thing about the step-progression of the melody from Chapter V. Therefore, the melody is correct, is logically constructed, and is thus of practical usefulness. This does not mean that it is also beautiful, moving, soulful. We can never rise into the domain of aesthetic evaluation with the technical materials with which alone a text-book is concerned, nor may we do so if we wish to learn the objective properties of the tone-material. Once we have mastered this we have complete freedom in applying it according to the dictates of joy, sorrow, depressed or ecstatic moods. For the present we should be satisfied if our work shows the greatest possible logic of construction; so much the better if it is also pleasing and expressive.

The harmonic contents of the cells and fields expressed in the melody degree-progression are, for the present, completely independent of the harmonies, which are produced by the addition of one or more voices to a melody. The ways of the logic of melody can readily coincide with those of the harmonies; often, however, they do not do so. In constructing the melody degree-progression, therefore, we must not think about what else may sound above and below the melody. The manner in which the melody is to be wedded to the harmonies, how melody degree-progression and harmony degree-progression are related to each other, will be treated in later chapters.

In further explanation of a topic mentioned in Chapter V, we should add that the present harmonic independence of a single melodic line in relation to the contributing harmonies naturally determines also the melodic significance of its individual tones. That which is a D or an N or some other melodic formula in relation to a 2d voice can be a chordal component of a harmonic field when the melody is separately considered; and, conversely, that which appears in the separate melody as W N or other relaxing of the fixed harmonic groups can become a main part of the total chord through its absorption into the simultaneously sounding tones.

C. Model Examples

We shall now examine, for their melody degree-progression, all active voices thus far written.

\[ \text{Example 1 (from Chapter III).} \]
The \( \Theta \) is not worked out very exactly. In the first five notes the \( c^2 \) is \( \Theta \) without a doubt; this tone stands at the beginning, occurs once again, and is supported by its \( \delta \). The close is ruled by \( a^1 \), which is strengthened by its \( \phi \). To speak of a change of \( \Theta \) (modulation) is not necessary with the scant use of harmonic means and the obvious weaker presentation of the \( \Theta \) \( a^1 \). Therefore, the \( c^2 \) is to be considered the \( \Theta \) of the melody.

EXAMPLE 2 (from Chapter III).

A simple case. The \( \Theta \) is \( c^1 \), supported by \( \phi \) and \( \delta \). In the first two measures the step-progression is stronger than the degree-progression \( c^1-d^2 \).

EXAMPLE 3 (from Chapter III).

EXERCISE 46

Take, in order, all active voices of the exercises of Chapters III, IV, and VI, extract the melody degree-progressions, and determine the \( \Theta \) of each.

EXERCISE 47

a) Write a melody model according to the rules of Chapter I.
b) Place above or below it a 2nd voice according to the rules of Chapter II.
c) Extract from the intervals the harmonic degree-progression and determine the \( \Theta \). Improve the melodic progression in case the degree-progression is unsatisfactory.
d) Use, as desired, melody formulae in the second voice.
e) Determine the step-progression of the active melody and improve it in case defects appear.

Take care! Improvements are followed by changes in the harmony degree-progression; after each melody change, therefore, the harmony degree-progression must be tested, and, if necessary, the harmonic intervals must be fitted to the melody. It follows from this that changes may occur in the melody model as well as in the first draft of the 2nd voice. In thus giving in to the ornamented melody, we depart somewhat from the original two-voice setting note against note. That does not matter; it serves us well for the setting up and first draft of our tonal structure; but the living effect of the melodic and harmonic progressions is now more important for us than barren adherence to the first aids.

f) Determine the harmonic fields of the active melody; extract from them (with the aid of the cells and, if necessary, the step-progression) the melody degree-progression; improve here, too, the active melody, if the melody degree-progression demands it (here the remarks under e also apply).

In this exercise everything is collected that we have learned and tried out in Chapters I to VIII. It does not suffice to solve it only once. We may demand of a student who sees his chief field of work in really learning tone-setting, that he work out at least ten different solutions. But even the students who have but little time for their exercises in tone-setting should work through four or five forms of this exercise.
CHAPTER IX

Elaboration of the Melody Model

In the last problem of Chapter VIII it was necessary for the first time to adapt the melody model to other requirements of the setting. The original inflexible rigidity of the basic melody thus began to waver, even if only very slight shifting were involved. That need not be surprising, for in the meantime we have learned about that force in the field of tonal motion which basically rules the harmonic and melodic patterns. This is the degree-progression, containing, as a matter of fact, the unimpeachable exactness, stability, and unerring neutrality which in the light of our newest experiences we must deny to the melody model itself. And, since we have thus begun to shake the supports which were necessary at the beginning, and which, in the meantime, have been supplemented, surpassed, and outclassed by the firmer building material of the permanent mould and supporting structure, we shall go a step further: the melody model itself is now to be changed into more fluid motion. What we have had before (Chapter II), namely, the simultaneous progression of two similarly constructed, equally important voices, we again attempt to achieve now on a higher plane, where we shall no longer be confined by the exact restrictions which there hindered our progress.

A. Work-Material

For the last time we shall use the settings note against note, constructed on a melody model progressing regularly in whole notes. At first we shall rework the settings of Chapters III, IV, VI by activating the passive melody model as we did the originally inactive 2d voice. Then, starting from newly written note-against-note settings, we shall set both activated voices against each other.

B. Work-Procedure

The assurance which we have already gained by working with the various elements of a two-voice setting (harmonic values, melody formulae, step-progression, melody degree-progression, harmony degree-progression, tonality) will keep us from seeing any essentially new or particularly difficult problem in handling two active voices. In this chapter, as in the last two chapters, the chief object is not so much the use of new work material or the acquisition of further knowledge. It is rather a question of freer ways of applying the given elements. The model melodies of Chapters III, IV, VI contain two voices of different degrees of tonal motion. If, now, we proceed to activate the passive voice, as we did the added voice in the preceding chapters, we reverse the original relationships. The active 2d voice is our guide-line for this chapter; along this we feel our way, joining to it the newly activated voice. The two voices, however, retain their former designations throughout the exercises. Thus we attach to the old melody model its original name (model) even when it has long since given up this position to its partner (2d voice) through its elaboration.

The melody model is elaborated into an active form in exactly the same manner that the 2d voice was previously elaborated: by supplying it with melody formulae. The original whole-notes of the model remain nucleal tones in the newly activated voice, just as those of the 2d voice previously did. All rules which, from Chapter III on, affected the course of an active voice, here apply to the model which is to be made active. Only a few remain of the rich assortment of rules governing the simultaneous progression of both voices, because of the freedom permitted as a necessary consequence of our greatly extended work-material.

These are:

Rule 16: No voice crossings;

Rules 18, 19: No intervals with root tone above as beginning, end, or important point in the course of the piece;

Rule 24: No $5^\#$, $7^\#$, and $6^\#$-parallels;

Rule 25: Covered $6^\#$- and $4^\#$-parallels only as closing formulae; for these, special rules;

Rule 27: Covered $6^\#$- and $4^\#$-parallels from below are prohibited in case they proceed from intervals smaller than the final interval;

Rule 29: No leaps from intervals of Group B (and the tritone) or into such intervals (exceptions: $N^\#$, $N$, $F$, $F$);

Rule 30: Care is to be taken with seventh and ninth formations in active voices.

All earlier rules of lower number do not count, or else they apply in the broader form stated in Chapter III, page 45. The rules from No. 31 on
already concern the progression of two active voices and are now suited to the student's greater dexterity in writing. They therefore retain their value.

A few other things, however, should be observed in the simultaneous leading of two voices.

**RULE 62.**

If one voice moves, keep the other quiet.

This broadly stated admonition may be disregarded in favor of simultaneous livelier motion or mutual tranquility of both voices, when the harmony degree-progression, or the strong striving for high and low points, or even the desire for heightened expression, makes necessary an equal apportioning of activity to both voices. The over-weighting of up-beats is especially striking; in most such cases equal rhythmic tension of the two voices is not attractive.

The working out of an example from Chapter III,

![Example](image)

will acquaint us with the new procedure better than any theoretical explanation.

![Example](image)

This solution is poor; instead of supporting the upper voice by means of a contrasting, active voice, the elaborated melody model here parallels the other in rhythm; besides, it is overburdened.

Here we have the overladen up-beats already mentioned; instead of a smooth progression we experience a panting, staggering effect. Let us try, therefore, some quieter rhythms!

In the first measure no tone higher than $f^1$ can be used on the last quarter (on account of the real or covered (5)-parallels, which result from the progression into the model tone of the 2d measure) except $b^1$ or $c^2$, neither of which, however, represents an ingenious solution. There remains the approach from below:

![Approach](image)

The form d again shows a kind of weighting of the up-beat which we wish to avoid; the form c, through its strong accentuation of the second quarter, brings restlessness into the setting which is not at all appropriate to the modest expression of this little exercise. The two following forms are not possible:

![Forms](image)

the first on account of the tritone leap ($b-f^1$) into the model tone of measure 2; the second on account of the cross-relation between the $b^1$ of measure 1 and the $b^1$ of measure 2, which here would be definitely disturbing. We prefer, therefore, for the first measure, one of the forms a or b of Figure 173, against which nothing can be said. For ornamenting the second measure, the following two versions result:

![Ornamentation](image)

and their derivatives

![Derivatives](image)

In a, we retrace a part of the way that we have traversed; this does not give much variety; the return over $eb^1$, accordingly, is to be preferred
(in spite of or just because of the cross-relation to the first and the third measure of the upper voice). The cross-relation \( e^2 - eb^1 \) does not disturb here, because \( eb^1 \) has merely a D-character.

Even if the \( eb^1 \) should count, not as D but as constituent of an independent interval, this tone is not very forceful, since it is not the root-tone of this interval. Also the \( e^2 \) which completes the cross-relation is not the root-tone of the interval to which it belongs; it is the root-tone and degree-progression tone \( c^1 \). Obviously, a tone standing at the weaker place in an interval can never manifest itself as strongly, whether in a good or a bad sense, as the tone standing at the more forceful place. The cross-relation \( e^2 - eb^1 \) thus in no case can be as disturbing as the just mentioned cross-relation \( bb - b^1 \) (Figure 174b), in which the \( bb \) appears as root-tone of the diad. To prove this statement: use the \( bb \) in the first measure so that it becomes less important, and no disturbing cross-relation will occur.

In Figure 178b the \( bb \) is but for a moment the root-tone of \( bb - f^2 \), where the D sounds together with the W. The \( bb \), however, has all the earmarks of a D as distinctly as the \( f^2 \) bears those of a W; the root-tone function of \( bb \) is thus scarcely noticed.

The versions c and d from Figure 176 are usable for the second measure; e and f are not bad, but they are rhythmically linked too closely to the upper voice and are, therefore, less suited. The remaining three forms, on account of their triplets, introduce too much restlessness.

In addition the following forms are possible:

Of these a and b are good, c less good on account of the covered \( b^3 \) parallels to the third measure. The ornamented lower voice for the third measure may be:

Of these a, again, is poor. It contributes nothing other than what is contained in the upper voice and, because it produces merely a decoration of the \( d^1 \), it creates a halting of the general development. The forms i and k may serve only if they can be fitted smoothly into the total progression; f and n form octave parallels \( (d^2 - c^2 - d^1 - c^1) \) with the upper voice. Although these do not occur exactly at the same time, they become more noticeable for that very reason.

**EXERCISE 48**

Write out in the manner indicated all possibilities of a freer movement in the melody model, using the remaining four measures of Figure 170. They should agree with our rules and should be judged on the basis of fitness.

We shall decide in favor of the following version of the melody model. This agrees with the simple style of the upper voice and maintains a pleasant mean between meagre dullness and note-rich "gossip."

The greater facility which we have acquired permits the use of the following quite daring tone-groups in the course of two active voices:

a) all previously forbidden or only conditionally permitted prepared or unprepared suspensions, e.g.:
Also, several pseudo-suspensions:

\[
\begin{array}{cccc}
\text{\textbackslash{}textbf{V}} & \text{\textbackslash{}textbf{N}} & \text{\textbackslash{}textbf{N}'} & \text{\textbackslash{}textbf{V}} \\
\text{\textbackslash{}textbf{V}} & \text{\textbackslash{}textbf{N}} & \text{\textbackslash{}textbf{N}'} & \text{\textbackslash{}textbf{V}} \\
\end{array}
\]

may be considered suspensions if a perceptible \textbf{V} effect is created by them. The formation of the degree-progression is thereby simplified. If no real \textbf{V} effect can be determined, it is better to apply the more detailed but dependable degree calculation, according to which each of the intervals gets one tone of the degree-progression.

The connection resembling a suspension, \textbf{V} \textbf{N},

\[
\begin{array}{cccc}
\text{\textbackslash{}textbf{V}} & \text{\textbackslash{}textbf{N}} & \text{\textbackslash{}textbf{N}'} & \text{\textbackslash{}textbf{V}} \\
\text{\textbackslash{}textbf{V}} & \text{\textbackslash{}textbf{N}} & \text{\textbackslash{}textbf{N}'} & \text{\textbackslash{}textbf{V}} \\
\end{array}
\]

may be used provided that the harshness of the sound does not disturb the progression of the setting. It is clear that such a tone-group, which even prepares its highly tensed \textbf{N} interval with another highly tensed interval, can never exert the normal effect of a \textbf{V} with its attractive principle of construction: preparation-tension-resolution.

b) A combination of \textbf{V} and \textbf{N}, which occurs frequently.

\[
\begin{array}{cccc}
\text{\textbackslash{}textbf{V}} & \text{\textbackslash{}textbf{N}} & \text{\textbackslash{}textbf{N}'} & \text{\textbackslash{}textbf{V}} \\
\text{\textbackslash{}textbf{V}} & \text{\textbackslash{}textbf{N}} & \text{\textbackslash{}textbf{N}'} & \text{\textbackslash{}textbf{V}} \\
\end{array}
\]

In the case noted here it is possible, instead of \textbf{V} and \textbf{N}, to assume a root-tone for the interval itself, which, after what has been said in the preceding chapter, can be either of the two tones of the tritone (here the \textbf{b} is the better).

c) The following connection of \textbf{V} and \textbf{N}',

\[
\begin{array}{cccc}
\text{\textbackslash{}textbf{V}'} & \text{\textbackslash{}textbf{N}'} & \text{\textbackslash{}textbf{N}'} & \text{\textbackslash{}textbf{V}'} \\
\text{\textbackslash{}textbf{V}'} & \text{\textbackslash{}textbf{N}'} & \text{\textbackslash{}textbf{N}'} & \text{\textbackslash{}textbf{V}'} \\
\end{array}
\]

in which the resolution of the \textbf{V} takes place, not by step, but, as with \textbf{N}', by leap into a tone that forms an A-interval with the other voice.

\[124\]

\[d) \textbf{V} \textbf{V} \text{ and } \textbf{N} \textbf{N} \text{ which occur on weak beats with clearly marked syncopation of the opposing voice.}
\]

\[
\begin{array}{cccc}
\text{\textbackslash{}textbf{V} \textbf{V}} & \text{\textbackslash{}textbf{N} \textbf{N}} & \text{\textbackslash{}textbf{N} \textbf{N}} & \text{\textbackslash{}textbf{V} \textbf{V}} \\
\text{\textbackslash{}textbf{V} \textbf{V}} & \text{\textbackslash{}textbf{N} \textbf{N}} & \text{\textbackslash{}textbf{N} \textbf{N}} & \text{\textbackslash{}textbf{V} \textbf{V}} \\
\end{array}
\]

With a syncopation (provided that it is accentuated by the other voice and is not through harmonic means made to resemble the normal un-syncopated measure rhythm) the relationships of accentuation in the measure are reversed. The previously unaccented part of the measure receives the accent; the accented part takes the less important place. The melody formulae, especially those which are more dependent upon the measure accent (\textbf{V}, \textbf{N}, \textbf{F}) than the others, can be used to confirm the syncopated "voice"; for example, by placing the tension of a \textbf{V} on a weak instead of on the normal strong measure point, and placing the resolution, on the other hand, upon an accented part. In many cases, with the application of this rule, nothing further will result than an exchange of meaning in the melodic formulae which brings with it only a change in name of some of the formulae tones in the harmonic analysis based on the degree-progression. Thus it is unimportant for the degree-progression whether the two tones designated \textbf{+} in Figure 186 are considered \textbf{N} or \textbf{D} (\textbf{N} or \textbf{N}). However, with some \textbf{V} \textbf{V} and \textbf{N} \textbf{N}, by means of the syncopated procedure the formulation of the degree-progression can often be made materially easier.

All this freedom of setting if awkwardly applied can become a veritable poison for two-voice settings. Whoever does not master it fully—and mastery shows itself in the flowing character of the voice-leading and in the ability to designate and to sing without error all that is written—should not use these forms. But even those who know how to arrange the work ingeniously must show by an especially searching analysis of the step-progression and of the melodic and harmonic degree-progressions that they are actually correctly applied.

The activated melodic model is subject to the same considerations as is the original active 2d voice; the step-progressions and the melodic degree-
progressions also must be extracted from it; and the quality of the progressions in it must be a measure for the build of the melody. The harmony degree-progression, which naturally does not possess any rhythmic independence, is, even with its shorter note values, an unfailing check upon the harmonic progression of the piece as a whole. If we wish to increase or decrease the frequency of harmonic change—which can be done independently of the tempo of the piece—it is easy, from the harmony degree-progression, to say where too much or too little harmonic motion takes place. By changing the tones of the degree-progression and adapting the tones of the now active model, the desired amount of harmonic change can readily be achieved.

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The many means of checking up on the technical construction of our exercises, dependable as they are in informing us of the value of the melodic and the harmonic development, leave us in complete doubt as to the stylistic design of a two-voice setting. It is entirely within the limit of our present technical ability to develop the following active voice, instead of the preceding one, from the melodic model:

In measure two one could conceive beyond this the following leading of the lower voice:

It would not be wrong in spite of its strange appearance at first glance. The degree-progression gives us exact information as to its value. This progression is the following:

which is naturally permitted according to the regulations of Chapter VII. Any strangeness lies entirely in the manner of notation.

In Figure 188 we note in the next to the last measure that it is not safe to let the melodic formulae have free sway at the same time in both voices. It is preferable to distribute the formulae so that they always occur in one voice when the other has an unaltered good interval tone, lest otherwise the coincidence of several formulae deprive the sound of all support, leaving it as it were suspended in the air.
Figure 188 shows that an elaboration of the original unassuming melodic model introduces a harmonic overrichness into the setting which does not suit it. It serves no purpose merely for the sake of more pungent harmonic intervals or more interesting voice leading to become styleless and to oppose such a modest upper voice with this expenditure of chromaticism, cross-relations, and piling up of formulae. Let the student now grow accustomed to economic use of the many and varied possibilities of employing his tone material. Above all, let him pay attention not only to technical clearness but also to the mutual agreement of the two voices in style and character. Concerning this no rules can be set up. Taste, which makes the decision in such questions, can be developed only through constant, highly critical observation of one's own work.

Whoever, in spite of the foregoing, holds that two-voice settings such as the last one can be worked out in our modest style of writing, has still to pass the highest and most important test. Can he, when he has written such a setting, sing each voice with someone else without effort or error? Most likely not, and thus, as far as he is concerned, we have definitely shown that his setting is not usable for our present demands. We shall not be unreasonable, however. If a student writes such settings, and if he can explain and sing them without error, we shall respect and reward the talent which is shown in such ingenuity. He may then write such things. But even for him it would be better to develop his taste along with his technique and apply such artifices only where they are appropriate.

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**EXERCISE 51**

a) Work out in the manner of Figure 187 all two-voice settings of Chapters III, IV and VI—those printed in the book as well as those resulting from the exercises in these chapters.
b) Criticize the new settings as to their stylistic structure.
c) Examine the elaborated melodic models for step-progressions; change them if necessary.
d) Examine the elaborated melodic models for melodic degree-progression; make changes if necessary.
e) Examine the degree-progression of the harmonic patterns of each total setting; make changes if necessary.
EXERCISE 52

a) Write a melodic model according to the rules of Chapter I.
b) Add, above or below, a 2d voice constructed according to the rules of Chapter II.
c) Extract the harmonic degree-progression and improve both voices in case the progression demands it.
d) Determine the $\Phi$ of the piece by means of the harmonic degree progression.
e) Lend the added voice active movement by means of melodic formulae and add the appropriate symbols for these.
f) Examine the step-progressions of the active voice; make changes if necessary.
g) Determine the melody degree-progression of the active voice; make changes if necessary.
h) Lend the melody-model freer motion; designate it with symbols and add to the previous active-voice changes in designation which may have become necessary.
i) Examine the step-progressions of the newly active melody-model; makes changes if necessary.
j) Determine its melody degree-progression; change, if necessary.
k) Extract again the degree-progression from the harmonies; consider it and compare it with the previously designated degree-progression under c. Change the course of the melody if necessary.
1) Determine the $\Theta$ and judge it.

m) Criticize the stylistic form of the whole piece.

The note added for the last exercise of Chapter VIII holds, in its entirety, for this exercise.

This is the work-procedure to which each two-voice exercise is henceforth to be subjected. It is a much magnified and hence coarsened presentation of all that the ear does in listening to such a setting; it hears and criticizes the step-progression, extracts the degree-progression of the separate lines and of the harmonies, and determines the tonal center. Only in the first steps of our exercise does the ear not play a role, since it does not elaborate a passive voice into an active voice. But in place of this it separates the added melody formulae from the nucleal sounds and thus in retrospect reproduces the unornamented form. It is self-evident that our work-procedure, which dissects the procedure of musical listening and understanding into its separate phases, taking it as the point of departure for the technical procedures, must in turn affect the auditory reaction. The ear is slowly trained to listen to the progressions and to weigh the values of sounds and relationships. This in turn suggests the question whether it is really necessary always to undertake these detailed analyses. The greater the sureness of the auditory perception of all the hidden currents of a setting, the less necessary will it be to consider all the demands of a minute analysis. One point after another will in time resolve itself. From the separate work-procedures one point after another will fall away, like the withered leaves of a tree; and, finally, the entire procedure will remain as a unified, uninterrupted, flowing combination of inventive technique. In this the detailed analysis serves merely to find possible means of improvement in passages requiring them by taking away here and adding there—in short by lending to the whole the final refinement. Nothing could be more disastrous, once such facility is attained, than constantly to restrict the procedure by thinking about steps, relationships, and formulae.

He who after thorough practice with these characteristics of writing and after diligent practical work in setting does not become so accustomed to the constant observation of the progressions, etc., that his ear, unconsciously and without reminding him thereof, analyzes constantly the sounds and lines in the sense here indicated, should be content with the mere recognition of these things and should not attempt to gain the rewards of actual composition; for meaningful and understandable compositions are attained only when the inspiration, the musical thoughts, of a composer can pass through the fine sieve of work-rules and restrictions of material without thereby being changed in their nature and their value. But even those musicians to whom a knowledge of tone-setting serves merely as a broadening of their general musical culture must reach the point at which the observing of all the many rules changes from a hindrance in the act of writing into a strong aid to hearing. They will then scarcely bring up the foolish objection that the analyses take up more space than the writing itself. Apart from the fact that the examining and analytical activity from now on is constantly more and more separated from productive work, nowhere is there set a measure for either the amount of effort or the time which must be expended in analyses. We are spoiled by the inadequate explanations of harmonic instruction. True, these are short; but what do they tell us other than the position of chord tones in relation to their bass tone and the simplest tonal relationships? How a chemist would laugh if one should demand of him that he complete the detailed analysis of a substance or object in the same short time which is needed for its well arranged production!
CHAPTER X
Free Two-Voice Setting: I

We have now acquired the skill to manipulate two active voices and, therefore, we can proceed to the final chapter of two-voice setting: the treatment of a melody-model progressing in free rhythm. For this we shall use folk-tunes from the Middle Ages and later periods, but in almost all cases examples written before Bach's time. It would be quite possible to use models from later periods; I shall restrict myself, however, to the older song material because in this the melody develops in the full freshness of unrestrained pleasure in linear design, without being hampered by overstressed harmonic considerations in the scheme of definite cadences and marked symmetrical phrase structure which later determines the form. These old songs thus give rich possibilities to a polyphonic treatment; above all, they are the ideal work-material for two-voice settings.

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At the beginning of such work we are confronted with the question: In which of the two main styles do we wish to formulate our settings? Shall we give melody the right to fill both voices with linear life, or shall we let the beauty of a melody rise above a broad, flat background of simple harmonies? Shall we write polyphonically or homophonically, linearly or statically, contrapuntally or harmonically? Without consideration of preference for one or another style, which continually changes according to localities, races, periods, and even according to the individual personality of the composer, a text-book of tone-setting must today make ready the technical tools for the polyphonic as well as for the homophonic style. The degree of our present technical ability permits us to apply our tonal material in the directions of both these technical opposites. However, we cannot—any more than could the masters in the free art of tone-setting of which they laid down the principles in their compositions—bring either one of the styles so to the fore that we get either pure counterpoint or solely a harmonic structure.

Just as in the smallest structural element—the interval—both forces, the melodic and the harmonic, are already inseparably operative, and we merely have the choice of moving one or the other into the foreground and there accentuating it, so we may have in the extended setting only predominatingly polyphonic or predominatingly homophonic progressions. We shall begin in Chapter X with the more readily mastered form, the homophonic.

A. Work-Material
I. Melody models to be placed in the upper voice.*

* This and all following melody-models are taken from Franz M. Böhme's "Altsdeutsches Liederbuch."
Die Fisch im Wasser wohnen, das Wild wohnt in dem Wald;  
Thus fish live in the water, wild beasts live in the wood;  

Daß sie tun sich mehr gar viel und man-nig-falt,  
That they themselves re pien ish so well and man-falt.

Ve - num, und dein Kind, seid ale bei-de blind, und  
You, thou and thy boy, are both of ye so blind, and

ich wohl hab er-fahren in meinen jun - gen Jah - ren.  
I so well have learned in my own youth ful lie - tag.

Yo - u • um - sich den, wer sich su such tut wen - den, wie  
they may well be blind - ed, who turn their gaze up - on thee, as

Du die schö ne Nann - erl ins Un - Glück ge - bracht,  
Thou the love - ly Nan - cy un - hap - py hast wrought.

Der Mai - en, der Mai - en, der bringt uns Blüm-lein viel.  
Ich The may-time, the may-time, it brings us flowers sweet.  

II. Melody models, which are to be developed as upper and as lower voice.
B. Work-Procedure

The purpose of the homophonic treatment of a melody-model of varying rhythmic activity is so to construct a second complementary supporting voice that the original melodic line blends with its companion, but, nevertheless, in all details is completely distinct from the harmonic foundation. That can occur only if the added voice never rises to the point of melodic self-sufficiency. It progresses in longer note-values than does its leader, and, at the most, becomes somewhat more active at the points where the other rests. Also, rhythmically and formally, it is subordinated to the main voice. It accentuates its rhythmic structure by placing its tones chiefly on the accented parts of the measures of the melody, and it confirms the form of the melody by aiding in the marking of sectional endings, caesuras, and cadences.

The full melodic preponderance of the melody model is served when the harmonies between the two voices are the good intervals of Group A and yield as little place as possible to the melodic formulae. In the main voice the simpler formulae (W D V) will probably be frequently found; the remaining ones should occur but rarely. The added voice, if the formulae occur frequently in it, would show too much inner tension and would also develop a strong resistance against the main voice. In the added voice, therefore, the formulae may occur only to the smallest possible extent; even W, D and V create a melodic development which disturbs the homophonic character. A V or even a N is among the greatest rarities in the 2d voice of such a setting. The harmony degree-progression shows plainly the clear, uncomplicated building of the harmonic relationships, on the support of which the melodic life can blossom free and undisturbed. The degree-progression moves chiefly in fifths and fourths, with occasional insertions of thirds and seconds—a sign that it is moving mainly within the closer degrees of relationship of a tonal center.

Before beginning the actual work of writing, we must determine the tonal structure of the given melody. (In Chapter VIII we learned how this is done.) We thus are informed specifically about the harmonic logic in the melodic development of a single tone-line. But as to the construction and order of the harmonies, we thus determine merely the $\Phi$ of the piece. That alone is a considerable help, but it does not indicate how the harmonies are to follow each other in developing a particular tonality. In order to find points of contact, we study the formal important points of the melody: its close and the sectional endings along its course. At these points we must have cadences in order to create a closing effect, and these cause a close association between the linear and the vertical elements by subordinating melody and harmony to the progressions of form. These are the points at which we can most readily adapt the 2d voice to the melody. From these cadence points, which are the fixed parts in the setting, we can develop the rest of the progression more effectively than by calculating one harmony after another from the beginning and adapting these to the demands of the whole harmonic structure in only a very limited way. The final interval (at least with our simple relationships) has the sound of $\Phi$. The tone representing the $\Phi$ must appear in the lower voice. This tone is the chief tone derived from the melody degree-progression, and is the basic tone of the series of relationships to be used in the harmony degree-progression.

The remaining cadences in the course of the melody are supplied with intervals, the root-tones of which are below. Moreover, in order not to distract the attention of the ear from the melody—which is always the most important part of the setting—we use in the degree-progression and in the lower voice the nearest possible related tones of the $\Phi$.

It may frequently occur that a melodic part-cadence (or even the final cadence) consists of two tones, of which the first stands at a better metrical point than the latter (feminine close as opposed to masculine, which ends on a good metrical point). If these two tones appear in the following forms,

\[ \text{the first can get the emphasis through its better metric position to such a degree that it maintains itself as root-tone of the harmonic cell even to the end of the second, the closing tone.} \]

Accordingly we shall here be frequently confronted with the question whether we should change the harmony between the two tones, or whether they should be linked by a common tone of the degree-progression. Feminine closes of which the last tone is itself the root-tone of the harmonic cell
are simpler to treat, since metric and harmonic closes here coincide; but even then we often have the choice between harmonic change and harmonic unity.

\[ \text{What should I then begin to do at best the way I've learned it through a new born song I'm singing. Fa-la-de-ri-dum.} \]

The \( \mathbf{\Phi} \) of this melody is \( g' \), supported mainly by its \( \mathbf{\Phi} \); whereas the \( \mathbf{\Omega} \) supplies only a subordinate function.

\[ \text{The partial closes on which the cadences must end are indicated in Figure 208 by an arrow. They are the four melody tones:} \]

If we wish to add a lower voice we shall obtain for each of these closes the following cadence possibilities:

\[ \text{The two } e_b^1 \text{ in 1 and 2, and the } a_b \text{ in 3, cannot be used because they make marked cross-relations with the melody-model. In 1 and 2, furthermore, the } c^1 \text{ is eliminated because this cadence will be used in 3, and it is inadvisable to destroy its fresh effect by using it earlier. For 1 and 2, therefore, only } g, g^1, \text{ and } e^1 \text{ remain. The cadence tone of the melody is } g^1 \text{ in both instances; at least once we shall have to use it also as root-tone of the part-cadence in the second voice. The closing cadence will not be affected thereby. The principal tone we have to use at least twice lest we should not discover the } \Phi. \text{ In order to eliminate all doubt it is advisable to use the cadence interval } g-g^1 \text{ immediately at the first part-cadence, so that it is at once clear in what tonal domain we are. The } e^1 \text{ then remains for the second cadence. The third cadence, by using an } a \text{ or } f, \text{ would overburden the little song needlessly and would be opposed to the harmonic style of this homophonic type of setting. There remains, accordingly, } c \text{ or } c^1; \text{ for the end the } g \text{ cannot be avoided. Thus we get for the second voice the closing root-tones } g, e, c, \text{ and } g, \text{ which we place below the model.} \]

\[ \text{In the simple, drastic form of harmony which we have selected, it is always advisable to support the } \mathbf{\Phi} \text{ with its immediately preceding } \mathbf{\Omega}. \text{ That can readily be done at the first cadence of the example.} \]

At the fourth cadence we should get with the \( e^1 \) of the melody an \( \mathbf{N} \) at this important melody point if the dominant tone \( d \) were in the 2d voice. This would add a rather marked tension to the exercise.

Here the 2d voice had better take the \( a \). We cannot use a \( \mathbf{\Phi} \) for the \( e \) of the second cadence, because the \( b \) may not be used with the \( a^1 \). Thus we can use the next most nearly related tone, the \( \mathbf{\Phi} \), either \( a \) or \( c \); or else we can do without the \( \mathbf{\Phi} \) and use \( f# \).
For the third cadence we can use neither the 6 nor the 9 of the final tone of the cadence. That is because the feminine close e¹-c¹ demands harmonic verification of the cellular linking of these two tones (which would best result if we added a c to the e¹ of the upper voice). Nevertheless, we shall not do this, because the relatively long delay on a single harmony would cause a serious halting of the auditory flow. Thus, e, g, a, b remain as possible tones preceding the already determined unison on c¹ of both voices. Of these four, the first three produce harmonic units for the entire sixth measure.

The applicability of a can be established as follows: the c¹ of the upper voice, which appears doubled in our cadence plan, tends, through this reinforcing, to maintain its root-tone character even when it is linked with another cellular harmony than c¹. Here, owing to the presence of a on the first half of the measure in the lower voice, the c¹ is only a 6 of the degree-progression tone a. The vain striving of c¹ for root-tone function is, nevertheless, so strong a refutation of the root-tone power of a that this version is not felt as a disturbing delay, with either e or g as first tone, 2d voice, in measure six. If b is used at this point, the harmony changes for the two measure-halfes (degree-progression is e-c).

The cadences, which require at least three tones of the degree-progression for their identification, are not yet completed. If at this point we should try to complete them, we might easily neglect too much the total course of the 2d voice in their favor. Accordingly, we now complete, in order, the remaining in-between parts. The missing cadence-tones will themselves then fit in.

At the beginning of the piece, the triple occurrence of the central tone g¹ in the upper voice suffices for determining the tonality; we do not, therefore, need to use the g again in the lower voice. Thus, e or c remains. The eb is omitted for the reason already given. The tones bᵇ and b, as constituent parts of an interval with root above, are not usable for beginning a piece. If the lower voice has c as first tone, the connection with the next measure, which is already given, may be made by inserting an e.
For the third phrase (measures five and six) the following possibilities exist:

9. +
8. ~
9. 1
10. ~

and for the last phrase (measures seven and eight) only the following:

of which the form a is preferable on account of the stronger interval b–d'. We get the best connection to this cadence of measures seven and eight by using any of the preceding forms which do not contain the note b, thus: 1, 3, 6, 7, 9, 10, 11.

Of these the less good are:
1 and 3, because they repeat the final tone of the second cadence; 7, because the melody has two NN, which, however, could occur for the sake of change; 9, because the connection to the b can be made only through the progression of a seventh and because an octave transposition of the last part of the entire lower voice would add an unwarranted rapid descent; 10, on account of the twice occurring g.

Thus 6 and 11 remain, of which 6 is to be preferred because 11, through the repetition of c just heard at the end of the second phrase, has not had so good an effect.

The NN in the melody for the first tone of form 6 is well placed, since we have allowed but little space to the melodic formulae, and a N does not occur at any other place.

Thus our piece appears:

The degree-progression is:

The twice-used d in the lower voice of the second and the third measure is somewhat monotonous. It could be avoided by an f# as first note of the second measure. Then, however, the degree-progression would stagnate and the harmony would not progress, which at this point would be the greater fault. Let us therefore retain the lesser. The markedly quiet measure 6 of the entire progression can be enlivened a bit by inserting a g in the lower voice.

The fourth measure can likewise be smoothed out by an inserted d.

We cannot criticize a 2d voice of this kind as severely as the other melodies fitted out with independent linearity. For in this type of 2d voice practically only strong harmonic steps occur, and, for the sake of harmonic effect, we almost completely dispense with separate melodic existence. In the melodic rudiments of the added voice in homophonic settings, neither the step-progression nor the melody degree-progression can be developed more than fragmentarily.

Now there remains only the setting of the text to the new voice. It is not the purpose of a text-book of tone-setting to present a complete course of musical declamation; it is, moreover, superfluous to load
upon the student in this field more than he now needs for our relatively modest demands. Besides, everyone is familiar with language from childhood. He knows how the words are to be accented and he will understand how to adapt the cadence of the written and the spoken sentences to the rhythm of the music if he leaves it to his natural feeling for language, without seeking for extraordinary associations. Nevertheless, three rules may be given him by following which he will be ready for all demands of our present work.

RULE 63.

Accented syllables — accented part of measure; at least (with syllables extending over several tones) an accented syllable should contain an accented metrical beat.

RULE 64.

If we have too many tones and too little text, we may repeat important words or parts of sentences or extend the main syllables over several tones.

RULE 65.

If we have too much text and too few tones, the text may be shortened by omitting unimportant words (adjectives, adverbs, etc.) or long tones may be subdivided into two or three shorter tones. If we are forced to use such tone repetitions, the effect may be dull and uninteresting if the change in syllabication takes place at the same time in both voices. Even in the homophonic style, therefore, it is advisable to set the voices against each other in regard to the text.

A case where too much text is to be set against a small number of tones confronts us in the 2d voice which we have constructed to go with Figure 207 (see Fig. 222). Through omission and repetition of tones the text, however, can be adapted to the new voice. Accordingly, our song has this final form:

EXAMPLE 1.

C. Model Examples
CHAPTER XI

Free Two-Voice Setting: II

We now arrive at the most important and most difficult but also the most beautiful style of writing which can be attained with two voices: that of two equally important voices—the contrapuntal, the polyphonic. If we had the desire in the preceding exercises to lift and to accent the melodic life of the model by giving it a firm unobtrusive harmonic foundation, we now give also to the 2d voice an independent melodic life. Its linearity now competes with that of the given melody; it opposes the climax points of the model with its own carefully calculated high points; it utilizes the same rich treasure of melodic formulas. Its melodic development can be so complete that it can then be used as melody-model of a new two-voice setting. And yet, in spite of this independence, which is felt even to the last note, the two voices should be most closely correlated and should affect the ear like an inseparable weave: an equally close but differently constructed combination from the one in the preceding homophonic style. There the melody-model rested upon the broadly spread harmonies; it was supported by their sound. Here the total sound is distributed between the two lines of tones, and carried by the separate melody parts of the two voices in their coinciding and diverging tendencies.

A. Work-Material

I. Melody-models, to be placed in the upper voice
Es ging ein wohl gezogener Knecht wohl über ein breites Grasgraum, die Harre stund am Wege, und Herr zu dem Lande kam.

Au - e, da sah er einen schönen Tanz von Männern und von Frauen, den Tanz, den wollt er schauen.

II. Melody-models to be treated both as upper and as lower voice.
B. Work-Procedure

The detailed description of the work-procedure in the preceding chapter serves just as well for the present problem; we must merely keep in mind that now we aim for the opposite goal. Instead of building the harmony on a supporting basis, we now seek to express it in less marked but for that reason more varied and more expressive outlines; we use the weaker sounds of our interval resources at least as often as the strong ones, and we no longer strive so eagerly for closest relationships in the degree-progression. The rhythmic course of the added voice is brought into greatest opposition to that of the model; the caesuras in the formal flow of both voices are now set against each other in an overlapping manner. The melodic line is developed to the most pronounced degree; melodic progressions of all kinds (not merely those in themselves prohibited) can greatly disturb the melodic flow; all such devices as cross-relations, wide leaps, and rich variety of motive, which detract from the desired result in homophonic style, can, on the other hand, be of pleasing effect in the contrapuntal style. This does not mean that these last mentioned devices should be overlooked, nor that the former are prohibited. In the polyphonic style everything may occur that could exist in the homophonic style, only it must aim at the goal of greatest melodic activity. Melodic lines are more sensitive than harmonic connections, awkwardnesses in them are more disturbing than poor harmonic successions. In working contrapuntally, therefore, there is a greater responsibility in deciding upon the means to be employed than there is in the putting together of intervals for a structure of homophonic style, where one strives more for a goal of external, sensuous beauty.

I urgently advise the avoidance of a device which is given such importance in books on counterpoint that it almost seems that the essence of polyphonic structure is exclusively expressed in this one way. I mean the use of imitation. Of course, imitation of themes and of melodic devices plays an important role in contrapuntal settings, and its use in teaching is recommended by the frequency with which it appears, especially in the music of earlier centuries, and by its importance as a constructive and decorative building unit for music of all styles. In teaching, however, in the realm of tone material with which the pupil has to work, it again and again becomes a cure-all which permits even the most untalented to worm out of all difficulties. Where invention and exact calculation fail, we can still help ourselves with an imitation. Entire fugues which meet all school rules, but which do not contain a single tone of music, can be built in this way.

In our exercises, therefore, the use of imitation is entirely dispensed with; rather, the creative ability is to be schooled by constantly finding new voice progressions without leaning slavishly upon the models. The learning of the important artistic device of imitative patterns is postponed until the student has so far steed his creativeness that he can conceive and employ it in its entire beauty and importance and not just use it as a crutch to feel his way forward with much effort—that is to say, until the attainment of a considerable command of three-voice and more-voice writing.
Wer mir zu trinken gab, den sing ich ein neues Lied.

Lied, all von der Frau von Luxemburg, wie sie ihren Landesherren verrät,

We select this song for working out, the progress of which is again carefully described in the following:

The melody degree-progression tells us that the \( \Theta \) of this song is \( g^1 \). It is supported by its \( D \) and has, on this account as well as through its beginning and final position, an advantage over \( f^1 \) and \( b h^1 \) which also strive strongly to assert themselves. The part cadences of the melody stand on \( f^1, a^1, f^1, \) and \( g^1 \). The \( a^1 \) of the second phrase-end has but little independence; it can, as part of the \( 23, a^2-d^2 \), be subordinated to the \( d^2 \), and we are thus confronted with the question whether this close is to be supplied with the harmony \( a \) or \( d \). The results of such determination are here not nearly so significant as in the homophonic style, since we do not at all put the caesuras of the 2d voice at the points indicated by the arrows, but instead shift them against those of the upper voice in order to make the melodic independence of the two voices that much clearer. With this, it is true, clearly noticeable cadences are removed; they would, with their strong accentuation of the formal structure, restrict the linear flow. The closing tone of a phrase, therefore, serves here scarcely more than as an approximate sign-post as to which direction we have to take. Only the last close must be reached with a legitimate cadence on \( g \), in order that the piece may be brought to a correct formal and harmonic end.

The problem for the first three measures is: to oppose the passivity and the thrice struck \( g^1 \) of the melody with pronounced tonal movement and tone change; to fill the second measure with tension; to place the caesura of the 2d voice (demanded by the text, by the breath control of the singer, and also by the listener's desire for comprehension) either before the end of the third measure or after the second half of the fourth measure.

The beginning could thus appear:

or, in case the many syncopations and dotted notes seem too heavy a burden for the simple song, in the following form:

The second part of the melody is itself richly active; we could, therefore, keep the opposing voice quieter. However, we are not, in this connection, entirely free in our decision. Since the new voice is to develop as independently as possible, we cannot, in case it has previously been active, suddenly slow it down except upon urgent need; instead, we must let the previously unfolding play of tones work itself out.

The continuation of both forms could be:
The first version, with its varied rhythm, its short note-values, needs a grouping into shorter parts in order to remain understandable. We have, therefore, not arrived with its second caesura as far as with the other version and equalize the difference as follows:

In order to maintain the tension throughout the example it is necessary that we set against the entirely step-wise progression of the model some leaps or marked contrary motion.

The text distribution in this song offers no difficulty, since we have sufficient tones to take care of the words. The song, in its two contrapuntal conceptions, supplied with text, then shows the following form:

The melodic independence of the new voice brings with it—far more than with the 2d voices of Chapter X—the possibility of attacking it by means of step-progression and melody degree-progression. The student
should examine it in this connection; he should also construct the degree-progression for the harmonies of both settings.

**EXERCISE 54**

a) Find the step-progressions of the added voices of both settings.
b) Extract their melody degree-progressions.
c) Write out both harmony degree-progressions.

**C. Model Examples**

**EXAMPLE 1.**

```
<table>
<thead>
<tr>
<th>Musicianship</th>
<th>Language</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ah, Gott, whom shall I plead then my pain.</td>
<td>Oh God, whom shall I plead then my pain.</td>
</tr>
<tr>
<td>I shall weep for my heart, my soul shall weep.</td>
<td>I shall weep for my heart, my soul shall weep.</td>
</tr>
<tr>
<td>Which I have chosen, the maid,</td>
<td>Which I have chosen, the maid,</td>
</tr>
<tr>
<td>I'll not lose her.</td>
<td>I'll not lose her.</td>
</tr>
<tr>
<td>For a dark-eyed maid I have chosen,</td>
<td>For a dark-eyed maid I have chosen,</td>
</tr>
<tr>
<td>And an other maid she has chosen me.</td>
<td>And an other maid she has chosen me.</td>
</tr>
</tbody>
</table>
```

**EXAMPLE 2.**

```
<table>
<thead>
<tr>
<th>Musicianship</th>
<th>Language</th>
</tr>
</thead>
<tbody>
<tr>
<td>Es saa ein Eul, es saa ein Eul und spun, es saa ein Eul und spun.</td>
<td>There sat an owl, there sat an owl and spun, there sat an owl and spun.</td>
</tr>
<tr>
<td>And spun and spun in some so dark-ened chamber small and watched me evil-eyed.</td>
<td>And spun and spun in some so dark-ened chamber small and watched me evil-eyed.</td>
</tr>
</tbody>
</table>
```

**EXERCISE 55**

a) Write out the step-progression of the added voices in the two preceding examples.
b) Add to both voices the symbols for the melodic formulae.
c) Extract the melody degree-progression of the added voices.
d) Extract the harmony degree-progression of the intervals.

**EXERCISE 56**

Work out the ten melody models given as work material as two-voice settings of polyphonic character and proceed with the completed settings exactly as described in Exercise 55.

We have now arrived at the end of the two-voice work. Whatever could be completely used in this attractive but restricted style of writing has been given to the student in all detail. The secrets of melodic and harmonic procedures unfolding in the play of melodic linearity should now be open to him, with the help of the step-progressions and the melody degree-progressions. In this field, he is supplied with sufficient knowledge to permit him, after thorough practice, to understand the structure and development of all melodic phenomena, whether these concern the highly developed
linear art of Gregorian Song or the curves of Gothic melody; whether he is considering the melodies of Bach’s period or those of the later classic or romantic styles; or whether he places the melodies of our time under the magnifying glass.* Even in melodies the style of which is unfamiliar to the student the composer will be revealed to him in even the most concealed refinements of his art. He does not thereby receive any evidence of the spiritual content of a linear progression—heaven be praised that this cannot be dealt with in progressions and other fixed means. Nevertheless, one is now no longer restricted to seeking information of things in mere aesthetic judgment; for the material of tone-setting can be comprehended in the smallest detail just as well as the orthography or the syntax of a literary piece.

We have not yet entered equally far into the domain of simultaneous sounds, or into the secrets of harmony. Nor would this have been possible with the scant harmonic results accruing from the chordally-so-ascetic two-voice setting! The miraculous effects of tone relations through which the entire broad domain of tone is surveyed; the root-tone determinants of the intervals, upon which depend the weight and physiognomy of all sounds of two or more tones; the countless possibilities of the introduction of melodic formulae, upon which the activating of the sound masses is based; the marked significance of step-progression analysis for the knowledge of harmonic procedures—of all these things, two-voice setting can give but a hint, compared with the important function which they fulfill in settings of more than two voices. Much as we have learned about them, eagerly as we have concerned ourselves with their application, we shall arrive at the full appreciation of their limitless effects in the technique of writing only when we are entrusted with the well-nigh inconceivable treasure of auditory experiences in the working out of three voices. The third volume of this treatise will lead into this new field of work.

* Book I of this work (pp. 229-250), contains analyses of portions of the following works:
  * *Dies Irae* (13th-century Chant)
  * Ballade “*Il m’est avis*” (Guillaume de Machaut, 14th century)
  * *Three-Part Invention* in F minor (J. S. Bach)
  * *Tristan und Isolde*—Prelude (Wagner)
  * *Sonata* for piano (Stravinsky)
  * *Klavierstück*, op. 33a (Schoenberg)
  * *Mathis der Maler*—Prelude (Hindemith)